



**higher education  
& training**

Department:  
Higher Education and Training  
**REPUBLIC OF SOUTH AFRICA**

# **NASIENRIGLYN**

**NATIONALE SERTIFIKAAT**

**MEGANOTEGNIEK N6**

**30 Julie 2021**

**Hierdie nasienriglyn bestaan uit 12 bladsye.**

**VRAAG 1**

- 1.1
- Eenvormige-slytasie-teorie is gebaseer op die aanname dat slytasie eenvormig is oor die totale kontakoppervlak voorkom✓ en met die toestand van 'n ou, geslyte koppelaar ooreenkom.✓
  - Eenvormige-druk-teorie is gebaseer op die aanname dat die druk eenvormig oor die totale kontakoppervlak versprei is✓ en met die toestand van 'n nuwe koppelaar wat nie geslyt is nie, ooreenkom.✓ (2 × 1½) (3)

$$1.2.1 \quad = \frac{2\pi NT}{60}$$

$$220 \times 1000 = \frac{2\pi \times 900 \times T}{60} \checkmark$$

$$T = 2334,272N.m \checkmark$$

$$T = \frac{2334,272N.m}{2}$$

$$T = 1167,136N.m \checkmark$$

(3)

$$1.2.2 \quad T = \mu \times p \times \frac{2}{3}\pi(R^3 - r^3)n$$

$$1167,136 = 0.3 \times 260000 \times \frac{2}{3}\pi(0.225^3 - r^3) \checkmark$$

$$r^3 = 4.246 \times 0.001 \checkmark$$

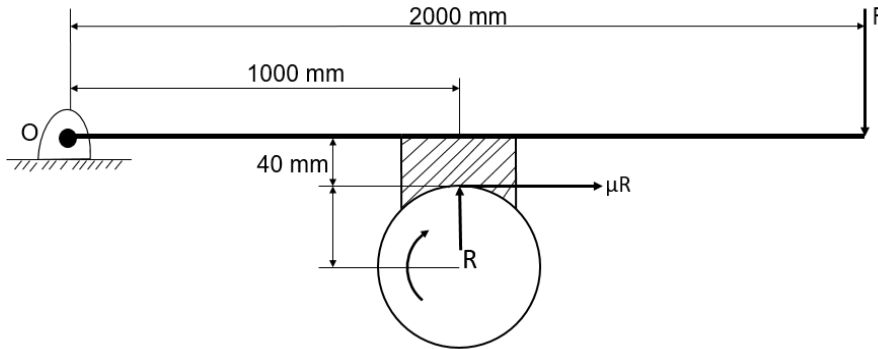
$$r = 0.162 \checkmark$$

$$d = 324 \text{ mm} \checkmark$$

(4)

**[10]**

**VRAAG 2**



2.1  $D = 400\text{mm} = 0,4\text{ m}$   
 $T = 200\text{ Nm}$   
 $N = 600\text{ r/mm}$   
 $\mu = 0,3$   
 $T = \mu R \times r$   
 $200 = 0,3R \times 0,2\checkmark$   
 $R = 3333,333\text{N}\checkmark$  (2)

2.2 **Neem momente om O:**  
 $\sum \text{kloksgewyse momente} = \sum \text{teenkloksgewyse momente}$   
 $F \times 2 = 3333,333 \times 1) + (0,3 \times 3333,33) \times 0,04\checkmark$   
 $F = \frac{3373,333}{2}\checkmark$   
 $F = 1686,667\text{N}\checkmark$  (3)

2.3  $P = \frac{2 \times \pi \times N \times T}{60}$   
 $P = \frac{2 \times \pi \times 600 \times 200}{60}$   
 $Krag = 12566,37\text{ N} \checkmark$   
 $= 12,566\text{ kN} \checkmark$

Alternatiewe antwoord

$$v = \frac{\pi \times D \times N}{60}$$

$$= \frac{\pi \times 0,4 \times 600}{60}$$

$$= 12,566\text{ m/s} \checkmark$$

$Krag = \mu R \times v = 1\,000 \times 12,566$   
 $= 12,566\text{ kW}\checkmark$  (2)

