



N6

Building and Structural Construction

Lecturer Guide

EAY Ebrahim

Additional resource material for this title includes:

- Electronic Lecturer Guide
- Exemplar examination paper memos
- PowerPoint presentation
- Past exam papers

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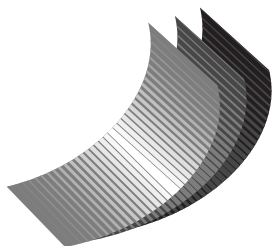
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Dedication

This book is dedicated to my four grandchildren as well as all the students who have attended my classes.

Acknowledgements

A very special thanks to Danny Mitchell – for your friendship, guidance and assistance during my early years of teaching. Without you, I would never have been able to teach this subject.

A very special thanks to Alfred Ramahlape – for your assistance in some of the difficult parts, for the encouragement and calculations. You remain a sincere and good friend.

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Introduction

This syllabus is specifically designed for the TVET college system. It is a continuation of the N5 system and concludes the building sciences regarding the design of reinforced concrete structural elements.

This syllabus is also the culmination of all the work between N1 to N3 Building Science, N4 and N5 Building and Structural Construction and some elements from N3 Building Drawing where reinforced steel was introduced.

Students will be pleased to know that the final examination and class tests will all be open-book exams. They will be allowed into the exam room with their subject files and notes, as well as all the required Codes of Practices for referencing. A BOE8/2 Hot-rolled structural steel section red book will be issued to them. However, NO past question papers and marking guidelines (memos) will be allowed in the exam room.

Students should not be fooled by an open-book exam – it could become very confusing to write the exam while searching through their notes.

Here are some solutions:

- Encourage your learners to prepare from day one, ie. the beginning of the semester.
- I suggest using a well-organised lever arch file.
- They should neatly rewrite all exercises on single-sided exam pad pages – one exercise at a time, and then number the pages and clip them together. They should keep all the same types of exercises together, eg. all concrete beams, then the slabs, then the columns, etc.
- With the final examination being an open-book exam and class test, they should create a column on the right-hand side of their exam pad page to write their OWN personal notes, eg. how to use the calculator when doing tricky calculations or anything of significance. This will be less time-consuming as they only have FOUR hours to sit for the exam.
- Students should copy ALL the relevant tables and keep it at the front of their files.

Always remember that as an educator, you are the students' main source of information and they will draw on your knowledge and experience. The Student Book remains a learning resource for them and does not replace a lecturer.

You are encouraged to work through the calculations yourself and ensure that you understand the answers so that you can explain these processes to your classes.

We wish you well and trust that you will enjoy teaching this course and guiding your students to success.

EAY Ebrahim

Lecturer Guidance

1. General aims

To provide students with knowledge and skills that is used for structural design in the construction industry.

2. Specific aims

- 2.1 Students should obtain thorough background knowledge of the theory and methodology as applied in Building and Structural Construction.
- 2.2 The teaching of this subject is aimed at introducing the student to the application of technological principles and practices in the building and structural construction industry.

3. Prerequisites

The student must have a N5 certificate in Civil Engineering.

4. Duration

Full-time: 7.5 hours per week. This instructional offering may also be offered part-time.

5. Evaluation

- 5.1 Evaluation is conducted continuously by means of two formal tests at college level. Learner must obtain a minimum ICASS mark of at least 40% in order to qualify to write the final examination and a mark will be calculated together in a ratio of 40:60 to derive the promotion mark. The learner must obtain at least 40% on the final examination.

The promotion mark will be calculated as follows:

Promotion mark = **40%** of (ICASS mark) + **60%** of (exam mark)

- 5.2 Examination

The open-book examination in N6 Building and Structural Construction (Engineering Studies – Report 191) will be conducted as follows:

Modules 1 to 3:

Marks: 100

Duration: 4 hours

Items permitted in the open-book examination are as follows:

- Students' subject files/notes may be brought into the exam room
(No past question papers and marking guidelines are allowed)
- A normal A4 answer book **MUST** be provided to students.
- Non-programmable scientific calculators may be used.
- The following addenda:
 - Schedule A: Cross-sectional area of reinforced rods for beams and columns
 - Schedule B: Cross-sectional area of reinforced rods per metre width for slabs and staircases
 - Schedule C: Isometric black hexagonal bolts and nuts
- Students are allowed to bring the following Codes of Practices for referencing into the exam room.
 - SABS 0100-1:1992
 - SABS 0100-2:1992
 - SABS 0162-1:1993
 - SABS 0144:1995
 - SABS 0162-3 1984
 - SABS 0144-1978
 - SANS 10100-1:2000
- For steel design work, the recognised tables may be used by making reference to the BOE8/2 Hot-rolled Structural Steel Sections as issued by National Examinations.

5.3 Weighting

The following weights are consequently awarded to each category:

Knowledge and understanding	Application	Analysis/synthesis and evaluation
5–10%	10–20%	10–80%

6. Learning content

THEORETICAL BACKGROUND

It is essential that this subject introduces students to basic principles applicable to different sections of building and structural construction before working through a typical design.

TECHNICAL BACKGROUND

It is essential that this subject should be illustrated and evaluated within the context of concrete and steel structural design work.



Note

Lecturers MUST make references to the following:

- Standard Building Regulation (Act 103 of 1977) as printed from Government Gazette and all amendments made to date;
- Codes of Practices when teaching:
 - SABS 0100-1:1992
 - SABS 0100-2:1992
 - SABS 0162-1:1993
 - SABS 0144:1995
 - SABS 0162-3 1984
 - SABS 0144-1978
 - SANS 10100-1:2000;
- The following schedules:
 - Schedule A: Cross-Sectional area of reinforced rods for beams and columns
 - Schedule B: Cross-Sectional area of reinforced rods per metre width for slabs and staircases
 - Schedule C: Isometric black hexagonal bolts and nuts for steel roof truss calculations;
- BOE8/2 Hot-rolled Structural Steel Sections (red book) for steel design work.

7. Mark allocation and weighted value of modules

MODULES	WEIGHTING (%)
1. Concrete	50
2. The bending schedule	5
3. Iron and steel	45
Total	100

8. Work schedule

Week	Topic	Content	Exercises	Hours
1–5	Module 1 Concrete	1.1 Concrete materials 1.2 Reinforced concrete beam design 1.3 Rectangular reinforced concrete beam design 1.4 One-way or unidirectional reinforced concrete slabs 1.5 Flanged T-beams of reinforced concrete 1.6 Flanged L-beams of reinforced concrete 1.7 Reinforced concrete column design 1.8 Reinforced concrete staircases	Exercise 1.1 Exercise 1.2 Exercise 1.3 Exercise 1.4 Exercise 1.5 Exercise 1.6 Exercise 1.7 Exercise 1.8	50 hours
6	Module 2 The bending schedule	2.1 Structural detailing	Exercise 2.1	5 hours
6–10	Module 3 Iron and steel	3.1 Materials 3.2 Binding joints 3.3 Roof frame connection joints 3.4 Welding connections 3.5 Steel beams 3.6 Steel columns 3.7 Eccentric-loaded beam connections	Exercise 3.1 Exercise 3.2 Exercise 3.3 Exercise 3.4 Exercise 3.5 Exercise 3.6 Exercise 3.7 Exercise 3.8 Exercise 3.9	45 hours
TOTAL				±100 hours

9. Lesson plan template

Subject and level	N6 Building and Structural Construction
Prescribed textbook (Title and author)	<i>N6 Building and Structural Construction</i> by EAY Ebrahim

WEEK 1				
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/aids (Please tick)	Student activity (exercise in textbook/additional supporting tasks) to be done this week
		Lecture	White board/OHP	
		Group work	Models	
		Demonstration	Handouts	
		Simulation	Multimedia	
		Introduction to lessons		
		Recapping/reinforcement		

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WEEK 2				
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/aids (Please tick)	Student activity (exercise in textbook/additional supporting tasks) to be done this week
		Lecture	White board/OHP	
		Group work	Models	
		Demonstration	Handouts	
		Simulation	Multimedia	
		Introduction to lessons		
		Recapping/reinforcement		

Subject and level	N6 Building and Structural Construction
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WEEK 3			
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/ aids (Please tick)
		Lecture	White board/OHP
		Group work	Models
		Demonstration	Handouts
		Simulation	Multimedia
		Introduction to lessons	
		Recapping/reinforcement	

Subject and level	N6 Building and Structural Construction
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WEEK 4				
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/aids (Please tick)	Student activity (exercise in textbook/additional supporting tasks) to be done this week
		Lecture	White board/OHP	
		Group work	Models	
		Demonstration	Handouts	
		Simulation	Multimedia	
		Introduction to lessons		
		Recapping/reinforcement		

Subject and level	N6 Building and Structural Construction
Prescribed textbook (Title and author)	<i>N6 Building and Structural Construction</i> by EAY Ebrahim

WEEK 5			
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/aids (Please tick)
		Lecture	White board/OHP
		Group work	Models
		Demonstration	Handouts
		Simulation	Multimedia
		Introduction to lessons	
		Recapping/reinforcement	

Student activity (exercise in textbook/additional supporting tasks) to be done this week

Subject and level	N6 Building and Structural Construction
Prescribed textbook (Title and author)	<i>N6 Building and Structural Construction</i> by EAY Ebrahim

WEEK 6				
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/aids (Please tick)	Student activity (exercise in textbook/additional supporting tasks) to be done this week
		Lecture	White board/OHP	
		Group work	Models	
		Demonstration	Handouts	
		Simulation	Multimedia	
		Introduction to lessons		
		Recapping/reinforcement		

Subject and level	N6 Building and Structural Construction	
Prescribed textbook (Title and author)	<i>N6 Building and Structural Construction</i> by EAY Ebrahim	

WEEK 7			Student activity (exercise in textbook/additional supporting tasks) to be done this week
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/aids (Please tick)
		Lecture	White board/OHP
		Group work	Models
		Demonstration	Handouts
		Simulation	Multimedia
		Introduction to lessons	
		Recapping/reinforcement	

Subject and level	N6 Building and Structural Construction
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WEEK 8				
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/aids (Please tick)	Student activity (exercise in textbook/additional supporting tasks) to be done this week
		Lecture	White board/OHP	
		Group work	Models	
		Demonstration	Handouts	
		Simulation	Multimedia	
		Introduction to lessons		
		Recapping/reinforcement		

Subject and level	N6 Building and Structural Construction
Prescribed textbook (Title and author)	<i>N6 Building and Structural Construction</i> by EAY Ebrahim

WEEK 9			
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/aids (Please tick)
		Lecture	White board/OHP
		Group work	Models
		Demonstration	Handouts
		Simulation	Multimedia
		Introduction to lessons	
		Recapping/reinforcement	
		Student activity (exercise in textbook/additional supporting tasks) to be done this week	

Subject and level	N6 Building and Structural Construction				
Prescribed textbook (Title and author)	<i>N6 Building and Structural Construction</i> by EAY Ebrahim				
WEEK 10					
Content/outcomes to be covered this week	List of examples to be done in class by the lecturer to explain the outcome/concept	Facilitation method (Please tick)	Teaching resources/aids (Please tick)	Student activity (exercise in textbook/additional supporting tasks) to be done this week	
		Lecture	White board/OHP		
		Group work	Models		
		Demonstration	Handouts		
		Simulation	Multimedia		
		Introduction to lessons			
		Recapping/reinforcement			

1 Concrete



By the end of this module, students should be able to:

Concrete materials

- define *concrete* by listing and explaining the materials that are used to mix concrete;
- determine by means of calculation the relation between the quantity of mixing water and the amount of cement in a concrete mix known as the water-cement ratio;
- explain the importance of curing using the following curing methods:
 - wet/damp sand
 - sawdust
 - hessian
 - polythene sheeting
 - curing compound
 - pounding
 - water sprinkling; and
 - curing by leaving the formwork in place or unremoved.
- explain and distinguish between the following tests that are done in concrete:
 - slump test
 - cube test
 - bending test
 - water permeability test
 - concrete abrasion test;

Reinforced concrete beam design

- determine the following, by means of calculation, on a simply supported reinforced concrete beam with effective depth and suitable reinforcement (live- and point loads):
 - the effective span if not given
 - the maximum bending moment due to imposed load
 - the effective depth
 - the overall depth
 - the dead load
 - the maximum bending moment due to dead load
 - the total bending moment

- the value of 'k'
- the distance of lever arm (Z)
- the tension reinforcement
- check the minimum reinforcement
- check the maximum area of reinforcement
- check the shear stress (v)
- the maximum design shear stress
- the shear reinforcement
- the anchorage for links;
- determine the following, by means of calculation, on a simply supported reinforced concrete beam with a maximum distributed load (tension and compression reinforcement):
 - the area of steel in tension
 - check the minimum reinforcing
 - the distance of the lever arm (Z)
 - the maximum moment of resistance in tension
 - the area of steel in compression
 - check the minimum reinforcing
 - the maximum moment of resistance in compression
 - the total load
 - the dead load
 - the maximum imposed load;
- determine the following, by means of calculation, on a simply supported reinforced concrete beam with maximum distributed load (tension reinforcement)
 - the area of steel in tension
 - check the minimum reinforcement
 - check the maximum reinforcement
 - the distance of the lever arm (Z)
 - the maximum moment of resistance
 - the total load
 - the dead load
 - the maximum imposed load;
- determine the following, by means of calculation, on a simply supported reinforced concrete beam (given uniformly distributed live load and a point load):
 - the design loads for the given beam
 - the reactions R_L and R_R
 - the shear force and bending moment diagram
 - the value of 'K';

Rectangular reinforced concrete beam design

- determine the following, by means of calculation, on a simply supported rectangular reinforced concrete beam:
 - the effective depth of the reinforced concrete beam
 - the suitable tension reinforcement for the reinforced concrete beam
 - the minimum and maximum required main reinforcement;

One-way or unidirectional reinforced concrete slabs

- determine the following, by means of calculation, on a simply supported reinforced concrete slab with maximum distributed load per-square meter:
 - the area of steel
 - the distance of lever arm (Z)
 - the maximum moment of resistance
 - the total load
 - the dead load
 - the imposed load
 - the maximum area of reinforcement
 - the check the shear stress (v)
 - the maximum design shear stress
 - the shear reinforcement
 - the anchorage for links
- determine the suitable tension and secondary reinforcement for a one-directional simple supported reinforced concrete slab using the following specifications:
 - the span
 - the live load
 - the concrete grade
 - the density of concrete
 - the main reinforcement
 - the secondary reinforcement
 - the self weight of the slab included/ not included;
- determine the following specifications, by means of calculation, on a simply supported reinforced concrete slab:
 - the effective span
 - the length of the slab
 - the overall depth
 - the density of concrete
 - the supported by I-profile parallel flange beams;
- calculate :
 - the total design dead load of the slab

- the suitable I-parallel flange steel beam to support the slab;

Flanged reinforced concrete T-beams

- determine, by means of calculation, $x < hf$ of the neutral axis lies within the flange, using the following specification:
 - the lever arm (Z)
 - the neutral axis (x)
 - the total design load
 - the maximum bending moment
 - the tension reinforcement
 - the minimum distance between bars
 - the minimum reinforcing
 - the maximum area of reinforcements
 - the check the shear stress (v)
 - the maximum design shear stress
 - the maximum spacing ($0,75d$)
 - the anchorage for links
- determine, by means of calculation, the required tension reinforcement if the neutral axis is within the flange of the flanged beam;

Flanged reinforced concrete L-beams

- determine by means of calculation the required tension reinforcement if the neutral axis is within the flange;
- use Clause 4.3.1.5 to calculate width 'X' of the L-beam;
- determine, by means of calculation, the suitable tension reinforcement for a simply supported L-beam given the following specifications:
 - the effective span if not given
 - the imposed load
 - the dead load
 - the maximum bending moment
 - the value of 'K'
 - the distance of the lever arm (Z)
 - the tension reinforcement
 - the minimum distance between bars
 - check the minimum reinforcing;

Reinforced concrete columns

- determine by means of calculation a square, rectangular and round axially loaded column the following:
 - the required number and diameter of the longitudinal bars
 - the maximum and minimum percentage of the steel reinforcement
 - the diameter and pitch of the helical binder

- the net area of the concrete
- the axial load the column can withstand
- the required diameter and spacing of the binders;
- determine by means of calculation the size and suitable reinforcement of pad foundation using the following:
 - the imposed load
 - the dead load
 - the self-weight
 - the given bearing pressure on the ground; and

Reinforced concrete stairs

- calculate the following using the relevant code references where necessary:
 - the total design, dead and imposed loads
 - the maximum bending moment
 - the value of the constant ‘K’
 - the size and spacing of suitable main and secondary reinforcements.

Concrete is one of the most used materials in most types of buildings structures. Concrete is a composite material composed of fine and coarse aggregate bonded together with a fluid cement that hardens over time. Concrete is the second most-used substance in the world after water, and is the most widely used for building material.

Concrete is produced by mixing aggregate and cement. The addition of enough water allows the mixture to set and gain strength. Concrete gains strength over time, as long it is given the time to cure.

Exercise 1.1

SB page 36

The following exercise focuses on single beams.

1.	<p><u>All references taken from SANS 10100-1 (2000)</u></p> <p>F_{cu} = 20 MPa</p> <p>F_y = 250 MPa</p> <p>Span = 7,00 m</p> <p>Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1)</p> <p>Table 3 (4.1.5.2)</p> <p>Table 3 (4.1.5.2)</p> <p>2 400 kg/m³</p>
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1.1	<u>Determine the effective depth of the slab</u> Effective depth = span / 16 Effective depth = 7 000 / 16 Effective depth = 437,5 mm	Table 10 (Cl 4.3.6.2.1)	
	<u>Determine the overall depth</u> Assume R20 main steel, R8 binders and 25 mm cover. Overall depth = 437,5 + 10 + 8 + 25 Overall depth = 480,5 mm (Use overall depth = 500 mm)		
	<u>Determine the design dead loads of the beam</u> Design dead load = Volume \times density $\times 9,81 \times 10^{-3} \times 1,2$ Gn DDL = $0,50 \times 0,32 \times 1 \times 2 400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2$ Gn Design dead load = 4,52 kNm Design imposed UDL = 7 kNm $\times 1,6$ Qn = 11,2 kNm Design imposed point load = 12 kN $\times 1,6$ Qn = 19,2 kN	Cl 4.2.2.1 Cl 4.2.2.1	
	<u>Calculate the maximum bending moment</u> $BM_{\max} = \frac{WL^2}{8} + \frac{WL^2}{8} + \frac{WL}{4}$ $BM_{\max} = \frac{4,52 \times 7^2}{8} + \frac{11,2 \times 7^2}{8} + \frac{19,2 \times 7}{4}$ $= 27,69 + 68,6 + 33,6$ $BM_{\max} = 129,89 \text{ kNm}$		
	<u>Calculate the value for 'K'</u> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{129,89 \times 10^6}{20 \times 320 \times 437,5^2}$ $K = 0,106 < K^1 = 0,156$ Provide tension reinforcement only.	(Cl 4.3.3.4.1)	
	<u>Calculate the distance of the lever arm (Z)</u> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k}{0,9}} \right\} \leq 0,95d$ $Z = 437,5 \left\{ 0,5 + \sqrt{0,25 - \frac{0,106}{0,9}} \right\} \leq 0,95 \times 437,5$ $Z = 437,5 \{0,864\} \leq 415,63$ $Z = 377,84 \text{ mm} < 415,63 \text{ mm}$	(Cl 4.3.3.4.1)	(2)

1.2

<p><u>Calculate the tension reinforcement</u></p> $A_s = \frac{M}{0,87 \times f_y \times z}$ $A_s = \frac{129,89 \times 10^6}{0,87 \times 250 \times 377,84}$ $A_s = 1\,518,72 \text{ mm}^2$ <p>Use 4R25 ($A_s = 1\,964 \text{ mm}^2$)</p>	<p>(Cl 4.3.3.4.1)</p>	<p>(3)</p>
<p><u>Check for the minimum main reinforcement</u></p> $\frac{100 A_s}{A_c} = \frac{100 \times 1\,964}{500 \times 320}$ $= 0,92$ <p>1,23 > 0,8</p> <p>The reinforcement is sufficient.</p>	<p>Table 23 (Cl 4.11.4)</p>	
<p><u>Check for the maximum area of reinforcement</u></p> <p>4% of AC</p> $4\% \times 500 \times 320$ $6\,400 \text{ mm}^2$ $964 < 6\,400$ <p>The reinforcement is sufficient.</p>	<p>(Cl 4.11.5.1)</p>	

2.

