

# higher education \& training 

Department:
Higher Education and Training REPUBLIC OF SOUTH AFRICA

## NATIONAL CERTIFICATE (VOCATIONAL)

## MATHEMATICS

(Second Paper)
NQF LEVEL 4
(10501064)

7 November 2019 (X-paper)
09:00-12:00

This question paper consists of $\mathbf{1 0}$ pages, $\mathbf{2}$ addenda and a formula sheet of $\mathbf{2}$ pages.

## TIME: 3 HOURS

MARKS: 100

## INSTRUCTIONS AND INFORMATION

1. Answer all the questions.
2. Read all the questions carefully.
3. Number the answers according to the numbering system used in this question paper.
4. Start each question on a new page.
5. Use only a blue or black pen.
6. Clearly show all the calculations, diagrams, graphs, et cetera, which you have used in determining the answers.
7. If necessary, answers should be rounded off to three decimal places, unless stated otherwise.
8. Diagrams are not drawn to scale.
9. Write neatly and legibly.

## QUESTION 1

1.1 In the diagram below (not drawn to scale), line AEB is parallel to line JCD. Line $H C$ is perpencicular to BC and HC is produced to G . $\mathrm{A} \widehat{B C}=60^{\circ}$ and $\mathrm{A} \widehat{\mathrm{EF}}=160^{\circ}$


Calculate the size of each of the angles marked $x, y, z, s$ and $r$.
In the figure below diameter $D E$ of the circle is produced to $C . A$ and $B$ are points on the circle with line AB also produced to C . O is the cente of the circle. $B C=O A$ and $A \widehat{C} O=28^{\circ}$. Calculate $A \widehat{O} D$ and give reasons for the answer.

1.3 In the diagram below, two tangents RP and RS are drawn from a point R outside the circle with centre 0 . PO produced cuts the circle at B and meets the tangent RS produced at T . Let $\widehat{\mathrm{S}}_{1}=x$.

1.3.1 Prove that POSR is a cyclic quadrilateral.
1.3.2 Prove that SB || OR.
1.4 A circle centred at $P(3 ; 2)$ touches the $x-$ axis at point $C$. DE is a tangent to the circle, touching it at point A . The equation of the tangent DE is given by
$y=\frac{4}{3} x+\frac{4}{3}$.

1.4.1 Why is PC perpendicular to OC?
1.4.2 Determine the coordinates of C.
1.4.3 Determine the equation of the circle with cente P in the form

$$
\begin{equation*}
(x-a)^{2}+(y-b)^{2}=r^{2} \tag{3}
\end{equation*}
$$

1.4.4 Determine the coordinates of G , the $x$-intercept of DE .
1.4.5 $\quad$ Determine the equation of the diameter AB in the form $y=m x+c$

## QUESTION 2

2.1 Express $\sin 290^{\circ}$ as a function of an acute angle.
2.2 If $\tan x=\frac{3}{\sqrt{40}}$ and $0^{\circ}<\hat{x}<90^{\circ}$, determine the value of $\cos x$ without the use of a calculator. Leave your answer in surd form.
2.3 Solve for $x$ in the interval $\left[0^{\circ} ; 90^{\circ}\right]$ if
$\frac{\sin 2 x \cos x+\cos 2 x \sin x}{\cos 2 x \cos x-\sin 2 x \sin x}=1$
2.4 Simplify the following expression without using a calculator:
$\frac{2 \sin 50^{\circ}\left(\cos 60^{\circ} \cos 10^{\circ}+\sin 60^{\circ} \sin 10^{\circ}\right)}{\cos 10^{\circ}}$
2.5 2.5.1 Express $\cos (x+y)$ as ratios of the angles $x$ and $y$.
2.5.2 Hence derive a formula for $\cos 2 x$ in terms of $\sin x$.
2.6 Prove the following identity: $\frac{\cos x+\sin x}{\cos x-\sin x}-\frac{\cos x-\sin x}{\cos x+\sin x}=2 \tan 2 x$
2.7 A, B and C are 3 points on the same horizontal plane. Two cylinderical pipes are planted vertically at B and C . The angle of elevation from D to E is $27^{\circ}$. $\mathrm{AC}=2000$ metres, $\mathrm{BA} \mathrm{C}=43^{\circ}$ and $\mathrm{B} \widehat{\mathrm{C}} \mathrm{A}=36^{\circ}$.

2.7.1 Calculate $\mathrm{A} \widehat{\mathrm{B}} \mathrm{C}$.
2.7.2 Calculate DE.

## QUESTION 3

Answer QUESTIONS 3.1, 3.2 and 3.3 on ADDENDA A and B. Write your EXAMINATION NUMBER and CENTRE NUMBER on the ADDENDA, detach them from the question paper and hand them in with the ANSWER BOOK.