2.4 Bandremme  $\checkmark$   
 Blok-en-bandremme  $\checkmark$  (2 × 1/2) (1)  
**[8]**

**VRAAG 3**

3.1

$$P = \frac{2\pi NT}{60}$$

$$20 \times 10^3 = \frac{2\pi \times 300 \times T}{60}$$

$$T = 636,62 \text{ N}\cdot\text{m} \checkmark$$

$$T = (T_1 - T_2)r$$

$$T_1 = 2,5T_2$$

$$636,62 = 1,5T_2 \times 0,225$$

$$T_2 = 1886,28 \text{ N} \checkmark$$

$$T_1 = 4715,70 \text{ N} \checkmark$$

Alternatiewe antwoord

$$v = \frac{\pi \times D \times N}{60}$$

$$= \frac{\pi \times 0,45 \times 300}{60}$$

$$= 7,0686 \text{ m/s} \checkmark$$

$$20 \times 10^3 = (T_1 - T_2)v$$

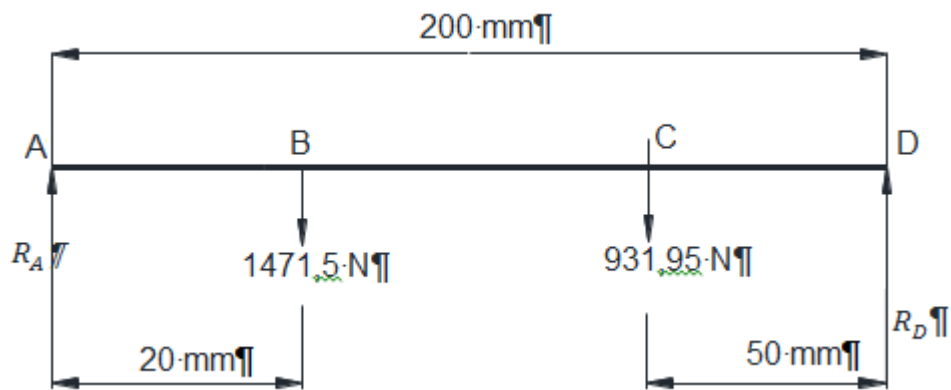
$$20 \times 10^3 = 1,5T_2 \times 7,0686$$

$$T_2 = 1886,28 \text{ N} \checkmark$$

$$T_1 = 4715,7 \text{ N} \checkmark$$

(3)

3.2



Neem momente om A:

$$\sum \text{kloksgewyse momente} = \sum \text{teenkloksgewyse momente}$$

$$(1\,471,5 \times 20) + (931,95 \times 150) = R_D \times 200 \checkmark$$

$$29\,430 + 139\,792,5 = R_D \times 200 \checkmark$$

$$R_D = \frac{169\,222,5}{200}$$

$$R_D = 846,113 \text{ N} \checkmark$$

(3)  
[6]

**VRAAG 4**

$$\begin{aligned}
 4.1 \quad m &= \rho \times v \\
 m &= 7\,500 \times \pi(1,2^2 - 0,9^2) \times 0,15 \\
 m &= \frac{2226,604}{4} = 556,65 \text{ kg} \checkmark \\
 I &= mk^2 \\
 I &= 556,65 \left( \frac{0,6^2 + 0,45^2}{2} \right) \\
 I &= 156,558 \text{ kg} \cdot \text{m}^2 \checkmark \quad (2)
 \end{aligned}$$

$$\begin{aligned}
 4.2 \quad E_K &= \frac{1}{2} I (\omega_f^2 - \omega_i^2) \\
 E_K &= \frac{1}{2} (156,558) [(2\pi \times 6)^2 - (2\pi \times 4,5)^2] \checkmark \\
 E_K &= 48\,672,714 \text{ kJ} \checkmark \quad (2)
 \end{aligned}$$

$$\begin{aligned}
 4.3 \quad &= E_K \times \text{ponsslae(siklusse)} / s \\
 P &= \frac{48\,672,714 \times 25}{60} \checkmark \\
 P &= 20,280 \text{ kW} \quad (2)
 \end{aligned}$$

