higher education & training

Department:
Higher Education and Training
REPUBLIC OF SOUTH AFRICA

NASIENRIGLYN

NASIONALE SERTIFIKAAT

WISKUNDE N2

24 JULIE 2018

Hierdie nasienriglyn bestaan uit 8 bladsye.

Kopiereg voorbehou

VRAAG 1

1.1 1.1.1

$$\frac{3^2\ e^{-2}\ fg^{-5}}{81e^{-4}\ f^3\ g^3}$$
$$= \frac{e^{-2+4}}{3^{4-2}\ f^{3-1}\ g^{3+5}} \checkmark$$
$$= \frac{e^{+2}}{3^2\ f^2\ g^8} \checkmark$$

(2)

1.1.2

$$\frac{3\log_8 64 - \log_2 64\ - \log_7 2\ 401}{\log 1000 + \ 2\log_2 8}$$
$$= \frac{3\log_8 8^2 - \log_2 2^6\ - \log_7 7^4}{\log 10^3 + \ 2\log_2 2^3} \checkmark$$
$$= \frac{6-6-4}{3+6} \checkmark$$
$$= \frac{-4}{9} \checkmark$$

(3)

1.1.3

$$\log_3 189 - (\log_7 3)^{-1}$$
$$= \log_3 189 - \frac{1}{\log_7 3}$$
$$= \log_3 189 - \log_3 7 \checkmark$$
$$= \log_3\left(\frac{189}{7}\right) \checkmark$$
$$= \log_3 27$$
$$= 3\log_3 3$$
$$= 3 \checkmark$$

(3)

1.2 1.2.1

$$3x^{\frac{3}{2}} = 24$$
$$x^{\frac{3}{2}} = 8 \checkmark$$
$$\left(x^{\frac{3}{2}}\right)^{\frac{2}{3}} = \left(2^3\right)^{\frac{2}{3}} \checkmark$$
$$x = 2^2 \checkmark$$

(3)

1.2.1

$$\log_3 x + \log_3(x-2) = 1$$
$$\log_3 x(x-2) = 1 \checkmark$$
$$x^2 - 2x = 3^1 \checkmark$$
$$x^2 - 2x - 3 = 0$$
$$(x-3)(x+1) = 0 \checkmark$$
$$x = 3\ ;\ \ x \neq -1 \checkmark$$

(4)

1.3
$$f = \frac{1}{2\pi\sqrt{LC}}$$
$$f\sqrt{LC} = \frac{1}{2\pi} \checkmark$$
$$\sqrt{LC} = \frac{1}{2\pi f}$$
$$\left(\sqrt{LC}\right)^2 = \left(\frac{1}{2\pi f}\right)^2 \checkmark$$
$$LC = \frac{1}{4\pi^2 f^2}$$
$$C = \frac{1}{4\pi^2 f^2 L} \checkmark$$
(3)
[18]

VRAAG 2

2.1 2.1.1
$$a^2 + 7a - 18 = (a+9)(a-2) \checkmark$$
$$4m^2 - 9y^2 = (2m-3y)(2m+3y) \checkmark$$
$$2m^2 - 3ym = m(2m-3y) \checkmark$$
(3)

2.1.2
$$\text{KGV} = m(a+9)(a-2)(2m-3y)(2m+3y) \quad (\checkmark\ \checkmark\ \checkmark)$$
(3)

2.1.3 $\text{GGD} = 1 \checkmark$ (1)

2.2 2.2.1
$$\frac{x^2 - x - 12}{x^2 - 3x - 10} \div \frac{x^2 - 9x + 20}{x^2 - 2x - 8} \times \frac{x-5}{x+3}$$
$$= \frac{(x-4)(x+3)}{(x-5)(x+2)} \times \frac{(x-4)(x+2)}{(x-4)(x-5)} \times \frac{x-5}{x+3} \quad (\checkmark\ \checkmark\ \checkmark)$$
$$= \frac{x-4}{x-5} \checkmark\checkmark$$
(5)

2.2.2
$$\frac{2}{x^2+3x-4}+\frac{4}{x^2-4x+3}$$
$$=\frac{2}{(x+4)(x+1)}+\frac{4}{(x-3)(x-1)}$$
$$=\frac{2(x-3)+4(x+4)}{(x+4)(x+1)(x-3)}$$
$$=\frac{2x-6+4x+16}{(x+4)(x+1)(x-3)}$$
$$=\frac{6x+10}{(x+4)(x+1)(x-3)}$$ (4)

2.3 2.3.1
$$20x^2-x-1$$
$$=(5x+1)(4x-1)$$ (2)

2.3.2
$$\frac{3}{64}-27y^2$$
$$=3\left(\frac{1}{64}-9y^2\right)$$
$$=3\left(\frac{1}{8}-3y\right)\left(\frac{1}{8}+3y\right)$$ (3)

[21]

VRAAG 3

3.1 Peter het Rx gehad.

Morris het $R\frac{1}{4}x$

Ayanda het $R\frac{1}{2}x$

$\frac{1}{4}x=\frac{1}{2}x-35$

$x=2x-140$

$x=140$ (5)

