



**higher education
& training**

Department:
Higher Education and Training
REPUBLIC OF SOUTH AFRICA

MARKING GUIDELINE

NATIONAL CERTIFICATE

MECHANOTECHNICS N6

4 APRIL 2018

This marking guideline consists of 6 pages.

QUESTION 1

$$1.1 \quad 1.1.1 \quad T = \frac{P \times 60}{2\pi N}$$

$$T = \frac{25\ 000 \times 60}{2\pi \times 1\ 200} \checkmark \\ = 198,94 \text{ Nm} \checkmark \quad (2)$$

$$1.1.2 \quad R_f = \frac{100+75}{2} \\ = 87,5 \text{ mm} \checkmark \\ T = \frac{\mu \times F_A \times R_f}{\sin \theta} \\ F_A = \frac{198,94 \times \sin 15^\circ}{0,28 \times 0,0875} \checkmark \\ = 2\ 101 \text{ N} \checkmark \quad (3)$$

$$1.1.3 \quad F_{eng} = F_A \left(1 + \frac{\mu}{\tan \theta} \right) \\ = 2\ 101 \left(1 + \frac{0,4}{\tan 15^\circ} \right) \checkmark \\ = 5\ 237 \text{ N} \checkmark \quad (2)$$

$$1.2 \quad \frac{T_1}{T_2} = \left[\frac{1+\mu \tan \theta}{1-\mu \tan \theta} \right]^n \\ = \left[\frac{1+0,35 \tan 5^\circ}{1-0,35 \tan 5^\circ} \right]^{15} \checkmark \\ = 2,51 \checkmark \\ P = (T_1 - T_2) \times \nu \\ T_1 - T_2 = \frac{200 \times 10^3 \times 60}{\pi \times 0,6 \times 650} \checkmark \\ = 9794 \text{ N} \checkmark \\ \therefore 2,51 T_2 - T_2 = 9794 \checkmark \\ T_2 = 6486 \text{ N} \checkmark \\ T_1 = 16280 \text{ N} \checkmark$$

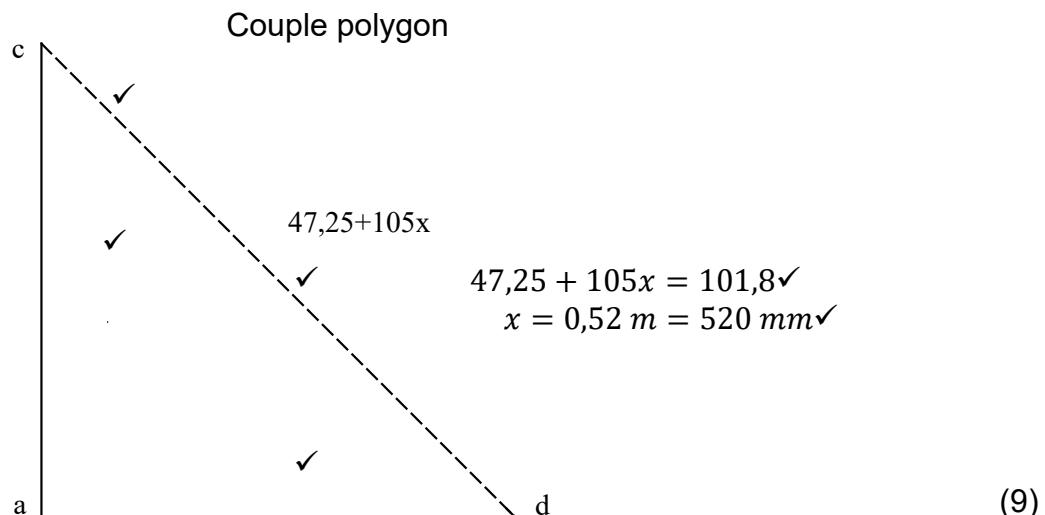
$$\sum \curvearrowright M = \sum \curvearrowright M \\ F \times 550 + T_2 \times 50 = T_1 \times 150 \checkmark \\ \therefore F \times 550 + 16280 \times 50 = 6486 \times 150 \checkmark \\ \therefore F = 288,9 \text{ N} \checkmark \quad (10) \\ [17]$$

QUESTION 2

2.1

Plane	$m \text{ (kg)}$	$r \text{ (m)}$	$mr \text{ (kg.m)}$	$l \text{ (m)}$	$mrl \text{ (kg.m}^2)$
A	6	30	180	-0,4	0
B	m	42	42m	0	0,375
C	4	40	160	0,45	0,844
D	3	35	105	0,45 + x	47,25 + x