**[6]**

**VRAAG 5**

$$\begin{aligned}
 5.1 \quad \text{Helikshoek } \tan \theta &= \frac{\text{leiding}}{\pi \times \text{gemiddelde middellyn}} \\
 \tan \theta &= \frac{2 \times 15}{\pi \times 80} = 0,1194 \\
 \theta &= 6,807^\circ \checkmark
 \end{aligned}$$

$$\text{Wrywingshoek } \tan \phi = 0,045$$

$$\phi = \tan^{-1} 0,045 = 2,577^\circ \checkmark$$

Die rendement van die wurm is:

$$\begin{aligned}
 \eta_{\text{wurm}} &= \frac{\tan \theta}{\tan(\theta + \phi)} \times 100\% = \frac{\tan 6,807}{\tan(6,807 + 2,577)} \times 100\% \checkmark \\
 &= \frac{0,1194}{0,1653} \times 100\% = 72,23\% \checkmark \quad (4)
 \end{aligned}$$

$$\begin{aligned}
 5.2 \quad \text{Krag}_{\text{wurm}} &= \frac{P_{\text{uit}}}{\eta_{\text{wurm}}} \times 100\% \\
 &= \frac{28000}{0,7223} = 39,457 \text{ kW} \checkmark \quad (1)
 \end{aligned}$$

5.3 1 rev van wurm =  $2 \times 15 = 30$  mm op wurm

$$\text{Draaispoed van die wurm in sekondes} = \frac{1680}{60} = 28 \text{ r/s} \checkmark$$

$$\text{Lineêre snelheid van die wurm, } v = 0,03 \times 28 = 0,84 \text{ m/s} \checkmark$$

$$P_{\text{uit}} = F_{\text{wurmrat}} \times v$$

$$F_{\text{wurmrat}} = \frac{P_{\text{uit}}}{v} = \frac{28000}{0,84} = 33,929 \text{ kN} \checkmark$$

(3)

5.4  $T_c = F_{\text{wurm}} \times R \times \mu$

$$T_c = 33,929 \times \frac{0,075}{2} \times 0,045 \checkmark$$

$$= 57,255 \text{ n.m} \checkmark$$

(2)

**[10]****VRAAG 6**

6.1.1 Die kantingshoek  $\theta$

*Kanting van die draai =  $\sin\theta \times$  spoorwydte*

$$\sin\theta = \frac{\text{kanting van die draai}}{\text{spoorwydte}}$$

$$= \frac{0,1}{1,2}$$

$$\theta = 4,78^\circ \checkmark$$

(1)

6.1.2 Die maksimum snelheid

$$v = \sqrt{\tan\theta \times rg}$$

$$v = 31 \text{ km/h} = \frac{31 \times 1000}{60 \times 60} = 8,611 \text{ m/s} \checkmark$$

$$8,611 = \sqrt{\tan(4,78) \times r \times 9,81}$$

$$8,611^2 = \tan(4,78) \times r \times 9,81 \checkmark$$

$$r = \frac{8,611^2}{\tan(4,78) \times 9,81} = 90,39 \text{ m} \checkmark$$

(3)

6.1.3  $F_g + mg \sin\theta = F_c \cos\theta$

$$F_g = F_c \cos\theta - mg \sin\theta$$

$$F_g = \frac{m \times v^2}{r} \cos\theta - mg \sin\theta$$

$$v = \frac{72 \times 1000}{60 \times 60} = 20 \text{ m/s} \checkmark$$

$$F_g = \frac{3000 \times 20^2}{90,39} \cos 4,78 - 3000 \times 9,81 \times \sin 4,78 = 10,78 \text{ kN} \checkmark \checkmark \checkmark$$

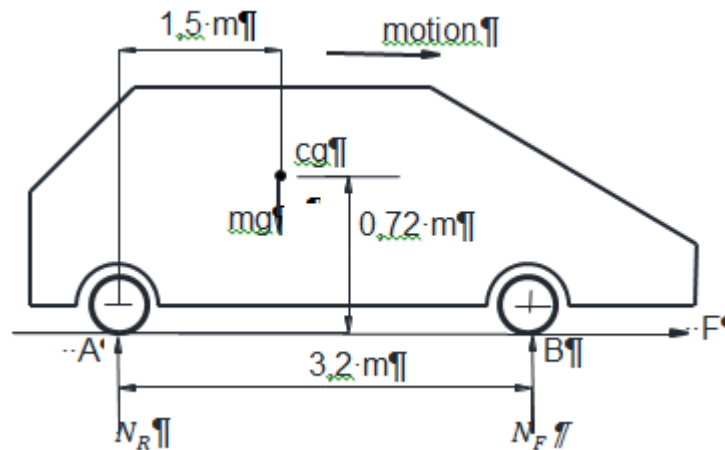
(4)

6.2 6.2.1 Lokomotieftrekkrag is die krag wat die lokomotief by die dryfwiele moet uitoefen om self en die waens of die trein te beweeg.