3.2 3.2.1
$$\frac{2x-1}{3}=x-1$$
$$2x-1=3(x-1)$$
$$2x-1=3x-3$$
$$-1+3=3x-2x$$
$$x=2$$ (2)

3.2.2 $13x^2 - 8 = 7x$

$13x^2 - 7x - 8 = 0$

$x = \dfrac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$x = \dfrac{-(-7) \pm \sqrt{(-7)^2 - 4(13)(-8)}}{2(13)}$ ✓

$x = \dfrac{7 \pm \sqrt{465}}{26}$

✓ ✓

$x = 1{,}099$ of $x = -0{,}560$ (3)

3.3 3.3.1 $\omega = 2\pi n$

$n = \dfrac{\omega}{2\pi}$

$n = \dfrac{272}{2\pi}$ ✓

$n = 43{,}290$ r/s✓ (2)

3.3.2 $v = \pi Dn$

✓ (punt vir die omsetting van cm in m)

$v = \pi\left(\dfrac{2 \times 3}{100}\right)(43{,}290)$ ✓

$v = 8{,}160$ m/s✓ (3)

3.3.3 $\omega = 272$ rad/s

$5\,\text{min} = 5 \times 60$

$= 300\,\text{sec}$ ✓

$\theta = 272$ radiale binne 1 sekonde

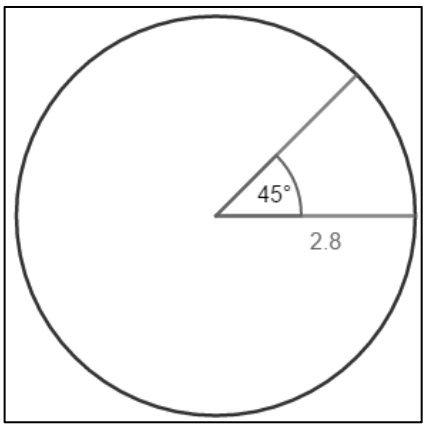
$\therefore \theta = 272 \times 300$ ✓

$\therefore \theta = 81600$ radiale binne 5 minute (300 sekondes)✓ (3)

3.4 $A = \dfrac{1}{2} r^2 \theta$ $\qquad \theta = 45° \times \dfrac{\pi}{180°}$

$A = \dfrac{1}{2}(2{,}8)^2(0{,}785)$ ✓ $\qquad \theta = 0{,}785$ rad✓

$A = 3{,}077$ ✓ cm^2



(3)

3.5 $64°45'54'' = 64,765°$ ✓

$\theta = 64,765° \times \frac{\pi}{180°}$

$\theta = 1,200$ radiale✓ (2)

[23]

VRAAG 4

4.1 $\text{Area} = \left[\frac{(\text{First ordinate} + \text{Last ordinate})}{2} + \text{Sum of all other ordinates}\right]$

$\times$The distance between ✓ the ordinates ✓

$\text{Area} = \left[\frac{(4+7)}{2} + 6 + 8 + 10 + 8\right] \times 3$

$\text{Area} = (37,5) \times 3$

$\text{Area} = 112,5$ ✓ eenhede^2 (3)

4.2 $\text{Volume} = \frac{4}{3}\pi r^3$ $\qquad r = \frac{280}{2}$

$\text{Volume} = \frac{4}{3}\pi (140)^3$ ✓ $\qquad r = 140$ mm ✓

$\text{Volume} = 11494040,32$ mm^3✓ (3)

4.3 $\cos\beta = 0,65$

$\beta = \cos^{-1}(0,65)$✓

$\beta = 49,458°$ ✓

$\beta = 360° - 49,458°$ ✓

$= 310,542°$ (3)

4.4 $V_{rect} = V_{sphere}$ ✓

$l.b.h = \frac{4}{3}\pi r^3$ ✓

$(5 \times 3 \times 4) = \frac{4}{3}\pi r^3$

$60 \times \frac{3}{4\pi} = r^3$ ✓

$r = \sqrt[3]{60 \times \frac{3}{4\pi}}$

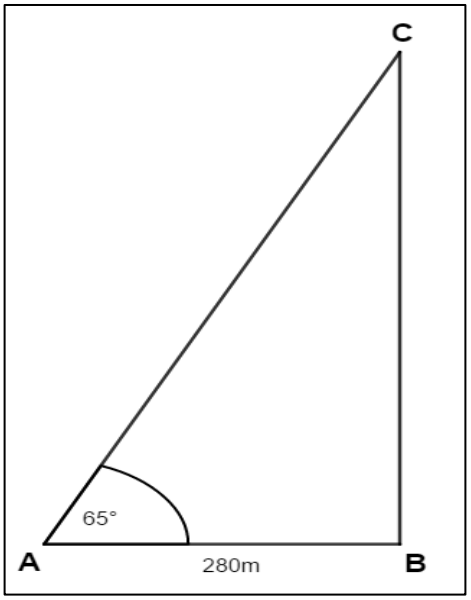
$r = 2,429$ ✓

$D = 2,429 \times 2$

$D = 4,858$ ✓ mm (5)