✓ ✓ ✓



2.2

2.2.1

$$\begin{aligned}
 P &= (T_1 - T_2) \times v & \frac{T_1}{T_2} &= e^{\mu\theta} \\
 T_1 - T_2 &= \frac{35 \times 10^3 \times 60}{\pi \times 0,9 \times 600} & &= e^{0,25\pi} \\
 T_1 - T_2 &= 1238 \text{ N} \checkmark & &= 2,19 \checkmark \\
 2,19T_2 - T_2 &= 1238 \text{ N} \\
 T_2 &= 1040 \text{ N} \checkmark \\
 T_1 &= 2278 \text{ N} \checkmark
 \end{aligned}$$

(4)

$$\begin{aligned}
 2.2.2 \quad T_s &= \frac{P \times 60}{2 \times \pi \times N} \\
 &= \frac{35 \ 000 \times 60}{2 \times \pi \times 600} \checkmark \\
 &= 557 \text{ Nm} \checkmark
 \end{aligned}$$

(2)

$$\begin{aligned}
 2.2.3 \quad T_p &= \frac{35 \ 000 \times 60}{2 \times \pi \times 1500} \\
 &= 222,8 \text{ Nm} \checkmark
 \end{aligned}$$

(1)

$$\begin{aligned}
 2.2.4 \quad F_t &= \frac{T \times 2}{PCD} \\
 &= \frac{222,8 \times 2}{0,12} \\
 &= 3713 \text{ N} \checkmark \\
 F_r &= F_t \sec \varphi \checkmark \\
 F_r &= 3713 \sec 20^\circ \\
 &= 3951 \text{ N} \checkmark
 \end{aligned}$$

(3)

[19]

QUESTION 3

$$\begin{aligned}
 3.1 \quad m &= \rho \times V \\
 &= \rho \times \pi(R^2 - r^2) \times w \checkmark \\
 &= 7\,300 \times \pi(0,45^2 - 0,3^2) \times 0,2 \checkmark \\
 &= 516 \text{ kg} \checkmark
 \end{aligned} \tag{3}$$

$$\begin{aligned}
 3.2 \quad I &= mk^2 \\
 &= 1/2m(R^2 + r^2) \checkmark \\
 &= 1/2 \times 516(0,45^2 + 0,3^2) \checkmark \\
 &= 75,465 \text{ kg m}^2 \checkmark
 \end{aligned} \tag{3}$$

$$\begin{aligned}
 3.3 \quad \omega_1 &= \frac{2\pi \times 210}{60} & \omega_2 &= \frac{2\pi \times 132}{60} \\
 &= 21,99 \text{ rad/s} \checkmark & &= 13,82 \text{ rad/s} \checkmark \\
 E_k &= \frac{1}{2} I (\omega_1^2 - \omega_2^2) \\
 E_k &= \frac{1}{2} \times 75,465 (21,99^2 - 13,82^2) \checkmark \\
 &= 11,039 \text{ kJ} \checkmark
 \end{aligned} \tag{4}$$

$$\begin{aligned}
 3.4 \quad t_a &= \frac{60}{\frac{12}{\omega_1 - \omega_2}} - 1,2 \\
 &= 3,8 \text{ seconds} \checkmark \\
 \alpha &= \frac{\omega_1 - \omega_2}{t} \\
 &= \frac{21,99 - 13,82}{3,8} \checkmark \\
 &= 2,15 \text{ rad/s}^2 \checkmark \\
 T &= I \times \alpha \\
 &= 75,465 \times 2,15 \checkmark \\
 &= 162,2 \text{ Nm} \checkmark
 \end{aligned} \tag{5}$$

$$3.5 \quad P_m = E_k \times n/s \\ = 11,039 \times 12/60 \checkmark \\ = 2,21 kW \checkmark \quad (2)$$

QUESTION 4

$$\begin{aligned}
 4.1 \quad \tan \theta &= \frac{p \times n}{\pi \times D_m} \\
 &= \frac{15 \times 2}{\pi \times 75} \\
 &= 0,1273 \checkmark \\
 \therefore \theta &= 7,26^\circ \checkmark \\
 \emptyset &= \tan^{-1} \mu \checkmark \\
 &= \tan^{-1} 0,03 \checkmark \\
 &= 1,72^\circ \checkmark \\
 \eta &= \frac{\tan 7,26}{\tan(7,26+1,72)} \times 100 \checkmark \\
 &= 80,6 \% \checkmark
 \end{aligned} \tag{7}$$

4.2 $P_w = \frac{P_o \times 100}{\eta}$
 $P_w = \frac{20 \times 100}{80,6} \checkmark$
 $= 24,8 \text{ kW} \checkmark$ (2)

4.3 $1 \text{ rev of worm} = 2 \times 15 = 30 \text{ mm} \checkmark$
 $1200 \text{ r/m} = 20 \text{ r/s} \checkmark$
 $v = 20 \times 30 = 600 \text{ mm/s} \checkmark$
 $= 0,6 \text{ m/s}$
 $P_o = F_w \times v \checkmark$
 $20 = F_w \times 0,6 \checkmark$
 $F_w = 33,33 \text{ kN} \checkmark$ (6)
[15]