6.2.2 Trekstangkrag is die krag wat aan die agterkant van die lokomotief vir die trek van die trokke beskikbaar is.

(2 × 1) (2)

6.3 6.3.1



Neem momente om A:

$$\sum \text{klokgewyse momente} = \sum \text{teenklokgewyse momente}$$

$$mg \times 1,5 = N_F \times 3,2$$

$$N_F = \frac{1,5 \times mg}{3,2} = 0,469 mg \checkmark$$

$$F_{rem} = \mu N_F$$

$$ma = 0,35 \times 0,468 mg$$

$$a = 0,35 \times 0,468 \times 9,81 = 1,607 \text{ m/s}^2$$

$$= -1,607 \text{ m/s}^2 \checkmark$$

$$s = \frac{v^2 - u^2}{2a}$$

$$\text{maar } u = \frac{97,2 \text{ km}}{h} = \frac{97,2 \times 1000}{60 \times 60} = 27 \text{ m/s}$$

Die afstand word gegee as:

$$s = \frac{0^2 - 27^2}{2 \times (-1,607)} = 226,82 \text{ m} \checkmark$$

(3)

## 6.3.2

## Agterwielremme

Neem momente aangaande B

$$\sum \text{Kloksgewyse momente} = \sum \text{Antikloksgewyse momente}$$

$$N_R \times 3,2 = mg \times (3,2 - 1,5)$$

$$N_R = \frac{mg \times 1,7}{3,2} = 0,531mg \quad \checkmark$$

$$F_{\text{braks}} = \mu N_R$$

$$ma = 0,35 \times 0,531 \times m \times 9,81$$

$$a = 0,35 \times 0,531 \times 9,81 = 1,823 \text{ m/s}^2$$

$$= -1,823 \text{ m/s}^2 \quad \checkmark$$

Die afstand is gee as:

$$s = \frac{v^2 - u^2}{2a} = \frac{0^2 - 27^2}{2 \times (-1,823)} = 199,945m \quad \checkmark$$

(3)



## 6.3.3 Voor- en agterwiele rem:

$$F_{rem} = \mu N_F + \mu N_R = \mu(N_F + N_R)$$

$$\mathbf{maar} \quad mg = N_F + N_R$$

$$ma = \mu mg$$

$$a = \mu g = 0,35 \times 9,81 = 3,435 \text{ m/s}^2 \checkmark$$

$$a = -3,435 \text{ m/s}^2$$

Die afstand word gegee as:

$$s = \frac{v^2 - u^2}{2a} = \frac{0^2 - 27^2}{2 \times (-3,435)} = 106,114 \text{ m} \checkmark \quad (2)$$

6.3.4 Vir verhouding:  $N_F : N_R$ 

$$F_{rem} = \mu(N_F + N_R)$$

Neem momente om die ewewigspunt:

$$\sum \text{kloksgewyse momente} = \sum \text{teenkloksgewyse momente}$$

$$(F_{rem} \times \text{afstand vanaf ep na die pad}) + (N_R \times 1,5) = (N_F \times 1,7)$$

$$\mu(N_F + N_R)0,72 + 1,5N_R = 1,7N_F$$

$$0,35(N_F + N_R)0,72 + 1,5N_R = 1,7N_F \checkmark$$

$$0,252N_F + 1,752N_R = 1,7N_F$$

$$1,7N_F - 0,252N_F = 1,752N_R$$

$$1,5N_F = 1,752N_R$$

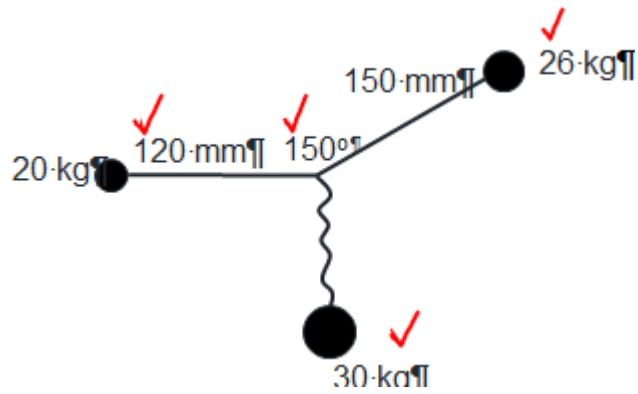
$$\frac{N_F}{N_R} = \frac{1,752}{1,5} = \frac{1,168}{1} \checkmark$$

(2)

**[20]**

**VRAAG 7**

7.1.