<p>All references taken from SANS 10100-1 (2000).</p>		
<p>$f_{cu} = 25 \text{ MPa}$ $f_y = 250 \text{ MPa}$ Span = 6,7 m Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) Clause 4.3.1.2 $2\,415 \text{ kg/m}^3$</p>	
<p><u>Determine steel in tension</u></p> $A_s = 2 \times \frac{\pi d^2}{4}$ $A_s = 2 \times \frac{\pi 20^2}{4}$ $A_s = 628 \text{ mm}^2$		
<p><u>Check the minimum area reinforcement</u></p> $\frac{100 A_s}{A_c}$ $\frac{100 \times 628}{220 \times 450} = 0,63 > 0,45 \text{ OK}$ <p><u>Check the maximum area of reinforcement</u></p> <p>4% of AC</p> $4\% \times (220 \times 450) = 3\,960 \text{ mm}^2 \quad \text{okay}$	<p>Table 23</p> <p>(Cl 4 11.5.4)</p>	

<p><u>Calculate the distance of lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K^1}{0,9}} \right\}$ $Z = 400 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 400 (0,777)$ $Z = 310,8 \text{ mm}$	<p>(Cl 4.3.3.4)</p> <p>Use effective depth 'd' = 400 mm.</p> <p>Where cover = 50 mm</p>	
<p><u>Determine the maximum moment of resistance in tension</u></p> <p>Where $A_s = \frac{M}{0,87 f_y z}$</p> <p>Then: $M = A_s \times 0,87 \times f_y \times z$</p> $M = 628 \text{ mm}^2 \times 0,87 \times 250 \text{ N/mm}^2 \times 310,8 \text{ mm}$ $M = 42,45 \text{ kNm}$	<p>(Cl 4.3.3.4)</p>	
<p><u>Determine the total load</u></p> <p>Where: Maximum bending moment = $\frac{WL}{4}$</p> $42,45 = \frac{w \times 6,70}{4}$ $W = 42,45 \times 4 / 6,70$ $W = 25,34 \text{ kN}$		
<p><u>Determine the dead load</u></p> <p>Dead load = Volume \times density \times g $\times 10^{-3}$</p> $\text{Dead load} = 0,45 \times 0,22 \times 1 \times 2415 \text{ kg/m}^3 \times 9,81 \times 10^{-3}$ $\text{Dead load} = 2,35 \text{ kN}$		
<p><u>Determine the maximum point load</u></p> $\text{Total load} = 1,2(G_n) + 1,6(Q_n)$ $25,53 \text{ kN} = 1,2(2,35) + 1,6(Q_n)$ $25,34 \text{ kN} - 2,35 = 1,6(Q_n)$ $Q_n = 22,99 / 1,6$ $\text{Maximum point load} = 14,37 \text{ kN}$	<p>(Cl 4.2.2.1)</p>	

3.	<p><u>All references taken from SANS 10100-1 (2000)</u> $f_{cu} = 25 \text{ MPa}$ $f_y = 250 \text{ MPa}$ Span = 5,5 m Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) Clause 4.3.1.2 2 400 kg/m³</p>	
3.1	<p><u>Determine the effective depth of the slab</u> Effective depth = span / 16 Effective depth = 5 500 / 16 Effective depth = 343,75 mm</p>	<p>Table 10 (Cl 4.3.6.2.1)</p>	
	<p><u>Determine the overall depth</u> Assume R20 main steel, R8 binders and 25 mm cover. Overall depth = 343,75 + 10 + 8 + 25 Overall depth = 386,75 mm (Use overall depth = 400 mm)</p>	<p>(SABS 0144 Cl 6.1 and SABS 0100–2 Cl 8.2)</p>	
	<p><u>Determine the design dead loads of the beam</u> Design dead load = Volume × density × $9,81 \times 10^{-3} \times 1,2 \text{ Gn}$ DDL = $0,40 \times 0,27 \times 1 \times 2\,400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2 \text{ Gn}$ Design dead load = 3,05 kNm Design imposed UDL = $3,5 \text{ kNm} \times 1,6 \text{ Qn} = 5,6 \text{ kNm}$</p>	<p>Cl 4.2.2.1 Cl 4.2.2.1</p>	
	<p><u>Calculate the maximum bending moment</u> $BM_{\max} = \frac{WL^2}{8} + \frac{WL^2}{8}$ $BM_{\max} = \frac{3,05 \times 5,5^2}{8} + \frac{5,6 \times 5,5^2}{8}$ $= 11,53 + 21,175$ $BM_{\max} = 32,71 \text{ kNm}$</p>		
	<p><u>Calculate the value for 'K'</u> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{32,71 \times 10^6}{25 \times 270 \times 386,75^2}$ $K = 0,03 < K^1 = 0,156$ Provide tension reinforcement only.</p>	<p>(Cl 4.3.3.4.1)</p>	

<p><u>Calculate the distance of the lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k}{0,9}} \right\} \leq 0,95d$ $Z = 386,75 \left\{ 0,5 + \sqrt{0,25 - \frac{0,03}{0,9}} \right\} \leq 0,95 \times 386,75$ $Z = 386,75 \{0,965\} \geq 367,4$ $Z = 373,4 \text{ mm} > 367,4 \text{ mm}$	(Cl 4.3.3.4.1)	
<p>3.2 <u>Calculate the tension reinforcement</u></p> $A_s = \frac{M}{0,87 \times f_y \times z}$ $A_s = \frac{32,71 \times 10^6}{0,87 \times 250 \times 373,4}$ $A_s = 402,7 \text{ mm}^2$ <p>Use 4R12 ($A_s = 452 \text{ mm}^2$)</p> <p>(The minimum distance between bars is OK (Cl 11.4.8).</p>	(Cl 4.3.3.4.1)	(2)
<p>3.3 <u>Check for the minimum main reinforcement</u></p> $\frac{100 A_s}{A_c} = \frac{100 \times 425}{400 \times 270}$ $= 0,39$ <p>$0,39 > 0,8$</p> <p>The minimum reinforcement is not sufficient.</p>	Table 23 (Cl 4.11.4)	
<p><u>Check for the maximum area of reinforcement</u></p> <p>4% of AC</p> $4\% \times 400 \times 270$ $5\,120 \text{ mm}^2$ $425 < 4\,320$ <p>The max reinforcement is sufficient.</p>	(Cl 4.11.5.1)	

Exercise 1.2

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The following exercise focuses on double beams.

<p>1.</p>	<p><u>All references taken from SANS 10100-1 (2000)</u> $f_{cu} = 25 \text{ MPa}$ $f_y = 450 \text{ MPa}$ Span = 6,50 m Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) Cl 4.3.1.2 $2\,425 \text{ kg/m}^3$</p>	
	<p><u>Determine the effective depth (d):</u> $460 \text{ mm} - 50 \text{ mm (cover)} = 410 \text{ mm}$</p>		
	<p><u>Loading of the beam</u> Dead load = Volume \times density $\times 9,81 \times 10^{-3}$ $= 0,46 \times 0,22 \times 1 \times 2\,425 \text{ kg/m}^3 \times 9,81 \times 10^{-3}$ $= 2,407 \text{ kN/m}$ Design dead load = $2,407 \times 1,2 \text{ Gn} = 2,889 \text{ kNm}$ Design imposed load = $18 \text{ kN/m} \times 1,6 \text{ Qn} = 28,8 \text{ kN/m}$</p>		
	<p><u>Loading of the beam</u> Dead load = Volume \times density $\times 9,81 \times 10^{-3}$ $= 0,46 \times 0,22 \times 1 \times 2\,425 \text{ kg/m}^3 \times 9,81 \times 10^{-3}$ $= 2,407 \text{ kNm}$ Design dead load = $2,407 \times 1,2 \text{ Gn} = 2,889 \text{ kNm}$ Design imposed load = $18 \text{ kNm} \times 1,6 \text{ Qn} = 28,8 \text{ kNm}$</p>	<p>(Cl 4.2.2.1) (Cl 4.2.2.1)</p>	
	<p><u>Calculate the maximum bending moment</u> $BM_{\max} = \frac{WL^2}{8} + \frac{WL^2}{8}$ $BM_{\max} = \frac{2,889 \times 6,50^2}{8} + \frac{28,8 \times 6,50^2}{8}$ $BM_{\max} = 15,26 + 152,10$ $BM_{\max} = 167,36 \text{ kNm}$</p>		
	<p><u>Calculate the value for 'K'</u> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{167,36 \times 10^6}{25 \times 220 \times 410^2}$ $K = 0,181 > K^1 = 0,156$ Tension and compression reinforcement required.</p>	<p>(CL 4.3.3.4.1)</p>	

<p><u>Determine the compression reinforcement</u></p> $A_s = \frac{(K - K^1) f_{cu} b d^2}{f_{yc} \times (d - d^1)}$ $A_s = \frac{(0,181 - 0,156) 25 \times 220 \times 410^2}{327 \times (410 - 35)}$ $A_s = \frac{23\,113\,750}{122\,625}$ $A_s = 188,49 \text{ mm}^2$ <p>Use 2Y12 bars ($A_s = 226 \text{ mm}^2$)</p>	<p>(Cl 4.3.3.4)</p> $F_{yc} = \frac{F_y}{1,15 + \frac{F_y}{2\,000}}$ $F_{yc} = \frac{450}{1,15 + \frac{450}{2\,000}}$ <p>$F_{yc} = 327 \text{ MPa}$</p>	
<p><u>Calculate the distance of the lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K^1}{0,9}} \right\}$ $Z = 410 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 410(0,777)$ $Z = 318,6 \text{ mm}$	<p>(Cl 4.3.3.4)</p>	
<p><u>Calculate the tension reinforcement</u></p> $A_s = \frac{K^1 f_{cu} b d^2}{0,87 f_y Z} + \frac{A_s' f_{yc} b d^2}{0,87 f_y}$ $A_s = \frac{0,156 \times 25 \times 220 \times 410^2}{0,87 \times 450 \times 318,6} + \frac{226 \times 327}{0,87 \times 450}$ $A_s = \frac{144\,229\,800}{124\,731,9} + \frac{73\,902}{391,5}$ $A_s = 1\,156,32 + 188,77$ $A_s = 1\,345,09 \text{ mm}^2$ <p>Use 3Y25 bars ($A_s = 1\,473 \text{ mm}^2$)</p>	<p>(Cl 4.3.3.4.1)</p>	
<p><u>Check the minimum area of reinforcement</u></p> $\frac{100 A_s}{A_C}$ $\frac{100 \times 1\,473}{460 \times 220} = 1,46 > 0,45 \text{ okay}$ <p><u>Check maximum area of reinforcement</u></p> <p>4% of AC</p> $4\% \times (460 \times 220) = 4\,048 \text{ mm}^2 \text{ okay}$	<p>Table 23</p> <p>(Cl 4 11.5.4)</p>	

2	<p><u>All references taken from SANS 10100-1 (2000)</u> $F_{cu} = 25 \text{ MPa}$ $F_y = 450 \text{ MPa}$ Span = 8 m Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) Clause 4.3.1.2 2 425 kg/m³</p>	(2)
2.1	<p><u>Determine the effective depth of the beam</u> Effective depth = span / 16 Effective depth = 8 000 / 16 Effective depth = 500 mm</p>	<p>Table 10 (4.3.6.2.1)</p>	
	<p><u>Determine the overall depth</u> Assume Y25 main steel and Y10 binders Assume Cover of 25 mm. $\text{Overall depth} = 500 + \frac{25}{2} + 10 + 25$ Overall depth = 547,5 mm (Use overall depth = 550 mm)</p>		
2.2	<p><u>Determine the design dead loads of the beam</u> Design dead load = Volume \times density $\times 9,81 \times 10^{-3} \times 1,2 \text{ Gn}$ $\text{DDL} = 0,55 \times 0,33 \times 1 \times 2 425 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2 \text{ Gn}$ Design dead load = 5,18 kNm</p> <p>Design imposed load = 36 kNm $\times 1,6 \text{ Qn}$ Design imposed load = 57,6 kNm</p> <p>Total design load = 5,18 + 57,6 = 62,78 kNm</p>	<p>(Cl 4.2.2.1)</p> <p>(Cl 4.2.2.1)</p>	
2.3	<p><u>Calculate the maximum bending moment</u> $\text{BM}_{\max} = \frac{WL^2}{8}$ $\text{BM}_{\max} = \frac{62,78 \times 8,0^2}{8}$ $\text{BM}_{\max} = 502,25 \text{ kNm}$</p>	<p>(Cl 4.3.3.4.1)</p>	

<p>Calculate the value for 'K'</p> $k = \frac{BM}{f_{cu} b d^2}$ $k = \frac{502,25 \times 10^6}{25 \times 330 \times 500^2}$ $k = 0,244 > K^1 = 0,156$ <p>Tension and compression reinforcement required.</p>		
<p>2.4 Calculate the distance of the lever arm (Z)</p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k^1}{0,9}} \right\}$ $Z = 500 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 500 \{0,777\}$ $Z = 388,50 \text{ mm}$	(Cl 4.3.3.4.1)	
<p>2.5 Determine the compression reinforcement</p> $A_s = \frac{(k - k^1) F_{cu} b d^2}{F_{yc} (d - d^1)} \quad (\text{Use } d^1 = 50 \text{ mm})$ <p>Where: $F_{yc} = \frac{F_y}{1,15 + \frac{F_y}{2000}}$</p> $F_{yc} = \frac{450}{1,15 + \frac{450}{2000}}$ $F_{yc} = 327 \text{ Mpa}$ $A_s = \frac{(0,244 - 0,156) 25 \times 330 \times 500^2}{327 (500 - 50)}$ $A_s = 1\,233,44 \text{ mm}^2$ <p>Use 4Y20 ($A_s = 1\,257 \text{ mm}^2$)</p>	(Cl 4.3.3.4.1)	Figure 2 $\gamma_m = 1,15$ (Cl 3.3.3.2)
<p>Check for the minimum compression reinforcement</p> $\frac{100 A_s}{A_c} = \frac{100 \times 1\,257}{550 \times 330}$ $= 1,06$ $0,69 > 0,24$ <p>The reinforcement is sufficient.</p>	Table 23 (Cl 4.11.4)	(1)

2.6	<p><u>Determine the tension reinforcement</u></p> $A_s = \frac{k^1 F_{cu} b d^2}{0,87 \times f_y \times z} + \frac{A's F_{yc}}{0,87 \times f_y}$ $A_s = \frac{0,156 \times 25 \times 330 \times 500^2}{0,87 \times 450 \times 388,5} + \frac{1\ 257 \times 327}{0,87 \times 450}$ $A_s = 2\ 115,42 + 1\ 049,91$ $A_s = 3\ 165,33\ \text{mm}^2$ <p>Use 4y32 ($A_s = 3\ 217\ \text{mm}^2$)</p>	(Cl 4.3.3.4.2)	
2.7	<p><u>Check for the minimum main reinforcement</u></p> $\frac{100 A_s}{A_c} = \frac{100 \times 3\ 217}{550 \times 330}$ $= 1,77$ <p>$1,77 > 0,45$</p> <p>The reinforcement is sufficient.</p>	Table 23 (Cl 4.11.4)	
	<p><u>Check for the maximum area of reinforcement</u></p> <p>4% of AC</p> $4\% \times 550 \times 330$ $5\ 940\ \text{mm}^2$ $(3\ 217 + 1\ 257) < 7\ 260$ <p>The reinforcement is sufficient.</p>	(Cl 4.11.5.1)	
3.	<p><u>All references taken from SANS 0100-1 (2000)</u></p> <p>$F_{cu} = 30\ \text{MPa}$</p> <p>$F_y = 450\ \text{MPa}$</p> <p>Maximum bending moment = 160 kNm</p> <p>Effective depth = 350 mm</p>	Table 2 (4.1.5.1) Table 3 (4.1.5.2)	
	<p><u>Calculate the value for 'K'</u></p> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{160 \times 10^6}{30 \times 230 \times 350^2}$ $K = 0,19 > K^1 = 0,156$ <p>Tension and compression reinforcement required.</p>	(Cl 4.3.3.4.1)	(2)

<p><u>Calculate the compression reinforcement</u></p> $A_s = \frac{(k - k^1) F_{cu} b d^2}{F_{yc} (d - d^1)}$ <p>Where: $F_{yc} = \frac{F_y}{1,15 + \frac{F_y}{2000}}$</p> $F_{yc} = \frac{450}{1,15 + \frac{450}{2000}}$ $F_{yc} = 327 \text{ MPa}$ $A_s = \frac{(0,19 - 0,156) 30 \times 230 \times 350^2}{327 (350 - 50)}$ $A_s = 293 \text{ mm}^2$ <p>Use 3Y12 ($A_s = 339 \text{ mm}^2$)</p>	<p>(Cl 4.3.3.4.1)</p> <p>Figure 2 $\gamma_m = 1,15$ (Cl 3.3.3.2)</p> <p>(Use $d^1 = 50$ mm)</p>	(3)
<p><u>Check for the minimum compression reinforcement</u></p> $\frac{100 A_s}{A_c} = 0,4$ $\frac{100 \times 339}{600 \times 300} = 0,19$ $0,19 < 0,4$ <p>The reinforcement is <u>not</u> sufficient.</p>	<p>Table 23 (Cl 4.11.4)</p>	(2)
<p><u>Calculate the distance of the lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k^1}{0,9}} \right\}$ $Z = 350 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 350 \{0,777\}$ $Z = 271,95 \text{ mm}$	<p>(Cl 4.3.3.4.1)</p>	(2)
<p><u>Calculate the tension reinforcement</u></p> $A_s = \frac{K^1 f_{cu} b d^2}{0,87 f_y Z} + \frac{A_s' f_{yc} b d^2}{0,87 f_y}$ $A_s = \frac{0,156 \times 30 \times 230 \times 350^2}{0,87 \times 450 \times 271,95} + \frac{339 \times 327}{0,87 \times 450}$ $A_s = \frac{131\,859\,000}{106\,468,425} + \frac{110\,944,53}{391,5}$ $A_s = 1\,238,48 + 283,15$ $A_s = 1\,521,63 \text{ mm}^2$ <p>Use 5Y20 bars ($A_s = 1\,571 \text{ mm}^2$)</p>	<p>(Cl 4.3.3.4.1)</p>	(4)

<p><u>Check for the minimum main reinforcement</u></p> $\frac{100 A_s}{A_c} = 0,45$ $\frac{100 \times 1571}{600 \times 300} = 0,87$ $0,45 < 0,87$ <p>The reinforcement is sufficient.</p>	<p>Table 23 (Cl 4.11.4)</p>	<p>(2) [15]</p>
<p>4. <u>Determine the area of steel in tension:</u></p> $A_s = 3 \times \frac{\pi 20^2}{4}$ $A_s = 942 \text{ mm}$	<p>CL 4.3.6.2.1 Table 10</p>	
<p><u>Check for the minimum main reinforcement</u></p> $\frac{100 A_s}{A_c} = \frac{100 \times 942}{480 \times 270}$ $= 0,72$ $0,72 > 0,3$ <p>The reinforcement is sufficient.</p>	<p>Table 23 (Cl 4.11.4)</p>	
<p><u>Calculate the distance of the lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k^1}{0,9}} \right\}$ $Z = \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 430 \times 0,777$ <p>Use Z = 334,11 mm</p>	<p>(Cl 4.3.3.4.1)</p>	
<p><u>The maximum moment of resistance in tension</u></p> $M = A_s 0,87 f_y z$ $M = 942 \times 0,87 \times 450 \times 334,11$ $M = 123,2 \text{ kNm}$	<p>(Cl 4.3.3.4.1)</p>	<p>(2)</p>
<p><u>Determine the area of steel in compression</u></p> $A'_s = 3 \times \frac{\pi 16^2}{4}$ $A'_s = 603 \text{ mm}$	<p>CL 4.3.6.2.1 Table 10</p>	

<p><u>Check for the minimum reinforcement</u></p> $\frac{100 A_s}{A_c} = \frac{100 \times 603}{480 \times 270}$ $= 0,31$ <p>0,47 > 0,2</p> <p>The reinforcement is sufficient.</p>	Table 23 (Cl 4.11.4)	
<p><u>The maximum moment of resistance in compression</u></p> <p>Substitute: $K = \frac{M}{b d^2 f_{cu}}$ into $A_s = \frac{(K - K^1)}{f_{cu} (d - d^1)}$</p> <p>Then: Make M the subject of the formula:</p> $M = A_s f_{yc} (d - d_1) + 0,156 f_{cu} b d^2$ $M = 603 \times 327,27 \times (430 - 40) + 0,156 \times 25 \times 270 \times 430^2$ $M = 76\,964\,085,9 + 194\,699\,700$ $M = 271,66 \text{ kNm}$ <div style="border: 1px solid black; padding: 5px; margin-top: 10px;"> $f_{yc} = \frac{fy}{1,15 + \frac{fy}{2000}}$ $f_{yc} = \frac{450}{1,15 + \frac{450}{2000}}$ $F_{yc} = 323,27 \text{ MPa}$ </div>	Cl 4.3.3.4.1	
<p><u>Use the lesser of the two bending moments</u></p> <p>Maximum moment of resistance in tension = 123,2 kNm</p> <p>Maximum moment of resistance in compression = 271,66 kNm</p> <p>Therefore: the lesser BM = 123,2 kN</p>		
<p><u>Determine the total load</u></p> $BM_{\max} = \frac{wl^2}{8}$ $123,2 = \frac{w \times 7^2}{8}$ $w = \frac{123,2 \times 8}{7^2}$ $w = 20,11 \text{ kN m}$		
<p><u>Determine the dead load</u></p> $\text{Dead load} = \text{area} \times \text{density} \times 9,81 \times 10^{-3}$ $\text{Dead load} = 0,48 \times 0,27 \times 2\,415 \text{ kg/m}^3 \times 9,81 \times 10^{-3}$ $\text{Dead load} = 3,07 \text{ kNm}$		

<u>Determine the maximum imposed load</u> Total load = 1,2 (Gn) + 1,6 (Qn) $20,11 = 1,2 (3,07) + 1,6 (Qn)$ $20,1 = 3,68 + 1,6 Qn$ $Qn = 10,26 \text{ kNm}$	(4.2.2.1)	
<u>The maximum imposed load</u> $\therefore Qn = 10,26 \text{ kNm}^2$		

Exercise 1.3

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The following exercise focuses on rectangular beams.