4.5 4.5.1

$$\tan 65° = \frac{BC}{AB}$$
$$BC = 280 \times \tan 65° \checkmark$$
$$BC = 600{,}462 \text{ m} \checkmark$$



(2)

4.5.2

$$\cos 65° = \frac{AB}{AC}$$
$$AC = \frac{280}{\cos 65°} \checkmark$$
$$AC = 662{,}536 \text{ m} \checkmark$$

OR

$$AC^2 = AB^2 + BC^2$$
$$AC = \sqrt{(280)^2 + (600{,}462)^2} \checkmark$$
$$AC = 662{,}536 \text{ m} \checkmark$$

(2)
[18]

VRAAG 5

5.1 5.1.1

$$x^2 + 6x - 7 = 0$$
$$(x+7)(x-1) = 0$$
$\checkmark$ $\checkmark$
$$x = -7 \text{ of } x = 1$$

(2)

5.1.2

$$x = \frac{-b}{2a}$$
$$x = \frac{-(6)}{2(1)}$$
$$x = -3 \checkmark$$

(1)

5.1.3

Vervang $x = -3$ in $x^2 + 6x - 7 = 0$
$$y = (-3)^2 + 6(-3) - 7 \checkmark$$
$$y = -16 \checkmark$$

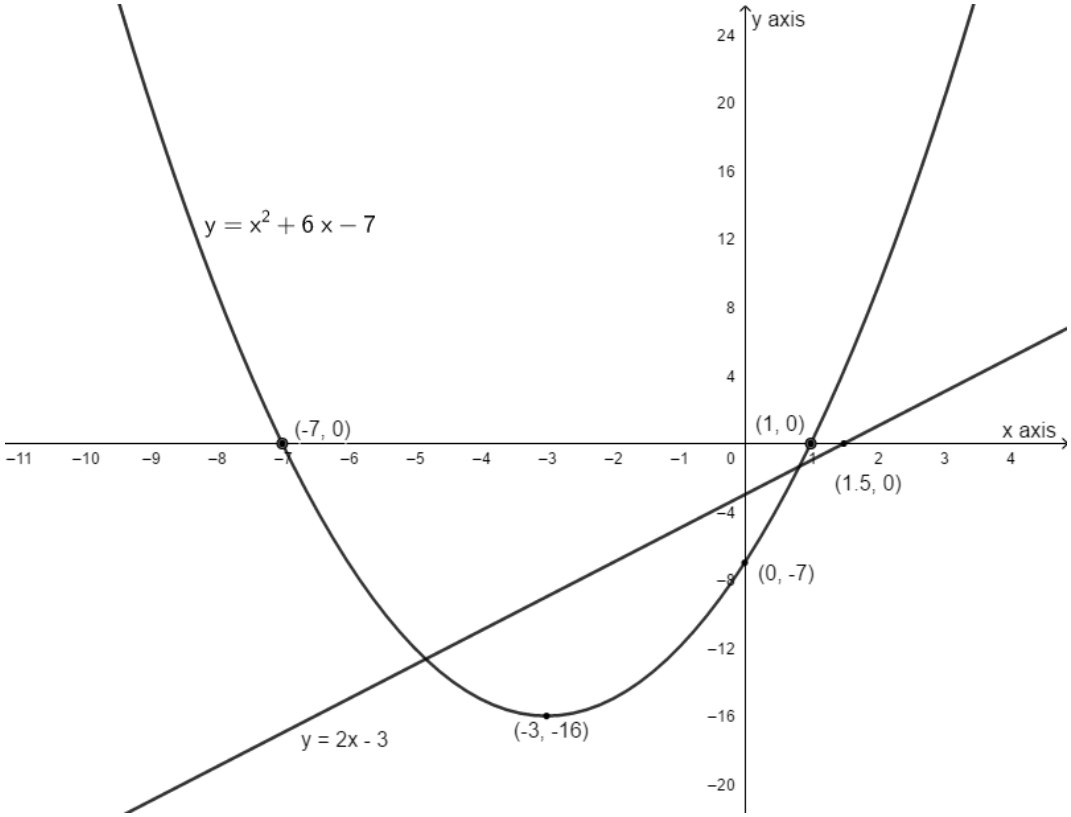
(2)

5.1.4

$$y = -7 \checkmark$$

(1)

5.2.1 2 punte vir die korrekte parabool getrek✓✓ (2)
en
5.2.2 2 punte vir die korrekte reguitlyn getrek✓✓ (2)



5.2.3 $(0{,}8\,;-1{,}3)$ en $(-4{,}8\,;-12{,}7)$ (2)

5.3.1 3 punte vir $f(x) = \sin x$ ✓✓✓ (3)
en
5.3.2 3 punte vir $g(x) = 2\cos x - 0{,}5$ ✓✓✓ (3)



5.3.3 $x = \pm 50°$ ✓ en $x = \pm 256°$ ✓ (2)
[20]

TOTAAL: 100

Kopiereg voorbehou