(4)

7.2

Vlak	Massa (kg)	r(m)	mr(kg.m)
A	20	0,12	2,4
B	26	0,15	3,9
C	30	x	30x

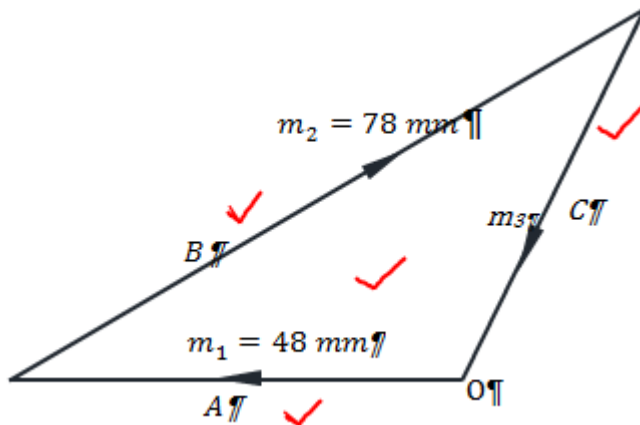
✓

✓

✓

(3)

7.2



(4)

7.2. Kragtediagram

Die sentrifugale krag van  $m_3$  is:

$$20 \text{ mm} = 1 \text{ kg} \cdot \text{m}$$

$$43,9 \text{ mm} = \frac{43,9 \text{ mm}}{20 \text{ mm}} \times 1 \text{ kg} \cdot \text{m} = 2,195 \text{ kg} \cdot \text{m} \checkmark$$

Die afstand van  $m_3$  vanaf senter O van die vlakplaat:

$$30x = 2,193$$

$$x = \frac{2,193}{30} = 0,0731 \text{ m} = 73,1 \text{ mm} \checkmark \checkmark$$

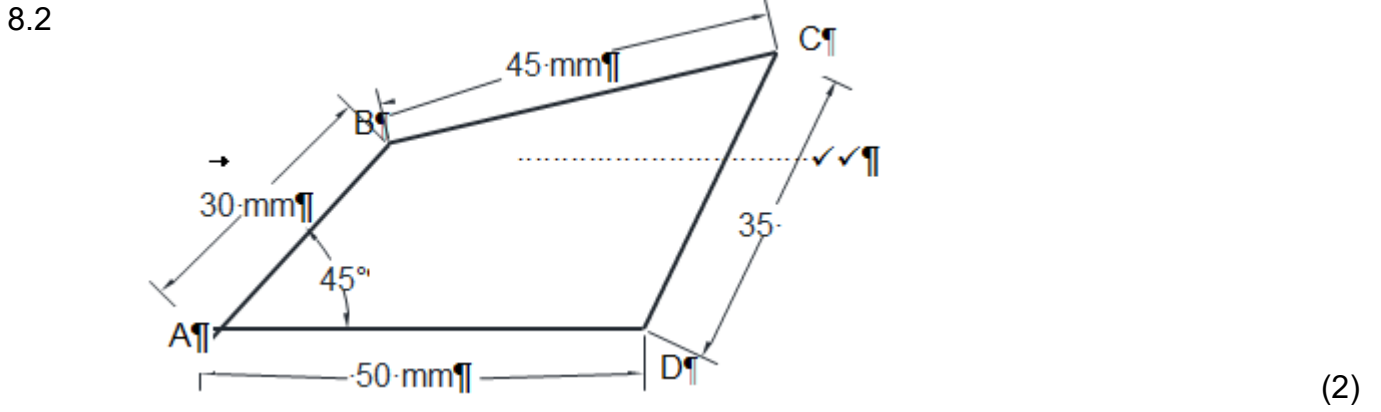
Die posisie van  $m_3$  tot vlak A is  $244^\circ$  kloksgewys en  $116^\circ$  tot A. ✓

(4)

[15]