1.1	<u>All references taken from SANS 10100-1 (2000)</u> $f_{cu} = 25 \text{ MPa}$ $f_y = 450 \text{ MPa}$ Effective Span = 6,0 m Density of reinforced concrete	Table 2 (4.1.5.1) Table 3 (4.1.5.2) Clause 4.3.1.2 2415 kg/m^3	
	<u>Determine the effective depth (d):</u> $600 \text{ mm} - 45 \text{ mm (cover)} = 555 \text{ mm}$		
	<u>Loading of the beam</u> Dead load = Volume \times density $\times 9,81 \times 10^{-3} \times 1,2Gn$ $= 0,6 \times 0,3 \times 2415 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2Gn$ $= 5,12 \text{ kN/m}$ <u>Design imposed load</u> = $24 \text{ kNm} \times 1,6Qn = 38,4 \text{ kN/m}$	(Cl 4.2.2.1) (Cl 4.2.2.1)	
	<u>Calculate the maximum bending moment</u> $BM_{\max} = \frac{WL^2}{8} + \frac{WL^2}{8}$ $BM_{\max} = \frac{5,12 \times 6^2}{8} + \frac{38,4 \times 6^2}{8}$ $BM_{\max} = 23,04 + 172,8$ $BM_{\max} = 195,84 \text{ kNm}$		(3)

<p><u>Calculate the value for 'K'</u></p> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{195,84 \times 10^6}{30 \times 300 \times 555^2}$ $K = 0,07 < K^1 0,156$ <p>Use tension reinforcement only.</p>	(Cl 4.3.3.4.1)	
<p><u>Calculate the distance of the lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k}{0,9}} \right\} \leq 0,95 d$ $Z = 555 \left\{ 0,5 + \sqrt{0,25 - \frac{0,07}{0,9}} \right\} \leq 0,95 \times 555$ $Z = 555\{0,91\} \leq 527,25$ $Z = 505,05 \text{ mm} < 527,25$ <p>Use Z = 505,05 mm (least Z)</p>	(Cl 4.3.3.4.1)	
<p><u>Calculate the tension reinforcement</u></p> $A_s = \frac{M}{f_y \times 0,87 \times z}$ $A_s = \frac{195,84 \times 10^6}{450 \times 0,87 \times 505,05}$ $A_s = 989,6 \text{ mm}^2$ <p>Use 4Y20 ($A_s = 1\,257 \text{ mm}^2$)</p>	(Cl 4.3.3.4.1)	
<p><u>Check for the minimum main reinforcement</u></p> $\frac{100 A_s}{A_c} = \frac{100 \times 1\,257}{600 \times 300}$ $0,69 > 0,45$ <p>The reinforcement is sufficient.</p>	Table 23 (Cl 4.11.4)	
<p><u>Check the maximum reinforcement</u></p> <p>4% of A_c</p> $4\% \times 600 \times 300$ $= 7\,200 \text{ mm}^2$ $1\,885 \text{ mm}^2 < 7\,200 \text{ mm}^2$	Cl 4.11.5.1	

2.2 Shear force diagram

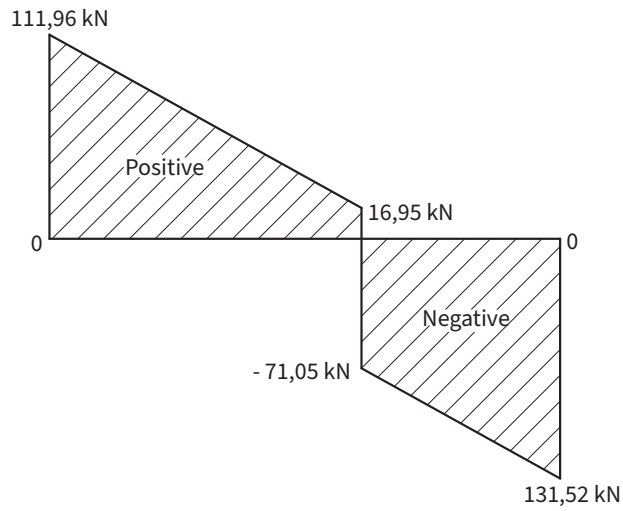


Figure 1.2

2.3

Calculate the maximum bending moment

$$\text{BM at 'C': } (131,52 \times 3,5) - (12,8 \times 3,5 \times 1,75) - (4,475 \times 3,5 \times 1,75)$$

$$460,32 - 78,4 - 27,41$$

$$\text{BM at 'C'} = 354,51 \text{ kNm}$$

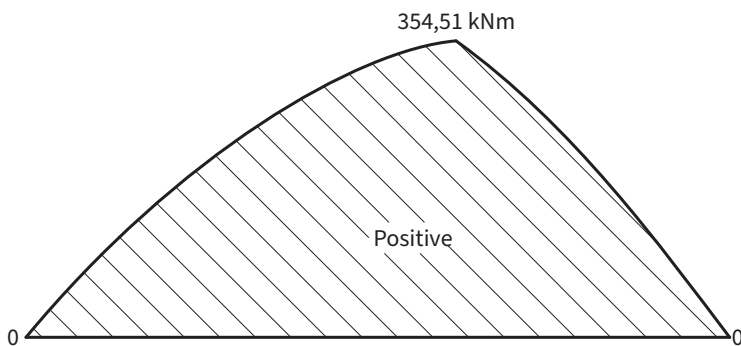
2.4 Bending moment diagram

Figure 1.3

2.5	<p>Calculate the value for 'K'</p> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{354,51 \times 10^6}{25 \times 330 \times 425^2}$ <p>K = 0,238 K < K¹ = 0,156 Compression reinforcement will therefore be required.</p>	<p>(Cl 4.3.3.4.1)</p> <p>d = 475 – 50 cover = 425 mm</p>	
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Exercise 1.4

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The following exercise focuses on slabs.

1.	<p>All references taken from SANS 0100-1 (2000)</p> <p>F_{cu} = 25 MPa F_y = 450 MPa Span = 4,5 mm Imposed live load</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) Clause 4.3.1.2 7,75 kNm²</p>	
	<p>Determine the effective dead loads of the slab</p> <p>Effective depth = Span/16 Effective depth = 4 500 / 16 Effective depth = 281,25 mm</p>	<p>Table 10 Cl 4.3.6.2.1</p>	
	<p>Determine the overall depth of the slab</p> <p>Assume Y16 main steel and 25 mm cover. Overall depth = 281,25 + 16/2 + 25 Overall depth = 315,25 mm (Use overall depth = 320 mm)</p>		



Important

The main steel lies below the secondary steel. Always round off to the nearest whole number; do not use decimals.

<p><u>Determine the design dead loads of the beam</u></p> <p>Design dead load = area \times density \times g.a $\times 10^{-3} \times 1,2G_n$ $= 0,320 \times 1 \text{ m} \times 2\,400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2G_n$ Design dead load = 9 kNm</p> <p>Design imposed live load = $7,75 \text{ kNm}^2 \times 1 \text{ m} \times 1,6Q_n$ Design imposed live load = 12,4 kNm Total design load = $9 + 12,4 = 21,4 \text{ kNm}$</p>	Cl 4.2.2.1	
<p><u>Calculate the maximum bending moment</u></p> $BM_{\max} = \frac{WL^2}{8}$ $BM_{\max} = \frac{21,4 \times 4,5^2}{8}$ $BM_{\max} = 54,17 \text{ kNm}$		
<p><u>Calculate the value for 'K'</u></p> $K = \frac{M}{f_{cu} b d^2}$ $K = \frac{54,17 \times 10^6}{25 \times 1\,000 \times 281,25^2}$ $K = 0,027$ $K < K^1 = 0,156 \text{ (only tension reinforcement required.)}$		
<p><u>Calculate the distance of the lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k}{0,9}} \right\} \leq 0,95 d$ $Z = 281,25 \left\{ 0,5 + \sqrt{0,25 - \frac{0,027}{0,9}} \right\} \leq 0,95 \times 281,25 \text{ mm}$ $Z = 281,25 \{0,969\} \leq 272,54 \text{ mm}$ $Z = 272,54 \text{ mm} > 258,92 \text{ mm}$ <p>Use lever arm = 258,92 mm (Lesser of the two)</p>	(Cl 4.3.3.4.1)	
<p><u>Calculate the tension reinforcement</u></p> $A_s = \frac{M}{0,87 \times f_y \times z}$ $A_s = \frac{54,17 \times 10^6}{0,87 \times 450 \times 258,92}$ $A_s = 534,4 \text{ mm}^2$ <p>Use Y10 at 125 centres ($A_s = 628 \text{ mm}^2$)</p>	(Cl 4.3.3.4.1)	



Note

The width of the slab is 1 000 mm or 1 m.

<p><u>Check for the minimum main reinforcement</u></p> $\frac{100 \times A_s}{A_c} = 0,13$ $\frac{100 \times 628}{1000 \times 320} = 0,22$ <p>0,19 > 0,13</p> <p>The reinforcement is sufficient.</p>	<p>Table 23 (Cl 4.11.4)</p>	
<p><u>Determine the secondary reinforcement</u></p> $\frac{100 A_s}{A_c} = 0,24$ $A_s = \frac{0,24 \times 1\,000 \times 320}{100}$ $A_s = 768 \text{ mm}^2$ <p>Use Y10 at 100 centres ($A_s = 785 \text{ mm}^2$)</p>	<p>Cl 4.11.4.3.1 & Table 23</p>	
<p>2. <u>All references taken from SANS 0100-1 (2000)</u></p> <p><u>Determine the area of the main steel</u></p> <p>Y12 at 200 centres: $A_s = 1\,005 \text{ mm}^2$</p>		
<p><u>Calculate the distance of the lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K^1}{0,9}} \right\}$ $Z = 185 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 815 \{0,777\}$ $Z = 143,75 \text{ mm}$	<p>(Cl 4.3.3.4.1)</p>	
<p><u>Calculate the maximum moment of resistance</u></p> $A_s = \frac{M}{0,87 \times f_y \times z}$ $M = 0,87 \times f_y \times Z \times A_s$ $M = 0,87 \times 250 \times 143,75 \times 1\,005$ $M = 31,42 \text{ kNm}$	<p>(Cl 4.3.3.4.1)</p>	

<p><u>Determine the total load</u></p> $BM_{\max} = \frac{wl^2}{8}$ $31,42 = \frac{w \times 4,5^2}{8}$ $w = \frac{31,42 \times 8}{4,5^2}$ $w = 12,41 \text{ kNm}$		
<p><u>Determine the dead load</u></p> <p>Dead load = Area \times density $\times 9,81 \times 10^{-3}$</p> <p>Dead load = $0,215 \times 1 \times 2\,400 \text{ kg/m}^3 \times 9,81 \times 10^{-3}$</p> <p>Dead load = 5,062 kNm</p>		
<p><u>Determine the maximum imposed load</u></p> <p>Total load = 1,2 (Gn) + 1,6 (Qn)</p> $12,41 = 1,2 (5,062) + 1,6 (Qn)$ $Qn = 3,959 \text{ kNm}$	(Cl 4.2.2.1)	

3. All references taken from SANS 0100-1 (2000)

<p>$f_{cu} = 25 \text{ MPa}$</p> <p>$f_y = 250 \text{ MPa}$</p> <p>Span = 4,2 mm</p> <p>Imposed live load</p>	<p>Table 2 (4.1.5.1)</p> <p>Table 3 (4.1.5.2)</p> <p>Clause 4.3.1.2</p> <p>6 kNm²</p>	
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Determine the effective dead loads of the slab

<p>Effective depth = Span/16</p> <p>Effective depth = $4\,200/16$</p> <p>Effective depth = 263 mm</p>	<p>Table 10</p> <p>Cl 4.3.6.2.1</p>	
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Determine the overall depth of the slab

<p>Assume Y16 main steel and 25 mm cover.</p> <p>Overall depth = $263 + 16/2 + 25$</p> <p>Overall depth = 291 mm (Use overall depth = 300 mm)</p>	<p>SANS 0144</p> <p>Cl 6.1 and</p> <p>SANS 0100-2</p> <p>Cl 8.2</p>	
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Important

The main steel lies below the secondary steel. Encourage students to round off to the nearest whole number; they must not use decimals.

<p><u>Determine the design dead loads of the beam</u></p> <p>Design dead load = area × density × g.a × 10⁻³ × 1,2Gn = 0,300 × 1m × 2 400 kg/m³ × 9,81 × 10⁻³ × 1,2Gn Design dead load = 8,48 kNm</p> <p>Design imposed live load = 6 kNm² × 1 m × 1,6Qn Design imposed live load = 9,6 kNm</p>	<p>Cl 4.2.2.1</p>	
<p><u>Calculate the maximum bending moment</u></p> $BM_{\max} = \frac{WL^2}{8} + \frac{WL^2}{8}$ $= \frac{8,48 \times 4,2^2}{8} + \frac{9,6 \times 4,2^2}{8}$ <p>BM_{max} = 18,7 + 21,2 BM_{max} = 39,87 kNm</p>		

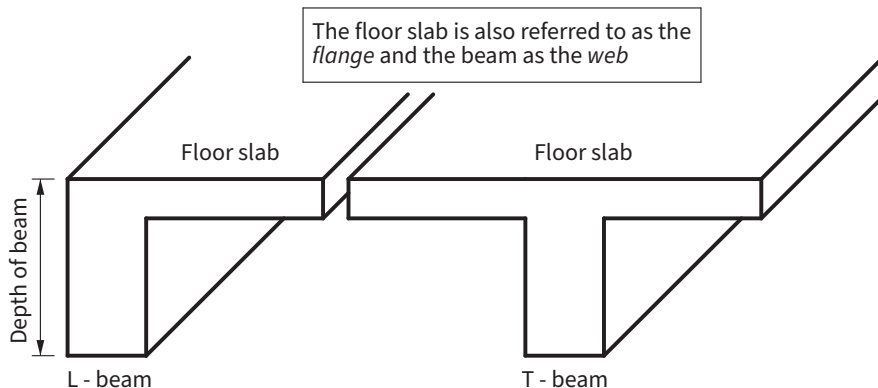


Figure 1.4

<p><u>Calculate the value for 'K'</u></p> $K = \frac{M}{f_{cu} b d^2}$ $K = \frac{39,87 \times 10^6}{25 \times 1\,000 \times 263^2}$ <p>K = 0,023 K < K¹ = 0,156 (Only tension reinforcement required.)</p>	<p>Cl 4.3.3.4.1</p>	
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<p><u>Calculate the distance of the lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k}{0,9}} \right\} \leq 0,95 d$ $263 \left\{ 0,5 + \sqrt{0,25 - \frac{0,023}{0,9}} \right\} \leq 0,95 \times 263 \text{ mm}$ $Z = 263\{0,97\} \leq 249,9 \text{ mm}$ $Z = 256 \text{ mm} > 249,9 \text{ mm}$ <p>Use lever arm = 249,9 mm (Lesser of the two)</p>	(Cl 4.3.3.4.1)	
<p><u>Calculate the tension reinforcement</u></p> $A_s = \frac{M}{0,87 \times f_y \times z}$ $A_s = \frac{39,87 \times 10^6}{0,87 \times 250 \times 249,9}$ $A_s = 733,5 \text{ mm}^2$ <p>Use R20 at 150 centres ($A_s = 754 \text{ mm}^2$)</p>	(Cl 4.3.3.4.1)	
<p><u>Check for the minimum main reinforcement</u></p> $\frac{100 \times A_s}{A_c} = 0,13$ $\frac{100 \times 754}{1000 \times 300} = 0,25$ $0,25 > 0,13$ <p>The reinforcement is sufficient.</p>	Table 23 (Cl 4.11.4)	
<p><u>Determine the secondary reinforcement</u></p> $\frac{100 A_s}{A_c} = 0,24$ $A_s = \frac{0,24 \times 1\,000 \times 300}{100}$ $A_s = 720 \text{ mm}^2$ <p>Use R12 at 150 centres ($A_s = 754 \text{ mm}^2$)</p>	Cl 4.11.4.3.1 & Table 23	

Exercise 1.5

SB page 89

1.	<p><u>All references taken from SANS 10100-1 (2000)</u></p> <p>$f_{cu} = 25 \text{ MPa}$</p> <p>$f_y = 450 \text{ MPa}$</p> <p>5Y20 steel rods</p>	<p>Table 2 (4.1.5.1)</p> <p>Table 3 (4.1.5.2)</p> <p>Area = 1 571 mm²</p>	
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<p><u>Calculate the lever arm distances</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K^1}{0,9}} \right\} \leq 0,95d$ $Z = 475 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\} \leq 0,5 \times 475$ $Z = 475(0,777) \leq 0,95 \times 475$ $Z = 369,08 \text{ mm} \leq 451,25$ <p>Use $Z = 369,08 \text{ mm}$</p>	(Cl 4.3.3.4.1)	
<p><u>Calculate the bending moment due to the concrete</u></p> $k = \frac{BM}{f_{cu} b d^2}$ $Bm = k \times f_{cu} \times b \times d^2$ $Bm = 0,156 \times 25 \times 1150 \times 475^2$ $Bm = 1\,011,93 \text{ kNm}$	(Cl 4.3.3.4.1)	
<p><u>Calculate the bending moment due to the reinforcement</u></p> $A_s = \frac{BM}{0,87 f_y z}$ $Bm = A_s \times 0,87 \times f_y \times z$ $Bm = 1\,571 \times 0,87 \times 450 \times 369,075$ $Bm = 226,9 \text{ kNm}$		
<p>Bending moment maximum is due to the reinforcement = 226,9 kNm</p>		
<p>2. <u>All references taken from SANS 10100-1 (2000)</u> $f_{cu} = 25 \text{ MPa}$ $f_y = 450 \text{ MPa}$</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2)</p>	
<p><u>Calculate the value for 'K'</u></p> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{285 \times 10^6}{25 \times 1\,155 \times 525^2}$ $K = 0,036 < k^1 = 0,156$	(Cl 4.3.3.4.1)	