The data below shows the mathematics marks of 10 learners at a TVET college for the internal examinations and the final examination.

| Internal examinations $(x)$ | 80 | 68 | 94 | 72 | 74 | 83 | 56 | 68 | 65 | 75 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Final examination $(y)$ | 72 | 71 | 96 | 77 | 82 | 72 | 58 | 83 | 78 | 80 |

3.1 Make a scatter plot of the marks in the above table on ADDENDUM A (attached).
3.2 Calculate the equation of the least squares regression line for the data. No marks will be awarded if answers are taken directly from a calculator. Use one of the two tables on ADDENDUM B (attached) and then complete all the calculations.
3.3 Draw the least squares regression line on ADDENDUM A.
3.4 Calculate the predicted final examination mark for a learner who scores 70 in the internal examination.

## QUESTION 4

4.1 A TVET college has sporting facilities on campus which include tennis and cricket. A survey showed that $72 \%$ of the learners used the cricket nets and $48 \%$ used the tennis courts. Some learners used both while $8 \%$ used neither of the facilities. The number of learners at the college is 700 .
4.1.1 Determine the number of learners who use at least one of the facilities.
4.1.2 If a learner is selected randomly, what is the probability that this learner uses exactly one facility? [You may use a Venn diagram to determine your answer.]
4.1.3 Determine whether the events, 'using the cricket nets' and 'using the tennis courts' are independent or not.

$$
\begin{equation*}
(3 \times 3) \tag{9}
\end{equation*}
$$

4.2 The data below was obtained from the NSFAS financial aid office at a certain college.

|  | Receiving financial <br> aid | Not receiving financial <br> aid | Total |
| :--- | ---: | ---: | ---: |
| First time recipients | 4222 | 3898 | 8120 |
| Repeating recipients | 1879 | 731 | 2610 |
| Total | 6101 | 4629 | 10730 |

Determine the probability that a student selected at random is:
4.2.1 A student receiving financial aid
4.2.2 A repeating learner and is not receiving financial aid
4.2.3 A first-time learner and is receiving financial aid

## QUESTION 5

5.1 Dhimbi invests R3 million into an account earning interest at $6 \%$ per annum, compounded annually.

How much will her investment be worth at the end of 6 years?
5.2 Weeds and Lawn is a garden services company that needs to buy a mowing tractor. The cost of the tractor is R210 000,00. The company signs a hire purchase loan agreement involving equal monthly payments over 3 years at an interest rate of $14 \%$ per annum. The company pays a $10 \%$ deposit. Weed and Lawn also takes out insurance on the tractor at a cost of R22 per month.

5.2.1 What monthly payments will Weed and Lawn have to make?
5.2.2 What will be the total cost to Weed and Lawn at the end of 3 years?
5.3 Given below is the individual rates table obtained from the South African Revenue Services (SARS). Use this information, as well as the income particulars of a certain Mr Dedricks, to answer the questions which follow.

| RATES OF TAX FOR INDIVIDUALS <br> 2019 tax year (1 March 2018 - 28 February 2019) |  |
| :--- | :--- |
| Taxable income (R) | Rates of tax (R) |
| $0-195850$ | $18 \%$ of taxable income |
| $195851-305850$ | $35253+26 \%$ of taxable income above 195850 |
| $305851-423300$ | $63853+31 \%$ of taxable income above 305850 |
| $423301-555600$ | $100263+36 \%$ of taxable income above 423300 |
| $555601-708310$ | $147891+39 \%$ of taxable income above 555600 |
| $708311-1500000$ | $207448+41 \%$ of taxable income above 708310 |
| 1500001 and above | $532041+45 \%$ of taxable income above 1500000 |


| Tax rebates 2019 tax year (1 March 2018-28 February 2019) |  |
| :--- | ---: |
| Tax rebate tax year 2019 |  |
| Primary | R14 067 |
| Secondary (65 and older) | R7 713 |
| Tertiary (75 and older) | R2 574 |


| Tax thresholds 2019 tax year (1 March 2018-28 February 2019) |  |
| :--- | ---: |
| Age | Tax Year 2019 |
| Under 65 | R78 150 |
| 65 and older | R121 000 |
| 75 and older | R135300 |


| Medical tax credit rates from 2013 tax year onwards |  |
| :--- | :---: |
| Per month (R) | $\mathbf{2 0 1 9}$ |
| For the taxpayer who paid the medical scheme contributions | R310 |
| For the first dependent | R310 |
| For each additional dependent | R209 |

[http://www.sars.gov.za/Tax-Rates/Income-Tax/Pages/Rates\ of\ Tax\ for\ Individuals.aspx]

A 45-year-old male, Mr Dedricks, is married and has 2 teenage children. His income and deductions are presented in the table below.

| INCOME |  | DEDUCTIONS |  |
| :--- | :--- | :--- | :---: |
| Income | Amount | Deductions | Amount <br> (monthly) |
| Gross salary | R25 000 per month | Tax deducted by employer | R2 500,00 |
| Income from <br> investments | R1 000 per month | Pension | R2 500,00 |
| Annual bonus | R30 000 | Medical aid | R4 000,00 |
|  |  | UIF | R250,00 |

Use the tax tables and the information above to answer the questions:
5.3.1 Calculate Mr Dedricks' annual taxable income.
5.3.2 Write down the tax bracket (from the tax table) in which Mr Dedricks
falls.
5.3.3 Calculate the amount of tax Mr Dedricks must pay or receive from SARS after assessment.