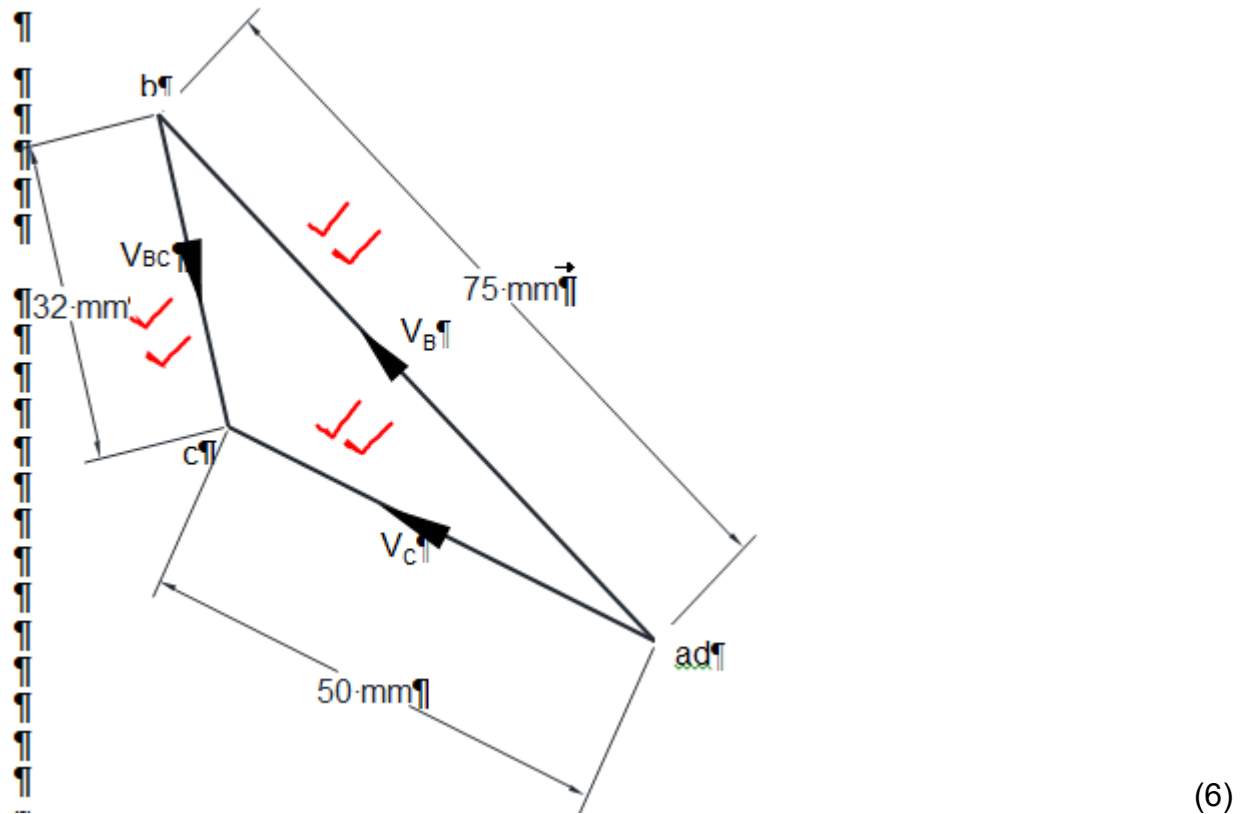
**VRAAG 8**

8.1  $AB = 30\text{ mm}$   $BC = 45\text{ mm}$   $CD = 30\text{ mm}$   $DA = 50\text{ mm}$   
 $V_B = \omega_{AB} \times AB = 5 \times 0,03 = 0,15\text{ m/s}$  ✓ (1)



Ruimtediagram

Skaal = 0,1 m/s = 50 mm



Snelheidsdiagram:

$$\text{Skaal } 0,1 \text{ m/s} = 5 \text{ mm}$$

$$ab = 75 \text{ mm}$$

Vanaf die snelheidsdiagram:

$$\text{Meting } bc = 32 \text{ mm} = 0,064 \text{ m/s}$$

$$\omega_{BC} = \frac{0,064}{0,046} = 1,422 \text{ rad/s} \checkmark$$

$$\text{Meting } cd = 35 \text{ mm} = 0,07 \text{ m/s}$$

$$\omega_{CD} = \frac{0,07}{0,035} = 2 \text{ rad/s} \checkmark$$

(2)