QUESTION 5

5.1 $TE = mgsin\theta$
 $= 1500 \times 9,81 sin 20^\circ \checkmark$
 $= 5032,8 \text{ N} \checkmark$
 $w = \frac{TE \times h}{d} \checkmark$
 $= \frac{5032,8 \times 0,8}{2,8} \checkmark$
 $= 1438 \text{ N}$
 $N_R = \frac{mg \times y}{d} \checkmark$
 $= \frac{1500 \times 9,81 \times 1,2}{2,8} \checkmark$
 $= 6306 \text{ N} \checkmark$

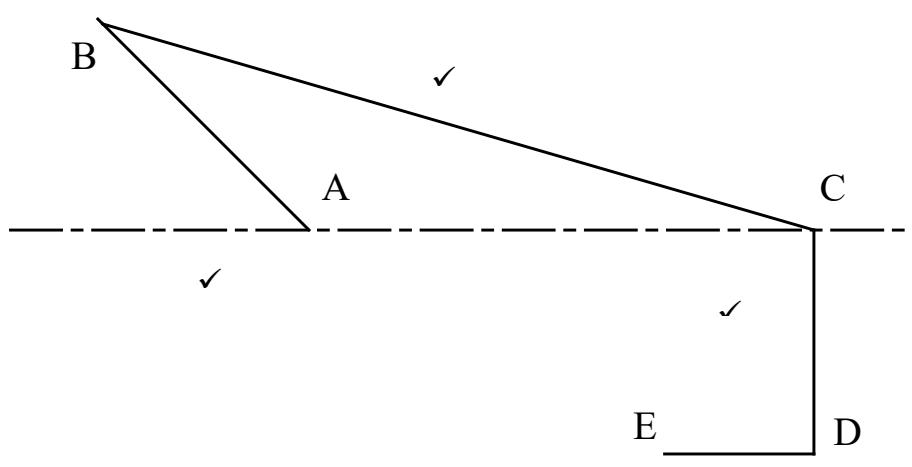
Load on rear wheels

$$\begin{aligned} &= 6306 + 1438 \checkmark \\ &= 7744 \text{ N} \checkmark \\ TE &= \mu N \checkmark \\ \mu &= \frac{5032,8}{7744} \checkmark \\ &= 0,65 \checkmark \end{aligned} \quad (12)$$

5.2 $P = TE \times v \times \frac{100}{\eta} \checkmark$
 $= 5032,8 \times \frac{25}{3,6} \times \frac{100}{52} \checkmark$
 $= 67,212 \text{ kW} \checkmark$ (3)
[15]

QUESTION 6

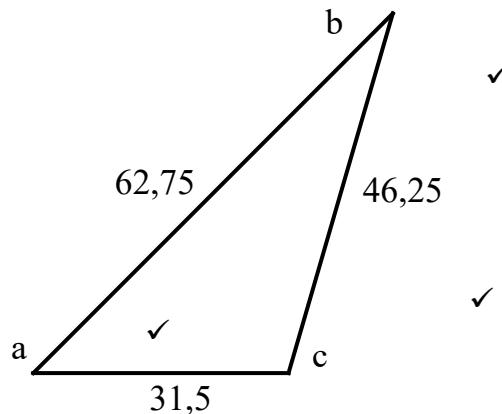
6.1



(3)

6.2 $v_B = 2\pi RN/60$
 $= 2\pi \times 0,1 \times 240/60$
 $= 2,51 \text{ m/s} \checkmark$ (1)

6.3



(3)

6.4 6.4.1 $v_{BtoC} = 46,25 \times 0,04 = 1,85 \text{ m/s} \checkmark$
 $\omega_{BC} = \frac{v_{BtoC}}{BC} = \frac{1,85}{0,3} \checkmark$
 $= 6,17 \text{ rad/s at } 73,83^\circ \checkmark$ (3)

6.1.2 $v_{CtoD} = 31,5 \times 0,04 = 1,26 \text{ m/s} \checkmark$
 $\omega_{CD} = \frac{v_{BtoC}}{BC} = \frac{1,26}{0,1} \checkmark$
 $= 12,6 \text{ rad/s at } 73,83^\circ \checkmark$ (3)

6.4.3 Centripetal acceleration B to C
 $= \omega_{BC}^2 \times BC$
 $= 6,17^2 \times 0,3 \checkmark$
 $= 11,42 \text{ m/s}^2 \checkmark$ (2)

6.4.4 Centripetal acceleration B to C
 $= \omega_{CD}^2 \times CD$
 $= 12,6^2 \times 0,1 \checkmark$
 $= 15,88 \text{ m/s}^2 \checkmark$ (2)

[17]

TOTAL: 100