## ADDENDUM A

## CENTRE NUMBER

## EXAMINATION NUMBER

## QUESTIONS 3.1 AND 3.3



## ADDENDUM B

CENTRE NUMBER
EXAMINATION NUMBER

## QUESTION 3.2 (Option 1)

| Internal examinations <br> $(\boldsymbol{x})$ | Final examination <br> $(\boldsymbol{y})$ | $\boldsymbol{x y}$ | $\boldsymbol{x}^{2}$ |
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|  |  |  |  |
|  |  | $\bar{y}=$ |  |

## QUESTION 3.2 (Option 2)

| Internal examinations <br> $(x)$ | Final examination <br> $(y)$ | $(\boldsymbol{x}-\overline{\boldsymbol{x}})(\boldsymbol{y}-\overline{\mathbf{y}})$ | $(\boldsymbol{x}-\overline{\boldsymbol{x}})^{2}$ |
| :---: | :---: | :---: | :---: |
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|  |  |  |  |
|  |  |  |  |
|  |  |  | $\sum(x-\bar{x})^{2}=$ |
| $\sum x=$ |  |  |  |
|  |  |  |  |
| $\bar{x}=$ |  |  |  |
|  | $\bar{y}=$ |  |  |
|  |  |  |  |
|  |  |  |  |

## FORMULA SHEET

NOTE: Some of the formulae in this formula sheet may not be generally true, but may hold under certain conditions. The candidate is required to select the appropriate formulae for a given situation.

1. $y=m x+c$
2. $m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}$
3. $y-y_{1}=m\left(x-x_{1}\right)$
4. $(x-a)^{2}+(y-b)^{2}=r^{2}$
5. $M\left(\frac{x_{1}+x_{2}}{2} ; \frac{y_{1}+y_{2}}{2}\right)$
6. $m=\tan \theta$
7. Distance $=\sqrt{\left(x_{2}-x_{1}\right)^{2}+\left(y_{2}-y_{1}\right)^{2}}$
8. $\frac{\sin \theta}{\cos \theta}=\tan \theta$
9. $\sin ^{2} \theta+\cos ^{2} \theta=1$
10. $\sin (\alpha \pm \beta)=\sin \alpha \cos \beta \pm \sin \beta \cos \alpha$
11. $\cos (\alpha \pm \beta)=\cos \alpha \cos \beta \mp \sin \alpha \sin \beta$
12. $\sin 2 \theta=2 \sin \theta \cos \theta$
13. $\cos 2 \theta=\cos ^{2} \theta-\sin ^{2} \theta$
14. $\cos 2 \theta=1-2 \sin ^{2} \theta$
15. $\cos 2 \theta=2 \cos ^{2} \theta-1$
16. $\frac{\sin \hat{A}}{a}=\frac{\sin \hat{B}}{b}=\frac{\sin \hat{C}}{c}$
17. $a^{2}=b^{2}+c^{2}-2 b c \cos \hat{A}$
18. $\bar{x}=\frac{\sum_{i=1}^{n} x_{i}}{n}$
19. $\quad$ Variance $=s^{2}=\frac{\sum\left(x_{i}-\bar{x}\right)^{2}}{n}$
20. Standard deviation $=\sqrt{\frac{\sum\left(x_{i}-\bar{x}\right)^{2}}{n}}$
21. $\hat{y}=a+b x$
22. $b=\frac{\sum(x-\bar{x})(y-\bar{y})}{\sum(x-\bar{x})^{2}} \quad$ or $\quad b=\frac{n \sum x y-\sum x \sum y}{n \sum x^{2}-\left(\sum x\right)^{2}}$
23. $a=\bar{y}-b \bar{x}$
24. $I=A_{0} \times \frac{r}{100} \times t$
or $\quad I=\frac{\operatorname{Pr} t}{100}$
or $\quad A=P(1+i n)$
25. $A_{t}=A_{0}\left(1+\frac{r}{100 \times m}\right)^{t \times m}$
or $\quad A_{t}=P\left(1+\frac{r}{100}\right)^{n}$
or $\quad A=P(1+i)^{n}$
26. $A_{t}=A_{o}\left(1-\frac{r}{100}\right)^{t}$
or $\quad A=P(1-$ in $)$
or $\quad A=P(1-i)^{n}$
27. $i=\frac{r}{100}$
28. $\mathrm{P}(\mathrm{A})=\frac{n(\mathrm{~A})}{n(\mathrm{~S})}$
29. $P(A$ and $B)=P(A) \times P(B)$
30. $P(A$ or $B)=P(A)+P(B)$
31. $P(A$ or $B)=P(A)+P(B)-P(A$ and $B)$
32. $\mathrm{P}(\mathrm{A} / \mathrm{B})=\frac{\mathrm{P}(\mathrm{A} \text { and } \mathrm{B})}{\mathrm{P}(\mathrm{B})}$