$$\begin{aligned} 8.2 \quad \text{Sentripetale skv van A relatief tot B} &= \omega_{AB}^2 \times AB \\ &= 5^2 \times 0,03 = 0,75 \text{ m/s}^2 \checkmark \end{aligned}$$

$$\begin{aligned} \text{Raaklynige skv van A relatief tot B} &= \alpha_{AB} \times B \\ &= \alpha_{AB} \times B = 19 \times 0,03 = 0,57 \text{ m/s}^2 \checkmark \end{aligned}$$

$$\text{Skaal } 0,75 \frac{\text{m}}{\text{s}^2} = 75 \text{ mm}$$

$$\begin{aligned} \text{Sentripetale skv van B relatief tot C} &= \omega_{BC}^2 \times BC \\ &= 1,422^2 \times 0,045 = 0,090 \text{ m/s}^2 \checkmark \end{aligned}$$

$$\begin{aligned} \text{Sentripetale skv van C relatief tot D} &= \omega_{CD}^2 \times CD \\ &= 2^2 \times 0,035 = 0,14 \text{ m/s}^2 \end{aligned}$$

Vanaf die versnellingsdiagram:

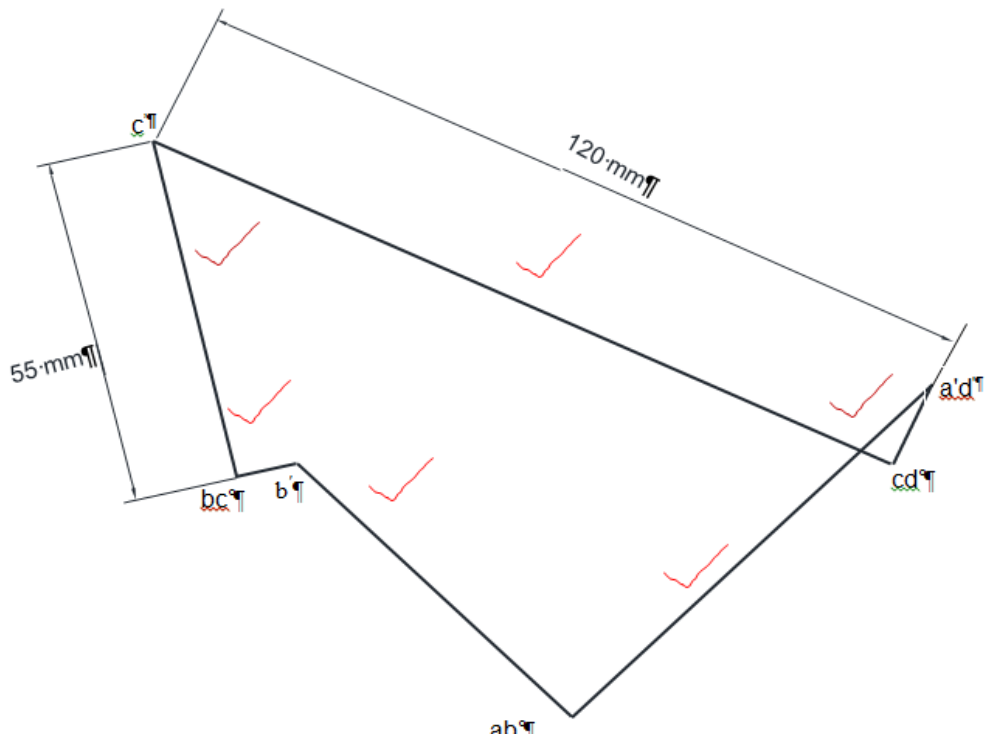
$$\text{Meting } c'bc = 55 \text{ mm} = \frac{0,75}{75} \times 55 = 0,55 \text{ m/s}^2 \checkmark$$

$$\text{Meting } c'dc = 120 \text{ mm} = \frac{0,75}{75} \times 120 = 1,2 \text{ m/s}^2 \checkmark$$

$$\alpha_{BC} = \frac{0,55}{0,045} = 12,22 \text{ rad/s}^2 \checkmark$$

$$\alpha_{CD} = \frac{1,2}{0,035} = 34,29 \text{ rad/s}^2 \checkmark$$

(7)



(7)  
(14)  
**[25]**

**TOTAAL: 100**