	<p><u>Calculate the lever arm distances</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k}{0,9}} \right\} \leq 0,95d$ $Z = 525 \left\{ 0,5 + \sqrt{0,25 - \frac{0,039}{0,9}} \right\} \leq 0,95 \times 525$ $Z = 525(0,955) \leq 0,95 \times 525$ $Z = 501,17 \text{ mm} \geq 498,75$ <p>Use $Z = 498,75 \text{ mm}$</p>	(Cl 4.3.3.4.1)	
	<p><u>Calculate the area of reinforcement</u></p> $A_s = \frac{BM}{f_y 0,87 Z}$ $A_s = \frac{285 \times 10^6}{450 \times 0,87 \times 498,75}$ $A_s = 1\,459,59 \text{ mm}^2$ <p>Use 3Y25 bars ($A_s = 1\,473 \text{ mm}^2$)</p>	(Cl 4.3.3.4.1)	
3.	<p><u>All references taken from SANS 10100-1 (2000)</u></p> <p>$f_{cu} = 25 \text{ MPa}$</p> <p>$f_y = 450 \text{ MPa}$</p> <p>Effective span =</p> <p>Dead load</p> <p>Imposed load</p>	<p>Table 2 (4.1.5.1)</p> <p>Table 3 (4.1.5.2)</p> <p>7,5 m</p> <p>13,5 kNm²</p> <p>9 kNm²</p>	
3.1	<p><u>Calculate the lever arm distances</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K^1}{0,9}} \right\}$ $Z = 350 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 505 (0,777)$ $Z = 271,95 \text{ mm}$	(CL 4.3.3.4.1)	
3.2	<p><u>Calculate the total design load</u></p> $W = 1,2(G_n) + 1,6(Q_n)$ $W = 1,2(13,5 \times 1) + 1,6(9 \times 1)$ $W = 16,2 + 14,4$ $W = 30 \text{ kNm}$	(Cl 4.3.3.4.1)	

3.3	<p><u>Calculate the maximum bending moment</u></p> $BM = \frac{wl^2}{8}$ $BM = \frac{30,6 \times 7^2}{8}$ $BM = 81,25 \text{ kNm}$		
3.4	<p><u>Calculate the tension reinforcement</u></p> $A_s = \frac{M}{0,87 \times f_y Z}$ $A_s = \frac{187,43 \times 10^6}{0,87 \times 20 \times 271,95}$	(Cl 4.3.3.4)	
4.	<p><u>All references taken from SANS 10100-1 (2000)</u></p> <p>F_{cu} = 30 MPa F_y = 450 MPa Effective span Dead load Imposed load</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) 5,75 m 14 kN/m² 9,25 kN/m²</p>	
4.1	<p><u>Calculate the effective width</u></p> <p>The web width + Lz/5 Web width = 250 + $\frac{5 \times 750}{5}$ Web width = 250 + 1 150 Web width (X) = 1 400 mm</p>	(Cl 4.3.1.5 (a))	
4.2	<p><u>Calculate the lever arm distances</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K^1}{0,9}} \right\}$ $Z = 585 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 585 (0,777)$ $Z = 376,85 \text{ mm}$	(Cl 4.3.3.4.1)	

4.3 Calculate the total design load

$$W = 1,2(G_n) + 1,6(Q_n)$$

$$W = 1,2(14 \times 1) + 1,6(9,5 \times 1)$$

$$W = 16,8 + 15,2$$

$$W = 32 \text{ kN/m}$$

(Cl 4.3.3.4.1)

4.4 Calculate the maximum bending moment

$$BM = \frac{wl^2}{8}$$

$$BM = \frac{32 \times 5,75^2}{8}$$

$$BM = 132,25 \text{ kNm}$$

4.5 Calculate the tension reinforcement

$$A_s = \frac{m + 0,1 f_{cu} b_w d (0,45d - h_f)}{0,87 f_y (d - 0,5 h_f)}$$

$$A_s = \frac{132,25 \times 10^6 + (0,1 \times 30 \times 250 \times 485) (0,45 \times 485 - 120)}{0,87 \times 450 (485 - 0,5 \times 120)}$$

$$A_s = \frac{132,25 \times 10^6 + (363\,750) (98,25)}{0,87 \times 450 (425)}$$

$$A_s = \frac{132,25 \times 10^6 + 397\,618,5}{166\,387,5}$$

$$A_s = \frac{264\,000\,000}{163\,451,25}$$

$$A_s = 1\,586 \text{ mm}^2$$

Use 4Y20 bars ($A_s = 1\,257 \text{ mm}^2$)

The neutral axis lies below the flange
(Cl 4.3.3.4.2)

4.6 Check the distance between the bars

$$250 - 2(25 \text{ cover}) - 4(20 \text{ bars}) = 120.$$

$$4 \text{ bars} = 3 \text{ spaces} = 120/3 = 40 \text{ mm.}$$

Spacing between bars is okay SANS 0144:2 000

Exercise 1.6

SB page 97

1. All references taken from SANS 0100-1 (2000)

$F_{cu} = 30 \text{ MPa}$
 $F_y = 450 \text{ MPa}$
 Span = 7,0 m

Table 2 (4.1.5.1)
 Table 3 (4.1.5.2)
 CL 4.3.1.5 (b)

1.1 Loading of the beam

Design dead load = $9 \text{ kNm}^2 \times 0,82 \text{ m} \times 1,2 \text{ Gn}$
 = 8,86 kNm

(Cl 4.2.2.1)

Design imposed load = $6 \text{ kNm}^2 \times 0,82 \text{ m} \times 1,6 \text{ Qn}$
 = 7,87 kNm

1.2 Calculate the maximum bending moment

$$BM_{\max} = \frac{WL^2}{8} + \frac{WL^2}{8}$$

$$BM_{\max} = \frac{8,86 \times 7,0^2}{8} + \frac{7,87 \times 7,0^2}{8}$$

$$BM_{\max} = 54,27 + 48,2$$

$$BM_{\max} = 102,47 \text{ kNm}$$

1.3 Calculate the distance of the lever arm (Z)

$$Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K}{0,9}} \right\}$$

$$Z = 300 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$$

$$Z = 300 (0,777)$$

$$Z = 233,1 \text{ mm}$$

(Cl 4.3.3.4.1)

1.4 Calculate the tension reinforcement

(The neutral axis lies within the flange.)

$$A_s = \frac{M}{0,87 f_y z}$$

$$A_s = \frac{102,47 \times 10^6}{0,87 \times 450 \times 233,1}$$

$$A_s = 1\,123 \text{ mm}^2$$

Use 4Y20 bars ($A_s = 1\,257 \text{ mm}^2$)

(Cl 4.3.3.4.1)



Note

Students may use any one of the two formulae. They don't need to use both.

Should the neutral axis be below the flange, do the following

$$M_u = 0,87 \times f_y \times A_s \left(d - \frac{hf}{2} \right)$$

$$A_s = \frac{M_u}{0,87 \times f_y \times \left(d - \frac{hf}{2} \right)}$$

$$A_s = \frac{102,47 \times 10^6}{0,87 \times 450 \times \left(300 - \frac{120}{2} \right)}$$

$$A_s = 1\,090,6 \text{ mm}^2$$

Use 3Y20 ($A_s = 1\,257 \text{ mm}^2$)

(Cl 4.3.3.4.3)

1.5

The minimum distance between the bars

Width of beam = 250 mm – 25 × 2 side cover = 200 mm

– 2 × 25 = 50 mm; 200 mm – 50 mm = 150 mm

Divide by 2 spacers then the distance between the bars =

75 mm (Minimum distance = 19 mm + 5 = 25 mm)

1.6

Check the minimum in the area of reinforcement

$$\frac{100 \times A_s}{b_w h} = \frac{100 \times 1\,257}{250 \times 120}$$

$$= 4,19 > 0,45 \text{ (Sufficient)}$$

Table 23

2.

All references taken from SANS 0100-1 (2000)

$f_{cu} = 25 \text{ MPa}$

$f_y = 450 \text{ MPa}$

Span = 6,750 m

Table 2 (4.1.5.1)

Table 3 (4.1.5.2)

Cl 4.3.1.5 (b)

2.1	<p><u>Calculate the effective width of the L-beam</u> Use the lesser of:</p> <p>1. Web width + $\frac{L_z}{10}$ $= 320 + \frac{6\,750}{10}$ $= 320 \text{ mm (0,320m)}$</p> <p>OR</p> <p>2. The actual width not given</p>	(Cl 4.3.1.2)	
2.2	<p><u>Calculate the design loads</u> Design dead load = $12,5 \text{ kNm}^2 \times 0,995 \text{ m} \times 1,2 \text{ Gn}$ $= 14,93 \text{ kNm}$</p> <p>Design imposed load = $7,75 \text{ kNm}^2 \times 0,995 \text{ m} \times 1,6 \text{ Qn}$ $= 12,34 \text{ kNm}$</p>	(Cl 4.2.2.1)	
2.3	<p><u>Calculate the maximum bending moment</u></p> $BM_{\max} = \frac{WL^2}{8} + \frac{WL^2}{8}$ $BM_{\max} = \frac{14,93 \times 6,75^2}{8} + \frac{12,34 \times 6,75^2}{8}$ $BM_{\max} = 81,44 + 70,28$ $BM_{\max} = 150,72 \text{ kNm}$		
2.4	<p><u>Calculate the distance of the lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k^1}{0,9}} \right\} \leq 0,95d$ $Z = 480 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\} \leq 0,95 \times 480$ $Z = 480 (0,777) \leq 0,95 \times 480$ $Z = 372,96 \text{ mm} < 456 \text{ mm}$ <p>Use $Z = 372,96 \text{ mm}$ (lesser between the two)</p>	(Cl 4.3.3.4.1)	

2.5	<p><u>Calculate the area of reinforcement</u> <i>Note: The neutral axis is within the flange.</i></p> $A_s = \frac{m}{0,87 f_y z}$ $A_s = \frac{150,72 \times 10^6}{0,87 \times 450 \times 372,96}$ $A_s = 1\,032,2 \text{ mm}^2$ <p>Use 4Y20 bars ($A_s = 1\,275 \text{ mm}^2$)</p>	(Cl 4.3.3.4.1)	
2.6	<p><u>The minimum distance between the bars</u> Width of beam = 320 mm – 25 × 2 side cover = 270 mm, –4 × 20 = 80 mm; 270 mm – 80 mm = 190 mm Divide by 3 spacers then distance between the bars = ± 60 mm. (Minimum distance = 19 mm + 5 = 25 mm)</p>		
2.7	<p><u>Check the minimum area of reinforcement</u></p> $\frac{100 \times A_s}{b w h} = \frac{100 \times 1\,257}{320 \times 180}$ $= 2,18 > 0,20 \text{ (Sufficient)}$	Table 23	

Exercise 1.7

SB page 107

1.	<p><u>All references taken from SANS 0100-1 (2000)</u></p>		
1.2	<p><u>Calculate the size of the pad foundation</u> Working load = 85 kN + 870 kN + 200 kN = 1 155 kN</p> $\text{Area} = \frac{\text{Force}}{\text{Pressure}}$ $\text{Area} = \frac{1\,155}{220}$ $\text{Area} = 5,25 \text{ m}^2$ <p>For the square base $\sqrt{5,25} = 2,29 \text{ m} \times 2,29 \text{ m}$ Use a base of 2,30 m × 2,30 m</p>		

2.	<u>All references taken from SANS 0100-1 (2000)</u>		
2.1	<u>Calculate the ultimate axial load</u> $N = 0,4 f_{cu} A_c + 0,67 f_y A_{sc}$ $N = 0,4 \times 30 \times (330 \times 220) + 0,67 \times 250 \times 1\ 885$ $N = 871\ 200 + 315\ 737,5$ $N = 1\ 186,94\ \text{kN}$	(Cl 4.7.4.3)	
2.2	<u>Calculate the diameter and spacing of the binders</u> <u>Binders:</u> $\frac{1}{4}$ of the smallest main bar $\frac{1}{4} \times 20 = 5\ \text{mm}$ (not available) Use: R8 binders. <u>Spacing of the binders:</u> $12 \times$ diameter of smallest main bar $12 \times 20 = 240\ \text{mm}$ (maximum) Use spacings of 240 mm centres.	Cl 4.11.4.5.1 (Cl 4.11.4.5.1)	
2.3	<u>Calculate the minimum and maximum area of the main steel</u> Minimum area of main steel: 0,4% AC $0,4\% \times 330 \times 220$ Minimum area = $290,4\ \text{mm}^2$ Maximum area of main steel: 6% AC $6\% \times 330 \times 220$ Minimum area = $4\ 356\ \text{mm}^2$ <u>Summary of round column</u> RC Column $330 \times 220\ \text{mm}$ with 6Y20 Main bars R8 binders at 240 mm c/c.	(Table 23) (Cl 4.11.5.2)	

2.4–2.5 Horizontal cross-sectional view of the column with dimensions

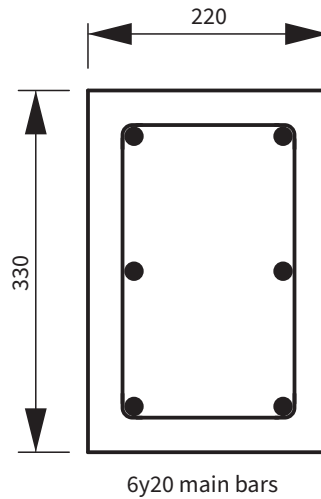


Figure 1.5

3. All references taken from SANS 0100-1 (2000)

3.1 Check for the short column

$$= \frac{Le}{b} < 10$$

$$= \frac{0,9 \times 3\,000 \text{ mm}}{280 \text{ mm}} < 10$$

$$= 9,6 < 10 \text{ okay}$$

Cl 4.7.1.4

3.2 Calculate the diameter and spacing of the binders.

Binders:

$\frac{1}{4}$ of the smallest main bar

$\frac{1}{4} \times 20 = 5 \text{ mm}$ (not available)

Use: R8 binders.

Cl 4.11.4.5.1

Spacing of the binders:

$12 \times$ diameter of smallest main bar

$12 \times 20 = 240 \text{ mm}$ (maximum)

Use spacings of 240 mm centres.

(Cl 4.11.4.5.1)

3.3 Calculate the area of reinforcement

$$N = 0,4 f_{cu} A_c + 0,67 f_y A_{sc}$$

(Cl 4.7.4.3)

$$A_{sc} = \frac{N - (0,4 f_{cu} A_c)}{0,67 f_y}$$

$$A_{sc} = \frac{1\,800 \times 10^3 - (0,4 \times 30 \times 400 \times 280)}{0,67 \times 450}$$

$$= \frac{1\,800 \times 10^3 - 1\,344\,000}{301,5}$$

$$A_{sc} = 1\,512,4 \text{ mm}^2$$

A_{sc} = Use 6Y20 bars (A_{sc} = 1 885 mm²)

3.4

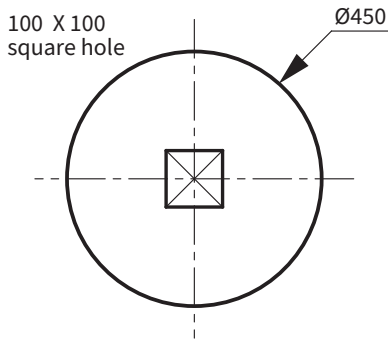


Figure 1.6

Calculate the minimum and maximum area of the main steel

Minimum area of main steel:

(Table 23)

$$\frac{100 \times A_{sc}}{A_c} \geq 0,4$$

$$\frac{100 \times 1\,512,4}{280 \times 400} \geq 0,4$$

(Cl 4.11.5.2)

1,35 > 0,4 Okay

Maximum area of main steel:

6% gross cross-sectional

$$6\% \times 280 \times 400$$

$$\text{Minimum area} = 6\,720 \text{ mm}^2$$

Summary of rectangular column:

RC Column 240 × 200 mm with 6Y20 Main bars Y8 binders at 240 mm c/c.

4.1

<p><u>Given info:</u> RC column: Load: Fcu: Fy:</p>	<p>450 mm diameter 2 200 kN 30 MPa (Table 2) 450 MPa (Table 3)</p>	
<p><u>All references taken from SANS 0100–2000</u> <u>Determine the area of the concrete</u> Net area = $\frac{\pi d^2}{4}$ – the area of the hole Net area = $\frac{\pi 450^2}{4}$ – (100 × 100) = 159 043,128 – 10 000 Net area = 149 043,13 mm²</p>		
<p><u>Calculate the suitable reinforcement</u> N = 0,4 fcu Ac + 0,67 fy Asc 2 350 × 10³ = (0,4 × 30 × 149 043,13) + (0,67 × 450 × Asc) 2 350 × 10³ = 1 788 517, 56 + 301,5 Asc Asc = $\frac{2\,350 \times 10^3 - 1\,788\,517,56}{301,5}$ Asc = 1 862,97 mm² Use 6Y20 (Asc = 1 885 mm²) Use minimum: Asc = 0,4% AC Asc = 0,4 %AC Asc = 0,4 × 282 743,3 mm² = 1 131 mm²</p>	<p>(Cl 4.7.4.3) (Table 23) (Cl 4.11.4.2.2)</p>	
<p><u>The size and spacing of the binders</u> <u>Binders:</u> ¼ of the smallest main bar ¼ × 20 = 5 mm (not available) Use: R8 helical binder. Spacing of binders: 12 × diameter of smallest main bar 12 × 20 = 240 mm Use helical binder spacing of 200 mm</p>	<p>(Cl 4.11.4.5.1)</p>	

4.2 Calculate the size of the pad foundation

$$\begin{aligned} \text{Working load} &= 2\,350 \text{ kN} + 250 \text{ kN} \\ &= 2\,600 \text{ kN} \end{aligned}$$

$$\text{Area} = \frac{\text{Force}}{\text{Pressure}}$$

$$\text{Area} = \frac{2\,600}{210} \quad \text{Area} = 3,52 \text{ m}^2$$

For the square base $\sqrt{3,52} = 2,29 \text{ m} \times 2,29 \text{ m}$

Use a base of 1,9 m \times 1,9 m

Exercise 1.8

SB page 115

1. All references taken from SANS 10100-1 (2000)

$$f_{cu} = 25 \text{ MPa}$$

$$f_y = 250 \text{ MPa}$$

Width = 1,5 m

Density of reinforced concrete

Table 2 (4.1.5.1)

Table 3 (4.1.5.2)

2 400 kg/m³

1.1 The slope formed by one step

$$\tan \varphi = \frac{165}{225}$$

$$\varphi = 36,25^\circ$$

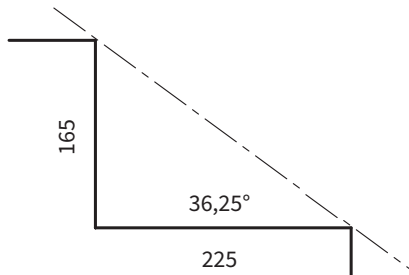


Figure 1.7

1.2 Calculate the length of the slope

$$\text{Length of slope} = \sqrt{1\,950^2 + 1\,050^2}$$

$$\text{Length of slope} = 2\,215 \text{ mm}$$

1.3	<p><u>Load calculations</u></p> <p><u>Waist:</u></p> $W = \text{Volume} \times \text{density} \times g \cdot a \times 10^{-3} \times 1,2G_n$ $W = 2,215 \times 1,2 \times 0,11 \times 2\,400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2G_n$ $W = 8,3 \text{ kN}$ <p><u>Treads or Steps:</u></p> $W = \text{Volume} \times \text{density} \times g \cdot a \times 9,81 \times 10^{-3} \times 1,2G_n$ $W = \frac{1}{2}bh \times \text{width} \times \text{density} \times g \cdot a \times 9,81 \times 10^{-3} \times 1,2G_n$ $W = \frac{1}{2} \times 0,225 \times 1,05 \times 1,2 \times 2\,400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2G_n$ $W = 4 \text{ kN}$	(Cl 4.2.2.1)	
1.4	<p><u>Design imposed load</u></p> $1,6 Q_n (3,5 \text{ kNm}^2 \times 1,95 \text{ m} \times 1,2 \text{ m}) = 13,1 \text{ kN}$	(Cl 4.2.2.1)	
1.5	<p><u>Calculate the maximum bending moment</u></p> $BM_{\max} = \frac{WL}{10}$ $BM_{\max} = \frac{(8,3 + 4 + 13,1) \times 1,95}{10}$ $BM_{\max} = 4,95 \text{ kNm}$		
2.	<p><u>All references taken from SANS 10100-1 (2000).</u></p> <p>$f_{cu} = 20 \text{ MPa}$</p> <p>$f_y = 250 \text{ MPa}$</p> <p>Width = 1,0 m</p> <p>Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1)</p> <p>Table 3 (4.1.5.2)</p> <p>2 400 kg/m³</p>	
2.1	<p><u>Calculate the length of the slope</u></p> $\text{Length of slope} = \sqrt{1\,620^2 + 900^2}$ $\text{Length of slope} = 1\,853,2 \text{ mm}$		

<p><u>Load calculations</u> Waist: $W = \text{Volume} \times \text{density} \times g \cdot a \times 10^{-3} \times 1,2Gn$ $W = 1\ 853,2 \times 1,0 \times 0,17 \times 2\ 400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2Gn$ $W = 12,1 \text{ kN}$ Treads or steps: $W = \text{Volume} \times \text{density} \times g \cdot a \times 9,81 \times 10^{-3} \times 1,2Gn$ $W = \frac{1}{2}bh \times \text{width} \times \text{density} \times g \cdot a \times 9,81 \times 10^{-3} \times 1,2Gn$ $W = \frac{1}{2} \times 0,25 \times 0,9 \times 1,0 \times 2\ 400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2Gn$ $W = 3,178 \text{ kN}$</p>	<p>(CI 4.2.2.1)</p> <p>(CI 4.2.2.1)</p>	
<p><u>Design imposed load</u> $1,6 Qn (5 \text{ kN/m}^2 \times 1,853 \text{ m} \times 1,0 \text{ m}) = 14,824 \text{ kN}$</p>	<p>(CI 4.2.2.1)</p>	
<p><u>Calculate the maximum bending moment</u> $BM_{\text{max}} = \frac{WL}{10}$ $BM_{\text{max}} = \frac{(12,1 + 3,178 + 14,824) \times 2,62}{10}$ $BM_{\text{max}} = 7,887 \text{ kNm}$</p>		

2.2

<p><u>Calculate the value for 'K'</u> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{7,887 \times 10^6}{20 \times 1\ 000 \times 145^2}$ $K = 0,018 < K1 = 0,156$ Compression reinforcement is not required.</p>	<p>(CI 4.3.3.4.1)</p> <p>Let effective depth (d) = 170 – 25 cover = 145 mm</p>	
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2.3

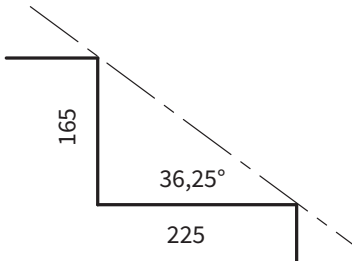
<p><u>Calculate the distance of lever arm (Z)</u> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K}{0,9}} \right\} \leq 0,95d$ $Z = 145 \left\{ 0,5 + \sqrt{0,25 - \frac{0,018}{0,9}} \right\} \leq 0,95 \times 145$ $Z = 145(0,98) \leq 0,95 \times 145$ $Z = 142 \text{ mm} > 137 \text{ mm}$ Use $Z = 137 \text{ mm}$ (least)</p>	<p>(CI 4.3.3.4.1)</p>	
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2.4

<p><u>Calculate the tension reinforcement</u></p> $A_s = \frac{BM}{0,87 f_y z}$ $A_s = \frac{7,887 \times 10^6}{0,87 \times 250 \times 137}$ $A_s = 264,69 \text{ mm}^2$ <p>Use R12 bars @ 175 c/c ($A_s = 646 \text{ mm}^2$)</p>	(Cl 4.3.3.4.1)	
<p><u>Determine the secondary reinforcement</u></p> $\frac{100 A_s}{AC} = 0,24$ $A_s = \frac{0,24 \times AC}{100}$ $A_s = \frac{0,24 \times 1000 \times 175}{100}$ $A_s = 420 \text{ mm}^2$ <p>Use R10 bars @ 175 c/c ($A_s = 449 \text{ mm}^2$)</p>	Table 23 (Cl 4.11.4.3)	
<p>$F_{cu} = 20 \text{ MPa}$ $F_y = 250 \text{ MPa}$ Width = 1,25 m Density of reinforced concrete</p>	Table 2 (4.1.5.1) Table 3 (4.1.5.2) 2 420 kg/m ³	
<p><u>Calculate the length of the slope</u></p> $\text{Length of slope} = \sqrt{3 \ 350^2 + 2 \ 200^2}$ $\text{Length of slope} = 4 \ 007,8 \text{ mm}$		
<p><u>Load calculations</u></p> <p>Waist:</p> $W = \text{Volume} \times \text{density} \times g \cdot a \times 10^{-3}$ $W = 4 \ 007,8 \times 0,12 \times 1,25 \times 2 \ 420 \text{ kg/m}^3 \times 9,81 \times 10^{-3}$ $W = 14,27 \text{ kN}$ <p>Treads or steps:</p> $W = \text{Volume} \times \text{density} \times g \cdot a \times 9,81 \times 10^{-3}$ $W = \frac{1}{2}bh \times \text{width} \times \text{density} \times g \cdot a \times 9,81 \times 10^{-3}$ $W = \frac{1}{2} \times 0,235 \times 2,2 \times 1,25 \times 2 \ 420 \text{ kg/m}^3 \times 9,81 \times 10^{-3}$ $W = 15,34 \text{ kN}$		

<p><u>Total design dead load</u> $1,2 G_n (14,27 \text{ kN} + 15,34 \text{ kN}) = 35,53 \text{ kN}$</p> <p><u>Design imposed load</u> $1,6 Q_n (11,5 \text{ kN/m}^2 \times 1,2 \text{ m} \times 3,35 \text{ m}) = 73,97 \text{ kN}$</p>		
<p><u>Calculate the maximum bending moment</u></p> $BM_{\max} = \frac{WL}{10} + \frac{WL}{10}$ $BM_{\max} = \frac{35,53 \times 3,35}{10} + \frac{73,97 \times 3,35}{10}$ $BM_{\max} = 11,9 + 24,78$ $BM_{\max} = 36,68 \text{ kNm}$		

3.	<p><u>All references taken from SANS 10100-1 (2000).</u></p> <p>$f_{cu} = 25 \text{ MPa}$</p> <p>$f_y = 250 \text{ MPa}$</p> <p>Width = 1,5 m</p> <p>Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1)</p> <p>Table 3 (4.1.5.2)</p> <p>2 400 kg/m³</p>	
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3.1	<p>The slope formed by one step</p> $\tan \phi = \frac{165}{225}$ $\phi = 37^\circ$  <p style="text-align: center;"><i>Figure 1.8</i></p>		
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3.2	<p><u>Calculate the length of the slope</u></p> $\text{Length of slope} = \sqrt{1\ 950^2 + 1\ 050^2}$ $\text{Length of slope} = 2\ 215 \text{ mm}$		
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3.3

Load calculations

Waist:

$$W = \text{Volume} \times \text{density} \times g.a \times 10^{-3} \times 1,2G_n \quad (\text{Cl 4.2.2.1})$$

$$W = 2,215 \times 1,3 \times 0,11 \times 2\,400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2G_n$$

$$W = 8,3 \text{ kN}$$

Treads or steps:

$$W = \text{Volume} \times \text{density} \times g.a \times 9,81 \times 10^{-3} \times 1,2G_n \quad (\text{Cl 4.2.2.1})$$

$$W = \frac{1}{2}bh \times \text{width} \times \text{density} \times g.a \times 9,81 \times 10^{-3} \times 1,2G_n$$

$$W = \frac{1}{2} \times 0,225 \times 1,05 \times 1,2 \times 2\,400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2G_n$$

$$W = 4 \text{ kN}$$

Design imposed load

$$1,6 Q_n (3,5 \text{ kN/m}^2 \times 1,95 \text{ m} \times 1,2 \text{ m}) = 13,1 \text{ kN} \quad (\text{Cl 4.2.2.1})$$

Calculate maximum bending moment

$$BM_{\max} = \frac{WL}{10} + \frac{WL}{10}$$

$$BM_{\max} = \frac{(8,3 + 4 + 13,1) \times 1,95}{10}$$

$$BM_{\max} = 4,95 \text{ kNm}$$

4.

All references taken from SANS 10100-1 (2000)

$$f_{cu} = 25 \text{ MPa}$$

Table 2 (4.1.5.1)

$$f_y = 250 \text{ MPa}$$

Table 3 (4.1.5.2)

$$\text{Width} = 1,35 \text{ m}$$

Density of reinforced concrete

2 425 kg/m³

4.1

Calculate the length of the slope

$$\text{Length of slope} = \sqrt{2\,250^2 + 1\,625^2}$$

$$\text{Length of slope} = 2,775 \text{ m} (2,775 \text{ m})$$

4.2 The slope formed by one step

$$\tan \varphi = \frac{160}{220}$$

$$\varphi = 37,5^\circ$$

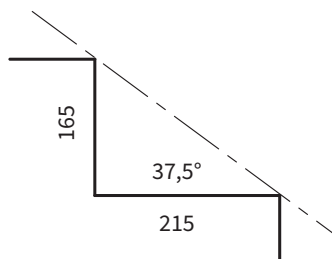


Figure 1.9

Load calculations

Waist:

$$W = \text{Volume} \times \text{density} \times g.a \times 10^{-3}$$

$$W = 2,775 \times 1,35 \times 0,12 \times 2\,425 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2\text{Gn}$$

$$W = 12,83 \text{ kN}$$

Treads or Steps:

$$W = \text{Volume} \times \text{density} \times g.a \times 9,81 \times 10^{-3}$$

$$W = \frac{1}{2}bh \times \text{width} \times \text{density} \times g.a \times 9,81 \times 10^{-3}$$

$$W = \frac{1}{2} \times 0,215 \times 1,625 \times 1,35 \times 2\,425 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2\text{Gn}$$

$$W = 6,73 \text{ kN}$$

(Cl 4.2.2.1)

(Cl 4.2.2.1)

4.3 Design imposed load

$$1,6 \text{ Qn} (10,5 \text{ kNm}^2 \times 1,35 \text{ m} \times 2,25 \text{ m}) = 51 \text{ kN}$$

(Cl 4.2.2.1)

4.4 Calculate the maximum bending moment

$$BM_{\max} = \frac{WL}{10} + \frac{WL}{10}$$

$$BM_{\max} = \frac{(12,83 + 6,73) \times 2,25}{10} + \frac{51 \times 2,25}{10}$$

$$BM_{\max} = 4,4 + 11,48$$

$$BM_{\max} = 15,88 \text{ kNm}$$

4.5

Calculate the value for 'K'

$$K = \frac{BM}{f_{cu} b d^2}$$

$$K = \frac{15,88 \times 10^6}{25 \times 1\,350 \times 90^2}$$

$$K = 0,058 < K^1 = 0,156$$

Only tension reinforcement will be required.

(Cl 4.3.3.4.1)

Let effective
depth (d) = 120
– 30 cover
= 90 mm

Calculate the distance of the lever arm (Z)

$$Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K}{0,9}} \right\} \leq 0,95d$$

$$Z = 90 \left\{ 0,5 + \sqrt{0,25 - \frac{0,058}{0,9}} \right\} \leq 0,95 \times 90$$

$$Z = 90(0,93) \leq 0,95 \times 90$$

$$Z = 83,77 \text{ mm} < 85,5 \text{ mm}$$

Use Z = 83,77 mm (least)

(Cl 4.3.3.4.1)

4.6

Calculate the tension reinforcement

$$A_s = \frac{M}{0,87 f_y z}$$

$$A_s = \frac{15,88 \times 10^6}{0,87 \times 250 \times 83,77}$$

$$A_s = 871,57 \text{ mm}^2$$

Use R12 bars @ 125 c/c (A_s = 905 mm²)

(Cl 4.3.3.4.1)

4.7

Determine the secondary reinforcement

$$\frac{100 A_s}{AC} = 0,24$$

$$A_s = \frac{0,24 \times AC}{100}$$

$$A_s = \frac{0,24 \times 1\,350 \times 120}{100}$$

$$A_s = 388 \text{ mm}^2$$

Use R8 bars @ 125 c/c (A_s = 402 mm²)

Table 23
(Cl 4.11.4.3)

2 *The bending schedule*



By the end of this module, students should be able to:

- interpret and make references to the SANS 282 summary of shape codes; and
- identify and categorise the details of a completed reinforcement bending bar schedule, with a clear understanding of the sections listed below:
 - the members (concrete staircase, concrete columns, concrete beams, concrete slabs and base foundations)
 - the bar mark
 - the type and size of reinforcement
 - the number of members
 - the number of bars in each member
 - the total number of bars
 - the length of each bar
 - the shape code
 - the columns A–E in the nearest 5-mm dimension.

The bending schedule is an itemised list of all the reinforcement required for single concrete elements. Civil engineers design the reinforcement, complete the reinforcement layout plan and section drawings as well as the bending schedule.

Exercise 2.1

SB page 137

1.	1.1	8	Number of bars
		Y	Type of steel – high-yield tensile steel bars
		12	Diameter of steel bars
		02	Bar mark
		175	Centre-to-centre spacing
		abr	Alternate bars reversed
	1.2	12	Number of bars
		R	Type of steel – mild steel bars
		08	Diameter of steel bars
		04	Bar mark
		T	Bars, place at the TOP.

2.

1	2	3	4	5	6	7	8	9	10	11	12	
Member	Reinforcement						Bending dimensions for shape codes (SANS 282)					
Mark size and no. off	Mark	Type and size	No. in each	Total no.	Length (mm)	Shape code	A	B	C	D	E or R	
Beam and Column (2 off)	01	Y20	03	6	6 550	35	6 350					
	02	Y16	02	4	6 350	20	6 350					
	03	Y16	03	6	6 550	35	3 350					
	04	Y10	17	34	1 700	60	500	300				
	05	Y16	04	8	1 300	37	1 000					
	06	R10	07	14	1 300	60	300	300				
	07	Y16	06	12	2 060	37	2 060	400				
	08	R08	09	18	1 460	60	240	240				

1	2	3	4	5	6	7	8	9	10	11	12
Member	Reinforcement					Bending dimensions for shape codes (SANS 282)					
Mark size and no. off	Mark	Type and size	No. in each	Total no.	Length (mm)	Shape code	A	B	C	D	E or R
Composite foundation beam (6 500 x 650) 2 off	01	Y 20	02	04	6 720	35	6 420				
	02	Y 20	02	04	6 720	35	6 420				
	03	Y 16	02	04	6 420	20	6 420				
	04	Y10	07	14	1 680	60	570	220			
	05	Y20	06	12	2 060	37	2 060	400			
	06	Y08	09	18	860	60	240	140			
	07	Y16	06	12	2 060	37	2 060	400			
	08	R08	09	18	1 460	60	240	240			






3.

4.1

A	Edge beam
B	Slab
C	Stairway
D	Stub column
E	Base

Any other suitable answer(s) will be accepted.

4.2

1	2	3	4	5	6	7
Mark, size and no. of	Mark	Type and size	No. of members	No. in each	Total number	Shape
Multiple members	01	Y25	01	04	04	
	02	Y20	01	04	04	
	03	Y20	01	03	03	
	04	Y16	01	05	05	
	05	R16	01	03	03	
	06	R12	01	08	08	
	07	Y16	01	05	05	

3 *Iron and steel*



By the end of this module, students should be able to:

- describe the raw materials used in the processes of producing of iron and steel by means of the following:
 - a cupula
 - an open hearth furnace
 - the Bessemer converter
 - an electric furnace;
- describe non-ferrous metals and their uses in structural work;
- determine, by means of calculation, the maximum load the connection can safely support within the thread of the shear plane using the following:
 - shearing formulae
 - shear stress
 - area
 - shear load
 - bearing formulae
 - bearing stress
 - area
 - bearing load
 - tearing formulae
 - tensile stress
 - area
 - tensile load;
- calculate the magnitude of given forces and distinguish between tension and compression on parts marked graphically or analytically;
- determine the following by means of a calculation:
 - the number of bolts required to safely secure parts to the gusset plate (the thread of the bolts will be within the shearing plane)
 - select a suitable equal-leg angle section for a part marked with a given total length;
- determine, by means of a calculation, the size and shear stress value of a bolt using the following:
 - the vertical load
 - the distance from the centroid to the furthest bolt
 - the direct load on the bolt due to an imposed load

- the total load of each bolt
 - the size of the bolt;
- determine, by means of a calculation, the maximum tensile load of a fillet-welded joint with a given leg size and a given effective length to safely support using the following:
 - the effective length
 - the throat
 - the area of weld
 - the allowable stress
 - the maximum load;
- determine, by means of a calculation, the central point load which the compound beam must safely support given the maximum bending stress and ignoring the self-weight of the beam;
- determine, by means of calculation, the maximum point load a beam can carry at midpoint, considering the self-weight of the beam given the following:
 - the effective length of the beam
 - the maximum bending stress
 - the uniformly distributed load (UDL);
- determine, by means of calculation, the maximum effective span it can support at midspan given the following:
 - the self-weight of the beam
 - the maximum bending stress;
- determine, by means of a calculation, a suitable I-parallel flange steel beam to support the given loads using the following:
 - the included self-weight of the beam
 - the maximum bending stress;
- calculate the imposed load as well as its own self-weight;
- determine the following by means of calculation:
 - the maximum load that a beam can support at a given point using a given bending stress value
 - the magnitude of the reactions RR and RL
 - the number of bolts to safely secure the steel beam to the concrete structure;
- determine, by means of a calculation, the maximum (UDL) that each of the beams will be able to carry given a bending stress value
- explain why the loads of two beams differ
- draw two neat sketches to show how beams can be joined to form one tension member; and
- determine, by means of a calculation, the maximum UDL that the structural steel can safely support.

The bending schedule is an itemised list of all the reinforcement required for single concrete elements. Civil engineers design the reinforcement, complete the reinforcement layout plan and section drawings as well as the bending schedule.

Exercise 3.1

SB page 169

- 1.1 Calculate the maximum load at 'B'

$$\text{Stress} = \frac{\text{Load}}{\text{Area}}$$

$$\text{Load} = \text{stress} \times \text{area} \times 4 \times 2$$

$$\text{Load} = 110 \frac{\text{N}}{\text{mm}^2} \times \frac{\pi 16^2}{4} \times 4 \times 2$$

$$\text{Load} = 110 \frac{\text{N}}{\text{mm}^2} \times 201,06 \times 4 \times 2$$

$$\text{Load} = 176,9 \text{ kN}$$

- 1.2 Calculate the size of the bolt at A-A

$$\text{Shear stress} = \frac{\text{Load}}{\text{Area}}$$

$$100 \frac{\text{N}}{\text{mm}^2} = \frac{46 \times 10^3}{\frac{\pi d^2}{4} \times 1 \times 2}$$

$$100 \frac{\text{N}}{\text{mm}^2} = \frac{46 \times 10^3 \times 4}{\pi d^2 \times 1 \times 2}$$

$$d = \sqrt{\frac{46 \times 10^3 \times 4}{110 \times \pi \times 1 \times 2}}$$

$$d = 16,3 \text{ mm}$$

Use a M16 or M18 bolt

- 1.3 Calculate the shear stress at 'B'

$$\text{Shear stress} = \frac{\text{Load}}{\text{Area}}$$

$$\text{Stress} = \frac{185 \times 10^3}{\frac{\pi 12^2}{4} \times 4 \times 2}$$

$$\text{Stress} = \frac{185 \times 10^3 \times 4}{\pi \times 12^2 \times 4 \times 2}$$

$$\text{Stress} = 204,5 \text{ MPa}$$

2.1 Calculate the force of the bolts in shearing

The screw thread is within the shearing plane.

Load = area × stress

$$F_s = A_s \times f_s \times n$$

$$\begin{aligned} \text{Force in shear} &= \frac{\pi (d - 0,9382 p)^2}{4} \times f_s \times n \\ &= \frac{\pi (12 - 0,9382 \times 1,75)^2}{4} \times 100 \text{ Nmm}^2 \times 6 \end{aligned}$$

$$\text{Force in shear} = 50,56 \text{ kN}$$

2.2 Calculate the force of the bolts in shearing

The screw thread is outside the shearing plane.

Load = area × stress

$$F_s = A_s \times f_s \times n$$

$$\begin{aligned} \text{Force in shear} &= \frac{\pi d^2}{4} \times f_s \times n \\ &= \frac{\pi 12^2}{4} \times 100 \text{ Nmm}^2 \times 6 \end{aligned}$$

$$\text{Force in shear} = 67,86 \text{ kN}$$

2.3 Calculate the force in tearing

Load = area × stress

$$F_t = A_t \times f_t \times n$$

$$\begin{aligned} \text{Force in tearing} &= [(B \times T) - n (d \times t)] \times f_t \\ &= [(56 \times 10) - 2(14 \times 10)] \times 155 \text{ Nmm}^2 \\ &= 560 - 280 \times 155 \text{ Nmm}^2 \end{aligned}$$

$$\text{Force in tearing} = 43,4 \text{ kN}$$

3.1 Calculate the force of the bolts in shearing

Load = area × stress

$$F_s = A_s \times f_s \times n$$

$$\begin{aligned} \text{Force in shear} &= \frac{\pi (d - 0,9382 p)^2}{4} \times f_s \times n \\ &= \frac{\pi (16 - 0,9382 \times 2)^2}{4} \times 100 \text{ Nmm}^2 \times 2 \end{aligned}$$

$$\text{Force in shear} = 156,67 \text{ kN}$$

3.2 Calculate the force in tearing

Load = area × stress

$$F_t = A_t \times f_t \times n$$

$$\begin{aligned} \text{Force in tearing} &= [(B \times T) - n(d \times t)] \times f_t \\ &= [(60 \times 6) - 2(18 \times 6)] \times 155 \text{ Nmm}^2 \\ &= 360 - 216 \times 155 \text{ Nmm}^2 \end{aligned}$$

Force in tearing = 22,32 kN

3.3 Calculate the force in bearing

$$F_b = A_t \times f_b \times n$$

$$F_b = (d \times t) \times 240 \times 2$$

$$F_b = (16 \times 6) \times 240 \times 2$$

$$F_b = 46,1 \text{ kN}$$

Exercise 3.2

SB page 179

1.1 Calculate the reactions of the roof truss

The truss is symmetrically loaded and therefore:

$$R_L = R_R = \frac{12 + 16 + 12}{2}$$

$$R_L = R_R = 20 \text{ kN}$$

$$\Sigma V_C = 0$$

$$AF \sin 30^\circ = 20 \text{ kN}$$

$$AF = \frac{20}{\sin 30^\circ}$$

$$AF = 40 \text{ kN (Strut)}$$

$$\Sigma H_C = 0$$

$$FE = AF \cos 30^\circ$$

$$FE = 40 \times \cos 30^\circ$$

$$FE = 34,64 \text{ kN (Tie)}$$

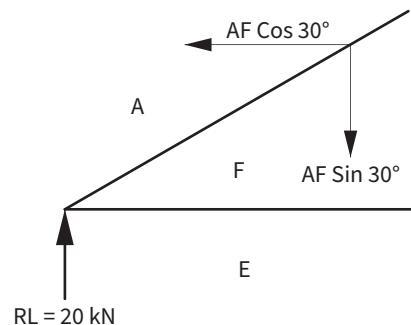


Figure 3.3: Node 1

$$VC = 0 \text{ (Force up = Forces down)}$$

$$40 \sin 30^\circ + FG \sin 30^\circ = 12 \text{ kN} + BG \sin 30^\circ$$

$$20 + 0,5 FG = 12 \times 0,5 BG$$

$$20 - 12 = 0,5 BG - 0,5 FG$$

$$8 + 0,5 FG = 0,5 BG$$

$$BG = \frac{8 + 0,5 BG}{0,5}$$

$$BG = 16 + FG$$

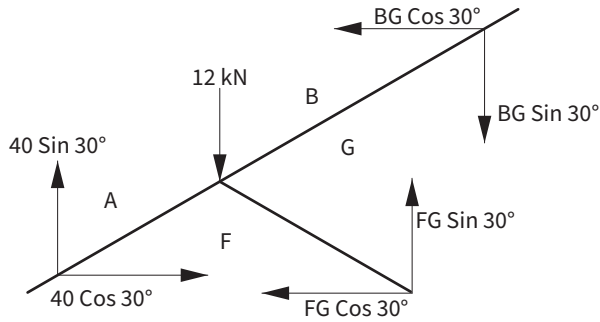


Figure 3.4: Node 2

$$\begin{aligned}
 HC &= 0 \\
 40 \cos 30^\circ &= BG \cos 30^\circ + FG \cos 30^\circ \\
 34,66 &= 0,866 BG + 0,866 FG \\
 34,66 \text{ kN} &= 0,866(16 + FG) + 0,866 FG \\
 &= 13,86 + 0,88 FG + 0,866 FG \\
 34,66 - 13,86 &= 1,732 FG \\
 FG &= \frac{20,8}{1,732} \\
 FG &= 12 \text{ kN (Strut)}
 \end{aligned}$$

And: $BG = 16 + FG$

$BG = 16 + 12$

$BG = 28 \text{ kN (strut)}$

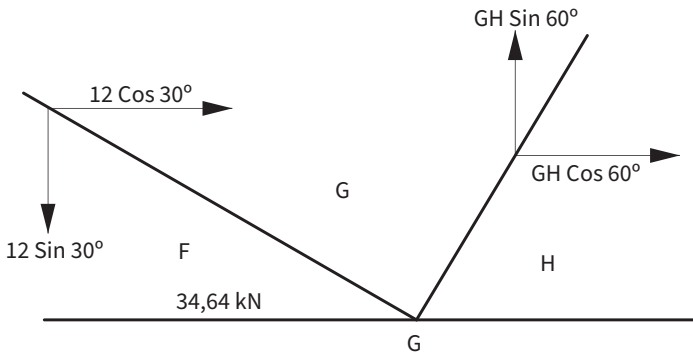


Figure 3.5: Node 3

$$\begin{aligned}
 VC &= 0 \\
 GH \sin 60^\circ &= 12 \sin 30^\circ \\
 GH &= \frac{6}{0,866} \\
 GH &= 6,93 \text{ (Tie)} \\
 HC &= 0
 \end{aligned}$$

$$34,64 \text{ kN} = EH + GH \cos 60^\circ + 12 \cos 30^\circ$$

$$34,64 = EH + 6,93 \cos 60^\circ + 10,39$$

$$HE = 134,64 - 3,465 - 10,39$$

$$HE = 20,79 \text{ kN (Tie)}$$

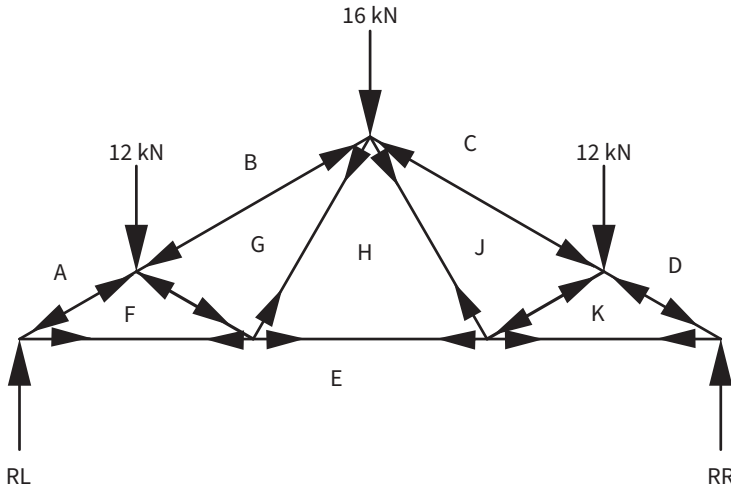


Figure 3.6:

1.2 Summary of all the forces

Member	Type	Magnitude
AF	Strut	220 kN
BG	Strut	187 kN
CJ	Strut	187 kN
DK	Strut	220 kN
FG	Tie	56,3 kN
GH	Tie	56,3 kN
HJ	Tie	56,3 kN
JK	Strut	56,3 kN
FE	Tie	190,5 kN
HE	Tie	134,2 kN
KE	Tie	190,5 kN

Exercise 3.3

1.1	<p>The welded tie Calculate the effective area</p> $A_{\text{eff}} = \frac{3A_1^2 + A_1 A_2}{3A_1 + A_2}$ <p>The tie is welded no holes required $A_1 = A_2$</p> $A_1 = t \left(b - \frac{t}{2} \right)$ $= 6 \left(50 - \frac{6}{2} \right)$ $A_1 = 282 \text{ mm}^2$ $A_2 = t \left(h - \frac{t}{2} \right)$ $= 6 \left(50 - \frac{6}{2} \right)$ $A_2 = 282 \text{ mm}^2$ <p>Therefore: $E_{\text{ff}} = \frac{3A_1^2 + 4A_1 A_2}{3A_1 + A_2}$</p> $E_{\text{ff}} = \frac{3(282^2) + 4(282)(282)}{3(282) + (282)}$ $E_{\text{ff}} = \frac{556\,668}{1\,128}$ $E_{\text{ff}} = 494 \text{ mm}^2$	(SANS 0162-CI 9.2.1)
	<p>Calculate the force Force = stress \times area</p> $= 155 \frac{\text{N}}{\text{mm}^2} \times 494 \text{ mm}^2$ <p>Force = 76 570 N = 76,57 kN</p>	Table 20
1.2	<p>The bolted tie Calculate the effective area</p> $A_{\text{eff}} = \frac{3A_1^2 + A_1 A_2}{3A_1 + A_2}$ <p>The tie is, bolted using M16 bolts.</p> $A_1 = t \left(b - \frac{t}{2} \right) - \text{area of the hole}$ $A_1 = 6 \left(50 - \frac{6}{2} \right) - (18 \times 6)$ $A_1 = 174 \text{ mm}^2$	(SANS 0162-CI 9.2.1)

<p>$A_2 = 282 \text{ mm}^2$ (we using the same as above)</p> <p>Therefore: $E_{ff} = \frac{3A_1^2 + 4A_1A_2}{3A_1 + A_2}$</p> $E_{ff} = \frac{3(174^2) + 4(174)(282)}{3(174) + (282)}$ $E_{ff} = \frac{287\,100}{804}$ $E_{ff} = 357 \text{ mm}^2$	<p>The hole is 2 mm larger than the bolt. M16 + 2 = 18 mm</p>
<p>Calculate the force</p> <p>Force = stress \times area</p> $= 155 \frac{\text{N}}{\text{mm}^2} \times 357 \text{ mm}^2$ <p>Force = 55,335 N</p> <p>= 55,3 kN</p>	<p>Table 20</p>

2.1

<p>The welded tie</p> <p>Calculate the effective area</p> $A_{\text{eff}} = \frac{3A_1^2 + A_1A_2}{3A_1 + A_2}$ <p>The tie is welded no holes required $A_1 = A_2$</p> $A_1 = t \left(b - \frac{t}{2} \right)$ $= 12 \left(90 - \frac{12}{2} \right)$ $A_1 = 1\,008 \text{ mm}^2$ $A_2 = t \left(h - \frac{t}{2} \right)$ $= 12 \left(90 - \frac{12}{2} \right)$ $A_2 = 1\,008 \text{ mm}^2$ <p>Therefore: $E_{ff} = \frac{3A_1^2 + 4A_1A_2}{3A_1 + A_2}$</p> $E_{ff} = \frac{3(1\,008^2) + 4(1\,008)(1\,008)}{3(1\,008) + (1\,008)}$ $E_{ff} = \frac{7\,112\,448}{4\,032}$ $E_{ff} = 1\,764 \text{ mm}^2$	<p>(SANS 0162-C1 9.2.1)</p>
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<p>Calculate the force this member may be subjected to</p> <p>Force = stress \times area</p> $= 155 \frac{\text{N}}{\text{mm}^2} \times 1\,764 \text{ mm}^2$ <p>Force = 273 420 N</p> <p>= 273,4 kN</p>	Table 20
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2.2

<p>The bolted tie</p> <p>Calculate the effective area</p> $A_{\text{eff}} = \frac{3A_1^2 + A_1 A_2}{3A_1 + A_2}$ <p>The tie is, bolted using M20 bolts.</p> <p>$A_1 = 12 \left(b - \frac{t}{2}\right)$ – area of the hole</p> <p>$A_1 = 12 \left(90 - \frac{12}{2}\right) - (22 \times 12)$</p> <p>$A_1 = 744 \text{ mm}^2$</p> <p>$A_2 = 950 \text{ mm}^2$ (we using the same as above)</p> <p>Therefore: $E_{\text{ff}} = \frac{3A_1^2 + 4A_1 A_2}{3A_1 + A_2}$</p> $E_{\text{ff}} = \frac{3(744^2) + 4(744)(1\,008)}{3(744) + (1\,008)}$ $E_{\text{ff}} = \frac{4\,660\,416}{3\,240}$ <p>$E_{\text{ff}} = 1\,438,4 \text{ mm}^2$</p>	<p>(SANS 0162-CI 9.2.1</p> <p>The hole is 2 mm larger than the bolt. M20 + 2 = 22</p>
<p>Calculate the force this member may be subjected to</p> <p>Force = stress \times area</p> $= 155 \frac{\text{N}}{\text{mm}^2} \times 1\,438,5 \text{ mm}^2$ <p>Force = 215, 85 N</p> <p>= 222 kN</p>	Table 20

The chosen angle is adequate, yet a $100 \times 100 \times 10$ member would also have been sufficient.

3.1

Determine a suitable strut for part marked

J (strut)

Required force = 56 kN

Actual length = 1,55 m (discontinuous)

$$L_{\text{eff}} = 1\,550 \times 0,85 = 1\,317,5 \text{ mm}$$

Select trial section: 60 × 60 × 8 mm.

$$\text{Area} = 0,903 \times 103 \text{ mm}^2$$

$$r_{\text{min}} = 11,6 \text{ mm}$$

$$L/r = \frac{1\,317,5}{11,6} = 113,6$$

$$113,6 = 65,5 \text{ MPa}$$

Therefore: Force = Stress × area

$$= 65,5 \times 0,903 \times 103 \text{ mm}^2$$

$$\text{Force} = 59,15 \text{ kN}$$

The welded strut will be able to withstand the given load of 56 kN.

(SABS 0162 Table 19)

(SABS 0162 Table 17)



Note

Hints to find the given load

Students should note that it is not as easy to select a strut as it is with a tie. In the previous calculations in the textbook, we required a suitable strut for a load of 56 kN. They can refer to to Table 17 and observe the L/r values; as this increases as the stress values decreases.

<p>Select a suitable rolled steel angle for marked Part 'G' (tie)</p> <p>Force = 65 kN</p> <p>Select trial section: 60 × 60 × 6 mm.</p> <p>Area = 0,599 × 103 mm²</p> <p>Allowable stress = 155 MPa</p> <p>Calculate effective area (A_{eff})</p> $A_{\text{eff}} = \frac{3(A_1)^2 + 4A_1A_2}{3A_1 + A_2}$ <p>A_1 = Connected leg</p> <p>$A_1 = t(b - \frac{t}{2})$ – area of hole</p> $A_1 = 6(60 - \frac{6}{2}) - (18 \times 6)$ $A_1 = 234 \text{ mm}^2$ <p>A_2 = Unconnected leg</p> $A_2 = t(b - \frac{t}{2})$ $A_2 = 6(60 - \frac{6}{2})$ $A_2 = 342 \text{ mm}^2$ <p>Calculate the effective area</p> $A_{\text{eff}} = \frac{3(234)^2 + 4(234)(342)}{3(234) + (342)}$ $A_{\text{eff}} = \frac{484\,389}{1\,044}$ $A_{\text{eff}} = 0,464 \text{ mm}^2 (0,464 \times 10^3 \text{ mm}^2)$	<p>(SABS 0162 Table 20)</p> <p>(SABS 0162 Clause 9.2.1)</p> <p>Where A_1 is the connected leg and A_2 is the unconnected leg</p>
<p>Therefore the tensile force:</p> <p>Force = $Pt \times A_{\text{eff}}$</p> $\text{Force} = 155 \text{ N/mm}^2 \times 0,464 \times 10^3 \text{ mm}^2$ <p>Force = 71,9 kN.</p> <p>The bolted tie bar will be able to withstand the given load of 65 kN.</p>	<p>(Table 20 SANS 10162)</p>

<p><u>Select a suitable rolled steel angle for marked Part 'T' (tie)</u> Required force = 65 kN Select trial section: 60 × 60 × 6 mm. Area = 0,691 × 10³ mm² Allowable stress = 155 MPa</p> <p>Calculate effective area (A_{eff}) $A_{\text{eff}} = \frac{3(A_1)^2 + 4 A_1 A_2}{3A_1 + A_2}$ $A_1 = \text{Connected leg}$ $A_1 = t(b - \frac{t}{2}) - (\text{area of hole})$ $A_1 = 6(60 - \frac{6}{2}) - (18 \times 6)$ (M16 bolts) $A_1 = 234 \text{ mm}^2$</p> <p>A_2 (unconnected leg) $A_2 = t(b - \frac{t}{2})$ $A_2 = 6(60 - \frac{6}{2})$ $A_2 = 650 \text{ mm}^2$</p> <p>$A_{\text{eff}} = \frac{3(A_1^2) + 4(430)(650)}{3(430) + (650)}$ $A_{\text{eff}} = \frac{1\ 672\ 700}{1\ 940}$ $A_{\text{eff}} = 862,2 \text{ mm}^2$ (0,8622 × 10³ mm²)</p>	<p>(SABS 0162 Table 20)</p> <p>(SABS 0162 Clause 9.2.1) Where A1 is the connected leg and A2 is the unconnected leg.</p>
<p>3.2 <u>The load:</u> Force = Pt × A_{eff} Force = 155 N/mm² × 0,8622 × 103 mm² Force = 133,6 kN The bolted tie bar will be able to withstand the given load of 128 kN</p>	<p>(Table 20 SANS 10162)</p>

3.3

Calculate the minimum length of the weld

$$\text{Force} = P \times A_{\text{eff}}$$

Calculate the throat thickness

$$= 8 \times \sin 45^\circ$$

$$= 5,66 \text{ mm}$$

$$\text{Effective length: } F = P \times A_{\text{eff}}$$

Where: $F = P \times \text{throat thickness} \times \text{length}$

$$\begin{aligned} \text{And length} &= \frac{F}{P \times \text{throat thickness}} \\ &= \frac{98 \times 10^3}{130 \times 5,66} \end{aligned}$$

$$\text{Length of weld} = 133,2 \text{ mm}$$

$$\text{Per side} = \frac{133,2}{2} = 66,6 \text{ mm}$$

(Cl 10.7.1.2)
SANS 10162)

Exercise 3.4

SB page 197

1.1

If the tie bar is welded

$$A_{\text{eff}} = \frac{3(A_1)^2 + 4 A_1 A_2}{3A_1 + A_2}$$

$$A_1 = t(b - \frac{t}{2})$$

$$A_1 = 8(80 - \frac{8}{2})$$

$$A_1 = 608 \text{ mm}^2$$

$$\text{And } A_2 = 608 \text{ mm}^2 \text{ (no holes)}$$

$$A_{\text{eff}} = \frac{3(608)^2 + 4(608)(608)}{3(608) + (608)}$$

$$A_{\text{eff}} = \frac{2\,587\,648}{2\,432}$$

$$A_{\text{eff}} = 1\,064,0 \text{ m}^2 \text{ (} 1,064 \times 10^3 \text{ mm}^2 \text{)}$$

(SABS 0162
Clause 9.2.1)
Where A_1 is the
connected leg and A_2
is the unconnected
leg.

Therefore tensile force:

$$\text{Force} = Pt \times A_{\text{eff}}$$

$$\text{Force} = 155 \text{ Nmm}^2 \times 1\,064 \text{ mm}^2$$

$$\text{Force} = 164,92 \text{ kN.}$$

The welded tie bar will be able to withstand the given load.

(Table 20
SANS 10162)

1.2

If the tie bar is bolted

$$A_{\text{eff}} = \frac{3(A_1)^2 + 4 A_1 A_2}{3A_1 + A_2}$$

$A_1 = t(b - \frac{t}{2})$ – (area of the hole)

$$A_1 = 8(80 - \frac{8}{2}) - (22 \times 10) \text{ (M20 bolts)}$$

$$A_1 = 608 - 220$$

$$A_1 = 388 \text{ mm}^2$$

$$\text{And } A_2 = 608 \text{ mm}^2$$

(SABS 0162 Clause 9.2.1)

Where A_1 is the connected leg and A_2 is the unconnected leg.

$$A_{\text{eff}} = \frac{3(388)^2 + 4(388)(608)}{3(388) + (608)}$$

$$A_{\text{eff}} = \frac{1\,395\,248}{1\,772}$$

$$A_{\text{eff}} = 787,39 \text{ mm}^2 \text{ (} 0,787 \times 10^3 \text{ mm}^2 \text{)}$$

Therefore tensile force:

$$\text{Force} = P t \times A_{\text{eff}}$$

$$\text{Force} = 155 \text{ Nmm}^2 \times 787,39 \text{ mm}^2$$

$$\text{Force} = 122,05 \text{ kN.}$$

The bolted tie bar will be able to withstand the given load.

(SABS 0162 Table 20)

1.3

Number of bolts required

$$F = P_v \times n \times A_{\text{eff}}$$

$$n = \frac{F}{P_v \times A_{\text{eff}}}$$

Where:

$$A_{\text{eff}} = \frac{(\varnothing - 0,9382P)^2}{4}$$

$$A_{\text{eff}} = \frac{(20 - 0,9382 \times 2,5)^2}{4}$$

$$A_{\text{eff}} = 244,79 \text{ mm}^2$$

$$n = \frac{120 \times 10^3}{100 \times 244,79}$$

$$n = 4,9 \text{ bolts}$$

Use 5M20 bolts to attach the tie bar to the gusset plate.

($P_v = 100 \text{ MPa}$)
(SABS 0162 Table 21)

(The screw thread is within the shearing plane.)

Exercise 3.5

1. I-Section profile parallel flange

$$356 \times 171 \times 56,7 \text{ kg/m:}$$

$$I_{xx} = 160,6 \times 10^{-6} \text{ m}^4$$

$$Y = \frac{h}{2} = \frac{358,6}{2} = 179,3 \text{ mm}$$

$$\text{Bending stress} = 160 \text{ MPa}$$

Self-weight of the channel ($356 \times 171 \times 56,7 \text{ kg/m}$)

$$\text{Weight} = 56,7 \text{ kg/m} \times 9,81 \times 10^{-3}$$

$$\text{Weight} = 0,556 \text{ kNm}$$

Bending moment at centre of the channel

$$M = \frac{I \times f}{y}$$

$$M = \frac{160,6 \times 10^6 \times 160}{179,3}$$

$$M = 143,3 \text{ kNm}$$

Calculate the maximum point load

$$\text{BM} = \frac{wl^2}{8} + \frac{WL}{4}$$

$$143,3 = \frac{0,556 \times 6^2}{8} + \frac{W \times 6}{4} \quad 143,3 = 2,5 + 1,5 W$$

$$W = \frac{143,3 - 2,5}{1,5}$$

$$W = 93,87 \text{ kN}$$

Calculate the maximum shear stress.

$$\text{Shear force maximum} = 6 (56,7 \text{ kg/m} \times 6 \text{ m} \times 9,81 \times 10^{-3}) + 93,87 \text{ divide by 2}$$

$$= 3,34 \text{ kN} + 93,78 \text{ divide by 2}$$

$$\text{Shear stress} = 48,56 \text{ kN}$$

$$\begin{aligned} \text{Shear stress} &= \frac{\text{SF max}}{d \times t_1} \\ &= \frac{48,56 \times 10^3}{358,6 \times 8} \end{aligned}$$

$$\text{Shear stress} = 17 \text{ MPa}$$

2. I-Section profile parallel flange
- $356 \times 171 \times 56,7 \text{ kg/m:}$

$$I_{xx} = 160,6 \times 10^{-6} \text{ m}^4$$

$$Y = \frac{h}{2} = \frac{358,6}{2} = 179,3 \text{ mm}$$

$$\text{Bending stress} = 160 \text{ MPa}$$

Self-weight of the channel ($356 \times 171 \times 56,7$ kg/m)

$$\text{Weight} = 56,7 \text{ kg/m} \times 9,81 \times 10^{-3}$$

$$\text{Weight} = 0,556 \text{ kNm}$$

Calculate the bending moment

$$\frac{M}{I} = \frac{f}{y}$$

$$M = \frac{I \times f}{y}$$

$$M = \frac{160,6 \times 10^6 \times 160}{179,3}$$

$$M = 143,3 \text{ kNm}$$

Equate to bending moment maximum

$$\text{BM} = \frac{wL^2}{8} + \frac{WL}{4}$$

$$143,3 = \frac{0,556 \times L^2}{8} + \frac{94 \times L}{4}$$

$$143,3 = 0,07 L^2 + 23,5 L$$

$$\text{Span (L)} = 0,07 L^2 + 23,5 L - 143$$

$$\text{Span (L)} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\text{Span (L)} = \frac{-23,5 \pm \sqrt{23,5^2 - 4 \times 0,07 \times -143,3}}{2 \times 0,7}$$

$$\text{Span (L)} = \frac{-23,5 \pm 24,33}{0,14}$$

$$\text{Span (L)} = 6 \text{ m}$$

3.1

Number of bolts required

$$F = P_v \times n \times A_{\text{eff}}$$

$$n = \frac{F}{P_v \times A_{\text{eff}}}$$

Where:

$$A_{\text{eff}} = \frac{(\emptyset - 0,9382P)^2}{4}$$

$$A_{\text{eff}} = \frac{(16 - 0,9382 \times 2)^2}{4}$$

$$A_{\text{eff}} = 156,7 \text{ mm}^2$$

$$n = \frac{143 \times 10^3}{100 \times 156,7}$$

$$n = 9,13 \text{ bolts}$$

Use 9M16 bolts to attach the tie bar to the gusset plate.

3.2

Calculate the length of the weld. The shear stress is 130 MPa.

Calculate the throat thickness:

$$T_{\text{th}} = \sin 45^\circ \times 6$$

$$= 4,24 \text{ mm}$$

Calculate effective length:

$$F = P \times A_{\text{eff}}$$

$$F = P \times \text{throat} \times L$$

$$L = \frac{143 \times 10^3}{130 \times 4,24}$$

$$L = 259,2 \text{ mm}$$

$$\text{Per side} = \frac{259,4}{2}$$

129,7 mm per side (use 130 mm)

$$P = 130 \text{ MPa}$$

$$(10.7.1.2)$$

Exercise 3.6

SB page 221

1.1

I-section profile parallel flange

(406 × 140 × 38,6 kg/m)

$$I_{xx} = 124,1 \times 10^{-6} \text{ m}^4$$

$$Y = \frac{h}{2} = \frac{397,3}{2} = 198,65 \text{ mm}$$

Bending stress = 156 MPa

Self-weight of the beam (406 × 140 × 38,6 kg/m)

Weight = 38,6 kg/m × 9,81 × 10⁻³

Weight = 0,379 kN/m

Bending moment at the centre of the channel

$$M = \frac{I \times f}{y}$$

$$M = \frac{124,1 \times 10^6 \times 156}{198,65}$$

M = 97,46 kNm

Calculate the maximum distributed load

$$= \frac{wl^2}{8} + \frac{wl^2}{8}$$

$$97,46 = \frac{0,379 \times 7,6^2}{8} + \frac{w \times 7,6^2}{8}$$

$$97,46 = 2,74 + 7,22 W$$

$$W = \frac{97,46 - 2,74}{7,22}$$

$$W = 13,12 \text{ kN/m}$$

1.2

Calculate the maximum shear stress

$$\begin{aligned} \text{Shear maximum force} &= (0,379 \text{ kN/m} \times 7,6 \text{ m} \times 9,81 \times 10^{-3}) \\ &\quad + (13,12 \text{ kN/m} \times 7,6 \text{ m}) \\ &= 0,028 \text{ kN} + 99,7 \text{ kN} \\ &= \frac{99,74}{2} \end{aligned}$$

$$\text{Shear stress} = 49,87 \text{ kN}$$

$$\begin{aligned} \text{Shear stress} &= \frac{\text{SF maximum}}{d \times t_1} \\ &= \frac{49,87 \times 10^3}{397,3 \times 6,3} \end{aligned}$$

$$\text{Shear stress} = 19,92 \text{ MPa}$$

2. I-Section profile parallel flange $356 \times 171 \times 56,7 \text{ kg/m}$:

$$I_{xx} = 160,6 \times 10^{-6} \text{ m}^4$$

$$Y = \frac{h}{2} = \frac{358,6}{2} = 179,3 \text{ mm}$$

$$\text{Bending stress} = 160 \text{ MPa}$$

Self-weight of the channel ($356 \times 171 \times 56,7 \text{ kg/m}$)

$$\text{Weight} = 56,7 \text{ kg/m} \times 9,81 \times 10^{-3}$$

$$\text{Weight} = 0,556 \text{ kNm}$$

Calculate the bending moment

$$\frac{M}{I} = \frac{f}{y}$$

$$M = \frac{I \times f}{y}$$

$$M = \frac{160,6 \times 10^6 \times 160}{179,3}$$

$$M = 143,3 \text{ kNm}$$

Equate to the maximum bending moment

$$BM = \frac{wl^2}{8} + \frac{WL}{4}$$

$$143,3 = \frac{0,556 \times L^2}{8} + \frac{94 \times L}{4}$$

$$143,3 = 0,07 L^2 + 23,5 L$$

$$\text{Span (L)} = 0,07 L^2 + 23,5 L - 143$$

$$\text{Span (L)} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\text{Span (L)} = \frac{-23,5 \pm \sqrt{23,5^2 - 4 \times 0,07 \times -143,3}}{2 \times 0,07}$$

$$\text{Span (L)} = \frac{-23,5 \pm 24,33}{0,14}$$

$$\text{Span(L)} = 6 \text{ metres}$$

Exercise 3.7

SB page 246

1. Self-weight of the channel section ($160 \times 65 \times 18,8 \text{ kg/m}$)

$$\text{Weight} = 18,8 \text{ kg/m} \times 9,81 \times 10^{-3}$$

$$\text{Weight} = 0,184 \text{ kN/m}$$

Bending moment at the centre of the taper flange beam

$$\frac{M}{I} = \frac{f}{y} \text{ Where:}$$

$$M = \frac{I \times f}{y}$$

$$M = \frac{9,247 \times 10^6 \times 145}{80}$$

$$M = 16,76 \text{ kNm}$$

$$I_{xx} = 9,247 \times 10^{-6} \text{ m}^4$$

$$Y = \frac{h}{2} = \frac{160}{2}$$

$$= 80 \text{ mm}$$

Calculate the maximum UDL

$$BM = \frac{wl^2}{8} + \frac{wl^2}{8}$$

$$16,76 = \frac{0,184 \times 5^2}{8} + \frac{w \times 5^2}{8}$$

$$16,76 = 0,575 + 3,125 w$$

$$3,125 w = 16,76 - 0,575$$

$$w = \frac{16,76 - 0,575}{3,125}$$

$$w = 5,179 \text{ kN/m}$$

2. Given information:

<p>I-Section 305 × 165 × 46,1 kg/m: $I_{xx} = 99,35 \times 10^{-6} \text{ m}^4$ Area = $5,878 \times 10^{-3} \text{ m}^2$ $\frac{h}{2} = \frac{307,1}{2} = 153,55 \text{ mm}$</p>	<p>Plate: 166 mm × 12 mm $I_{xx} = \frac{BD^3}{12} = \frac{0,166 \times 0,012^3}{12}$ $= 0,024 \times 10^{-6} \text{ m}^4$ Area = $0,166 \times 0,012$ $= 1,922 \times 10^{-3} \text{ m}^2$</p>
<p>Total area = $5,878 \times 10^{-3} \text{ m}^2 + 1,922 \times 10^{-3} \text{ m}^2$ Total area = $7,87 \times 10^{-3} \text{ m}^2$</p>	

Calculate the neutral axis using area moments from the bottom

$$7,87 \times 10^{-3} \text{ m}^2 \times Y_1$$

$$= (5,878 \times 10^{-3} \text{ m}^2 \times 0,16555) + (1,922 \times 10^{-3} \text{ m}^2 \times 0,006)$$

$$Y_1 = \frac{0,973 \times 10^{-3} \text{ m}^2 + 0,0115 \times 10^{-3} \text{ m}^2}{7,87 \times 10^{-3} \text{ m}^2}$$

$$Y_1 = \frac{0,985 \times 10^{-3} \text{ m}^2}{7,87 \times 10^{-3} \text{ m}^2}$$

$$Y_1 = 0,125 \text{ m}$$

$$Y_1 = 125 \text{ mm}$$

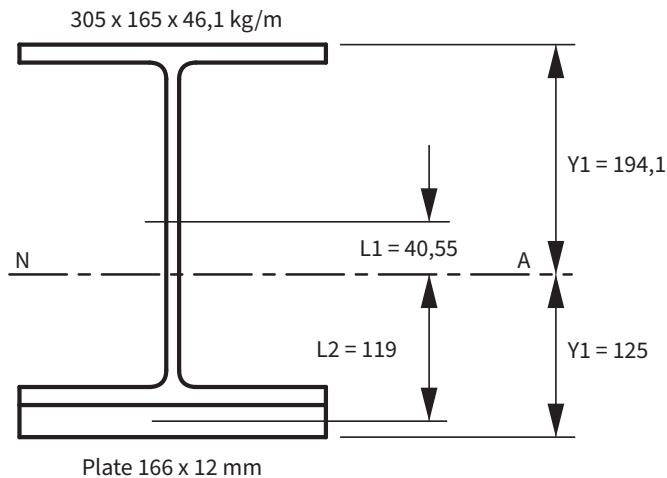


Figure 3.7

Calculate the second moment of area

$$I_{xx \text{ total}} = (I_{xx \text{ beam}} + al^2) + (I_{xx \text{ plate}} + al^2)$$

$$I_{xx \text{ Beam}} = (99,35 \times 10^{-6} + 5,878 \times 10^{-3} \times 0,04055^2)$$

$$= (99,35 \times 10^{-6} + 9,67 \times 10^{-6}) = 109,02 \times 10^{-6} \text{ m}^4$$

$$I_{xx \text{ Plate}} = (0,024 \times 10^{-6} + 1,992 \times 10^{-3} \times 0,119^2)$$

$$(0,024 \times 10^{-6} + 28,21 \times 10^{-6}) = 28,23 \times 10^{-6} \text{ m}^4$$

$$I_{xx \text{ total}} = 137,25 \times 10^{-6} \text{ m}^4$$

Calculate the maximum bending moment

$$\frac{M}{I} = \frac{f}{y} \text{ where } M = \frac{I \times f}{y}$$

$$BM_{\text{max}} = \frac{137,25 \times 10^6 \times 151}{125}$$

$$BM_{\text{max}} = 165,798 \text{ kNm}$$

Calculate the central point load

The self-weight of the compound beam limited to 1,5 kNm.

$$BM = \frac{Wl^2}{8} + \frac{Wl}{4}$$

$$165,798 = \frac{1,5 \times 6,75^2}{8} + \frac{W \times 6,75}{4}$$

$$165,798 = 8,54 + 1,69W$$

$$W = \frac{165,798 - 8,54}{1,69}$$

$$W = 93,05 \text{ kN}$$

3. Given information

<p><u>200 × 75 × 25,3 kg/m channel:</u></p> $I_{yy} = 1,478 \times 10^{-6} \text{ m}^4$ $\text{Area} = 3,218 \times 10^{-3} \text{ m}^2$ $A_y = 20,1 \text{ m}$	<p><u>365 × 171 × 56,7 kg/m I-parallel flange:</u></p> $I_{xx} = 160,6 \times 10^{-6} \text{ m}^4$ $\text{Area} = 7,225 \times 10^{-3} \text{ m}^2$ $\frac{h}{2} = \frac{358,6}{2} = 179,3 \text{ mm}$
<p>Plate: 205 mm × 16 mm</p> $I_{xx} = \frac{bd^3}{12} = \frac{0,205 \times 0,016^3}{12} = 0,06997 \times 10^{-6} \text{ m}^4$ $\text{Area} = 0,205 \times 0,016 = 3,28 \times 10^{-3} \text{ m}^2$	

$$\text{Total area} = 3,218 \times 10^{-3} \text{ m}^2 + 7,225 \times 10^{-3} \text{ m}^2 + 3,28 \times 10^{-3} \text{ m}^2$$

$$\text{Total area} = 13,723 \times 10^{-3} \text{ m}^2$$

Calculate the neutral axis using area moments from the bottom

$$13,723 \times 10^{-3} \text{ m}^2 \times Y_1 = (3,218 \times 10^{-3} \text{ m}^2 \times 0,0549)$$

$$+ (7,225 \times 10^{-3} \text{ m}^2 \times 0,2543)$$

$$+ (3,28 \times 10^{-3} \text{ m}^2 \times 0,4416)$$

$$Y_1 = \frac{0,17667 \times 10^{-3} \text{ m}^2 + 1,837 \text{ m}^2 \times 10^{-3} + 1,448 \times 10^{-3} \text{ m}^2}{13,723 \times 10^{-3} \text{ m}^2}$$

$$Y_1 = \frac{3,462 \times 10^{-3} \text{ m}^2}{13,723 \times 10^{-3} \text{ m}^2}$$

$$Y_1 = 0,25229 \text{ m}$$

$$Y_1 = 252,29 \text{ mm}$$

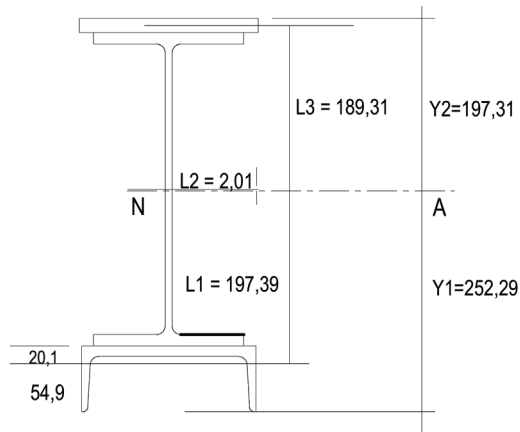


Figure 3.8

The L-distances: $L_1 = 252,29 - 54,9 = 197,39 \text{ mm}$

$$L_2 = 252,29 - 75 - 358,6/2 (179,31) = - 2,01 \text{ mm}$$

$$L_2 = 197,31 - 16 - 358,6/2 (179,31) = 2,01 \text{ mm}$$

$$L_3 = 197,31 - 16/2 (8) = 189,31 \text{ mm}$$

Calculate the second moment of area (I_{xx} total)

$$I_{xx \text{ tot}} = (I_{yy \text{ Channel}} + a^2) + (I_{xx \text{ Beam}} + a^2) + (I_{xx \text{ Plate}} + a^2)$$

$$I_{yy \text{ Channel}} = (1,478 \times 10^{-6} + 3,218 \times 10^{-3} \times 0,19739^2) \\ = (1,478 \times 10^{-6} + 0,1254 \times 10^{-6}) = 1,6 \times 10^{-6} \text{ m}^4$$

$$I_{xx \text{ Beam}} = (160,6 \times 10^{-6} + 7,225 \times 10^{-3} \times 2,01^2) \\ = (160,6 \times 10^{-6} + 29,19 \times 10^{-6}) = 189,79 \times 10^{-6} \text{ m}^4$$

$$I_{xx \text{ Plate}} = (0,06997 \times 10^{-6} + 3,28 \times 10^{-3} \times 0,18931^2) \\ = (0,06997 \times 10^{-6} + 0,118 \times 10^{-6}) = 0,1875 \times 10^{-6} \text{ m}^4$$

$$I_{xx \text{ total}} = 191,578 \times 10^{-6} \text{ m}^4$$

Calculate the maximum bending moment (Bending stress = 145 MPa)

$$\frac{M}{I} = \frac{f}{y} \text{ where } M = \frac{I \times f}{y} \\ BM_{\max} = \frac{191,578 \times 10^6 \times 145}{252,29}$$

$$BM_{\max} = 110,11 \text{ kNm}$$

Calculate the self-weight of the compound steel beam

$$\text{Channel: } 25,3 \times 9,81 \times 10^{-3} = 0,248 \text{ kN/m}$$

$$\text{I-beam: } 56,7 \text{ kg/m} \times 9,81 \times 10^{-3} = 0,556 \text{ kN/m}$$

$$\text{Plate: } 0,205 \times 0,016 \times 1 \times 1786 \text{ kg/m}^3 \times 9,81 \times 10^{-3} = 0,0575 \text{ kN/m}$$

$$\text{Self-weight} = 0,862 \text{ kN/m}$$

Calculate the UDL

Include the self-weight of the beam with an additional load of 3 kN/m.

$$BM = \frac{W l^2}{8} + \frac{W l^2}{8} + \frac{W l^2}{8} \\ 110,11 = \frac{0,862 \times 9,5^2}{8} + \frac{3 \times 9,5^2}{8} + \frac{W \times 9,5^2}{8}$$

$$110,11 = 9,72 + 33,84 + 11,28 W$$

$$W = \frac{110,11 - 43,56}{11,28}$$

$$W = 5,9 \text{ kN/m}^2$$

Exercise 3.8

SB page 261

<p>Calculate the effective height of the column Effective height (l) = $1,0L$ Where: $L_{\text{effective}} = 1,0 \times 3,25 \text{ m}$ $= 3,25 \text{ m (3 250 mm)}$</p>	<p>SABS 0162-1984 Table 19</p>
--	---

Calculate the effective cross-sectional area of the column

$$A_c = \frac{\pi d^2}{4} - \frac{\pi d^2}{4}$$

$$A_c = \frac{\pi 76,2^2}{4} - \frac{\pi 71,2^2}{4}$$

$$\text{Area} = 4\,560,4 - 3\,981,5 \text{ mm}^2$$

$$\text{Cross-sectional area} = 578,9 \text{ mm}^2$$

Calculate the second moment of area about the x - x axis.

$$I_{xx} = I_{yy} = \frac{\pi D^4}{64} - \frac{\pi d^4}{64}$$

$$I_{xx} = I_{yy} = \frac{\pi 76,2^4}{64} - \frac{\pi 71,2^4}{64}$$

$$I_{xx} = I_{yy} = 1\,654\,968,7 \text{ mm}^4 - 1\,261\,507,6 \text{ mm}^4$$

$$I_{xx} = I_{yy} = 393\,461,1 \text{ mm}^4$$

Calculate the radius of gyration.

$$r = \sqrt{\frac{I}{\text{Area}}}$$

$$r = \sqrt{\frac{393\,461,1}{578,9}}$$

$$r = 26,1 \text{ mm}$$

<p>Calculate the slenderness ratio $L/r = \frac{3\,250}{26,1} = 124,5$ $124,5 = 56 \text{ MPa}$</p>	<p>From Table 17 (SANS 0162)</p>
---	---

Calculate the maximum load

$$\text{Load} = \text{Stress} \times \text{Area}$$

$$\text{Load} = 56 \text{ Nmm}^2 \times 578,9 \text{ mm}^2$$

$$\text{Load} = 32,4 \text{ kN}$$

Exercise 3.9

1. Calculate the direct shear on each bolt.

$$\text{Force direct} = \frac{\text{Force}}{\text{No of bolts}}$$

$$F_{\text{direct}} = \frac{16 \text{ kN}}{2} = 8 \text{ kN}$$

Calculate the distance from the centroid to the furthest bolt.

$$r = \frac{180}{2} = 90 \text{ mm}$$

The direct load on the bolts due to the imposed load

$$\Sigma cwm = \Sigma acwm$$

$$(16 \times 190) = (F_T \times 90 \times 2)$$

$$F_T = \frac{16 \times 190}{90 \times 2}$$

$$F_T = 16,9 \text{ kN}$$

The resultant load on each bolt

$$F_R = 16,9 + 8 = 24,9 \text{ kN}$$

Calculate the size of the bolts. (Shear stress = 100 MPa)

$$F_R = \text{Shear stress} \times \text{Area of bolt}$$

$$\frac{\pi d^2}{4} = \frac{Fr}{\text{Shear stress}}$$

$$d = \sqrt{\frac{Fr \times 4}{\pi \times \text{stress}}}$$

$$d = \sqrt{\frac{24,9 \times 10^3 \times 4}{\pi \times 100}}$$

$$d = 17,8 \text{ mm}$$

Use 2M20 bolts

2. Calculate the direct shear on each bolt.

$$\text{Force direct} = \frac{\text{Force}}{\text{No of bolts}}$$

$$F_{\text{direct}} = \frac{45 \text{ kN}}{4} = 11,25 \text{ kN}$$

Distance from the centroid to the furthest bolt.

$$r = \sqrt{160^2 + 105^2}$$

$$r = 191,4 \text{ mm}$$

The direct load on the bolts due to the imposed load

$$\Sigma cwm = \Sigma acw$$

$$(45 \times 450) = (F_T \times 191,4 \times 4)$$

$$20\,250 = 765,6 F_T$$

$$F_T = \frac{20\,250}{765,6}$$

$$F_T = 26,4 \text{ kN}$$

$$\tan \theta = \frac{160}{105}$$

$$\theta = 56,73^\circ$$

$$F_{T \text{ hor.}} = F_T \times \cos \theta$$

$$= 26,4 \times \cos 56,73^\circ$$

$$F_{T \text{ hor.}} = 14,48 \text{ kN}$$

$$F_{T \text{ vert.}} = F_T \times \sin \theta$$

$$= 26,4 \times \sin 56,73^\circ$$

$$F_{T \text{ vert.}} = 22,07 \text{ kN}$$

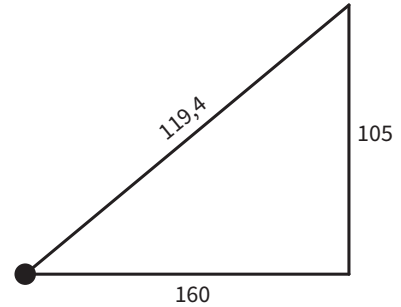


Figure 3.9

Resultant force

$$F_R = \sqrt{14,48^2 + (22,07 + 11,25)^2}$$

$$F_R = 36,33 \text{ kN}$$

Calculate the size of the bolts.

$$F_R = \text{Shear stress} \times \text{Area of bolt}$$

$$\frac{\pi d^2}{4} = \frac{F_r}{\text{Shear stress}}$$

$$d = \sqrt{\frac{F_r \times 4}{\pi \times \text{stress}}}$$

$$d = \sqrt{\frac{36,33 \times 10^3 \times 4}{\pi \times 115}}$$

$$d = 20 \text{ mm}$$

Use 4M20 bolts

- Distance l_a from the centroid to the furthest bolt.

$$l_a = \sqrt{100^2 + 75^2}$$

$$l_a = 125 \text{ mm}$$

Calculate Σl^2

$$\Sigma l^2 = n \times l_a^2$$

$$= 4 \times (125)^2$$

$$\Sigma l^2 = 62\,500 \text{ mm}^2$$

Calculate shearing force due to each bolt

$$\text{Force direct} = \frac{\text{Force}}{\text{No of bolts}}$$

$$F_{\text{direct}} = \frac{25 \text{ kN}}{4} = 6,25 \text{ kN}$$

The direct load on the bolts due to the imposed load

$$\Sigma cwm = \Sigma acwm$$

$$(25 \times 450) = (F_T \times 125,8 \times 4) \quad (4 = \text{No of bolts})$$

$$11\,250 = 500 F_T$$

$$F_T = \frac{11\,250}{500}$$

$$F_T = 22,5 \text{ kN}$$

<p>Force on any bolt</p> $X = \frac{\Sigma la}{n \times e}$ $X = \frac{62\,500}{4 \times 450}$ $X = 34,72 \text{ mm}^2$	<p>X = The distance between the centroid and the point through which the resultant force acts.</p>
---	--

Load on any bolt

$$= \frac{f \times e}{\Sigma la^2}$$

$$= \frac{25 \times 10^3 \times 450}{62\,500}$$

Load on any bolt = 180 kN

Load on bolts A & B

$$180 = \sqrt{(100^2 + (75 + 34,72)^2)}$$

$$= 26,721 \text{ kN}$$

Load on bolts C & D

$$180 = \sqrt{(100^2 + (75 - 34,72)^2)}$$

$$= 19,4 \text{ kN}$$

4. Determine ΣI^2 about the edge at 'x'

$$\begin{aligned}\Sigma I_a &= N(I^{21} + I^{22} + I^{23} \dots) \\ &= 2(36^2 + 106^2 + 176^2 + 246^2 + 316^2) \\ \Sigma I_a &= 407\,706 \text{ mm}^2\end{aligned}$$

Determine the tensile load due to the moment about 'X'

$$\begin{aligned}\text{Ft moment} &= \frac{P \times e \times I_a}{\Sigma I_a} \\ &= \frac{170 \times 10^3 \times 200 \times 316}{407\,760}\end{aligned}$$

$$\text{Ft moment} = 26,35 \text{ kN}$$

Load Fs due to direct shear

$$\text{Force direct} = \frac{\text{Force}}{\text{No of bolts}}$$

$$F_{\text{direct}} = \frac{170 \text{ kN}}{10} = 17 \text{ kN}$$

Area of the bolt

$$\begin{aligned}\text{Effective area} &= \frac{\pi d^2}{4} \\ &= \frac{\pi 24^2}{4}\end{aligned}$$

$$\text{Effective area} = 352,4 \text{ mm}^2$$

<p>Tensile stress area</p> $\begin{aligned}\text{Effective area} &= \frac{\pi}{4} (d - 0,9382 P)^2 \\ &= \frac{\pi}{4} (24 - 0,9382 \times 3)^2\end{aligned}$ <p>Effective area = 352,5 mm²</p>	<p>SANS 0162 Cl 10.5.1</p>
--	--------------------------------

<p>Check actual stress</p> $\begin{aligned}\text{Tensile stress } F_t &= \frac{Ft}{A_t} \\ &= \frac{26,35 \times 10^3}{352,5} \\ F_t &= 74,75 \text{ MPa} < 145 \text{ MPa}\end{aligned}$	<p>SANS 0162 Table 21</p>
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Shear stress

$$F_s = \frac{F_s}{A_s}$$

$$F_s = \frac{17 \times 10^3}{452,39}$$

$$F_s = 37,6 \text{ MPa} < 100 \text{ MPa}$$

Check combined stresses

$$\frac{F_s}{P_s} + \frac{F_t}{P_t} = 1,4$$

$$\frac{37,58}{100} + \frac{91,92}{145} = 1,4 = \text{Sufficient.}$$

The chosen M24 bolts are satisfactory.

SANS 0162
Cl 10.5.1



Exemplar examination paper 1

The following is an example of a final question paper.

Candidates are always reminded to carefully read the instructions before answering the questions.

Duration: 4 hours

Mark allocation: 100 marks

Instructions and information:

1. Answer ALL the questions. You may start with any question.
2. Number the answers according to the numbering system laid out in the question paper.
3. Start each question on a new page.
4. Draw a line across the page at the end of each answer.
6. All calculations must conform to the relevant SABS / SANS Codes of Practice.
7. All the applicable codes and reference clause numbers must be indicated.
8. Complement your answers with neat sketches.
9. Use the applicable required schedules at the back of your textbook.

REQUIREMENTS: BOE 8/6 Hot-rolled structural steel sections (red book)

OPEN-BOOK EXAMINATION

Candidates may use their own personal notes and textbooks. No past question papers and marking guidelines will be allowed in the examination centre.

QUESTION 1

Figure 1 shows a compound steel beam with TWO steel plates attached to the flanges of a $356 \times 171 \times 56,7$ kg/m H-section parallel flange steel beam with a channel section to form a compound beam. The span of the beam is 6,75 m.

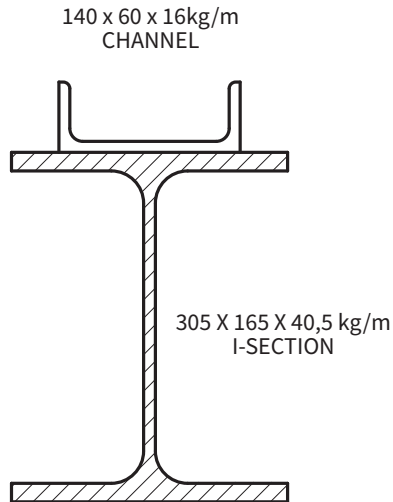


Figure 1

The steel beam must support an additional point load of 25 kN.

Include the self-weight of the compound beam and calculate the maximum uniformly distributed load that the compound beam can safely support.

Use a bending stress of 156 MPa and note that the density of structural steel is $7\,860 \text{ kg/m}^3$.

[20]

QUESTION 2

Figure 2 shows part of a one-directional, simply supported reinforced concrete slab with an effective span of 4,80 m. The slab will be cast over TWO 270-mm wide brick walls.

Use Grade 25 concrete with a density of $2\,430 \text{ kg/m}^3$ then calculate the maximum uniformly distributed imposed load the slab must support.

The self-weight of the concrete slab must be included in the calculations.

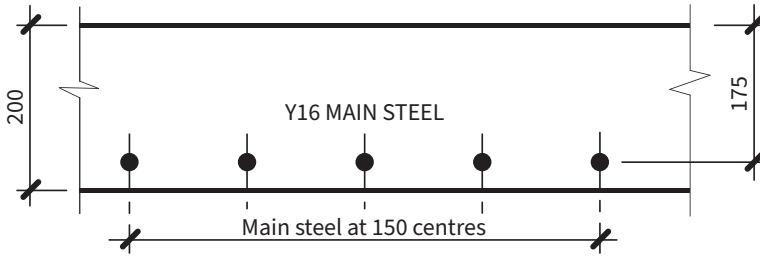


Figure 2

[12]

QUESTION 3

3.1 Figure 3 shows a rectangular reinforced concrete column. The column is reinforced with 4Y20 and 2Y16 main bars. The characteristic strength of the concrete is limited to 30 MPa.

Calculate the following:

- 3.1.1 The nett area of the concrete
- 3.1.2 The axial load the column can withstand
- 3.1.3 The required diameter and spacing of the binders.

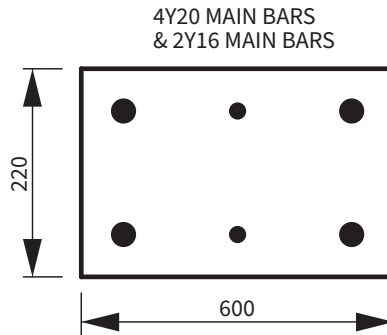


Figure 3

(9)

3.2 Calculate the minimum area of a square isolated pad foundation for the RC column mentioned in Question 3.1. The column must also resist the following loads:

Imposed load: 600 kN

Mass of foundation concrete: 85 kN

Use a safe bearing upward soil pressure of 220 kNm².

(5)

[14]

QUESTION 4

- 4.1 Calculate the amount of cement required for a concrete mix with a water: cement ratio of 0,35 and 46 litres of water. (3)
- 4.2 Explain the characteristics of non-ferrous metals. (2)
- 4.3 State the difference between brass and bronze. (2)
- [7]

QUESTION 5

A simply supported reinforced concrete beam has an effective span of 5,35 m. The beam is 230 mm wide and must support the following loads:

- (a) A 12-kN point load in the centre of the beam
- (b) A uniformly distributed load of 7 kNm.

The beam will be made up by using Grade 25 MPa concrete and mild steel reinforcement. The density of the concrete must be taken as 2 400 kg/m³. The self-weight of the reinforced concrete beam must be taken into consideration.

Answer the following:

- 5.1 The effective depth of the reinforced concrete beam (3)
- 5.2 Determine the suitable tension reinforcement for the reinforced concrete beam (14)
- 5.3 Check for the minimum required main reinforcement. (1)
- [18]

QUESTION 6

- 6.1 A 356 × 171 × 44,8 kg/m I-section steel column is used in a warehouse as part of the structure. The actual height of the column is 4,750 m. The column will, however, be effectively held in position at both ends, but not restrained against rotation. Calculate the maximum load that the column will be able to support. All the reference codes must be clearly indicated. (7)
- 6.2 State the degree of restraint of a compression member where the effective length is given as 0,70 L. State the code and reference. Also include a neat sketch to show the fixing symbol. (4)
- [11]

QUESTION 7

Figure 4 shows TWO methods of using a 203 × 133 × 25,3 kg/m I-section parallel flange as a tension member to span a distance of 5,55 m.

- 7.1 Calculate the maximum uniformly distributed load (UDL) that each of the beams will be able to carry. Use a bending stress of 165 MPa. (10)
- 7.2 Explain why the loads of the two beams differ. (2)

7.3 Draw TWO neat drawings to show how the beams can be joined to form ONE compression member. (4)

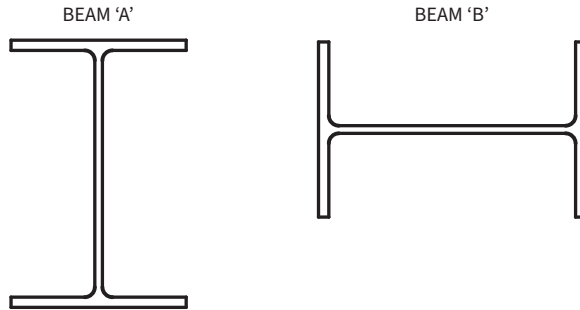


Figure 4

[16]

Total: 100 marks



Exemplar examination paper 2

The following is an example of a final question paper.

Candidates are always reminded to carefully read the instructions before answering the questions.

Duration: 4 hours

Mark allocation: 100 marks

Instructions and information:

1. Answer ALL the questions. You may start with any question.
2. Number the answers according to the numbering system laid out in the question paper.
3. Start each question on a new page.
4. Draw a line across the page at the end of each answer.
6. All calculations must conform to the relevant SABS / SANS Codes of Practice.
7. All the applicable codes and reference clause numbers must be indicated.
8. Complement your answers with neat sketches.
9. Use the applicable required schedules at the back of your textbook.

REQUIREMENTS: BOE 8/6 Hot-rolled structural steel sections (red book)

OPEN-BOOK EXAMINATION

Candidates may use their own personal notes and textbooks. No past question papers and marking guidelines will be allowed in the examination centre.

QUESTION 1

A short, axially loaded reinforced round concrete column with a diameter of 850 mm has to support an ultimate load of 7 500 kN. Use Grade 30 concrete with high-yield tensile steel main reinforcement and a mild steel binder.

Calculate the following:

- 1.1 The required number and diameter of the longitudinal bars (4)
 - 1.2 The maximum and minimum percentage of the steel reinforcement (2)
 - 1.3 The diameter and pitch of the helical binder (4)
 - 1.4 Draw TWO neat drawings to show the cross-sectional view and longitudinal vertical section of the column. Clearly show the positions of the main steel and THREE binders. (5)
- [15]**

QUESTION 2

Figure 1 shows the front view of a loaded steel roof truss.

Ignore the self-weight of the roof truss but calculate the following:

- 2.1 The upward forces of the reactions RR and RL (4)
 - 2.2 The magnitude of the forces in parts 'AB', 'CD' and 'BD' (9)
 - 2.3 Distinguish between tension and compression forces in the members. (5)
- (No marks will be awarded for the graphical solutions.)

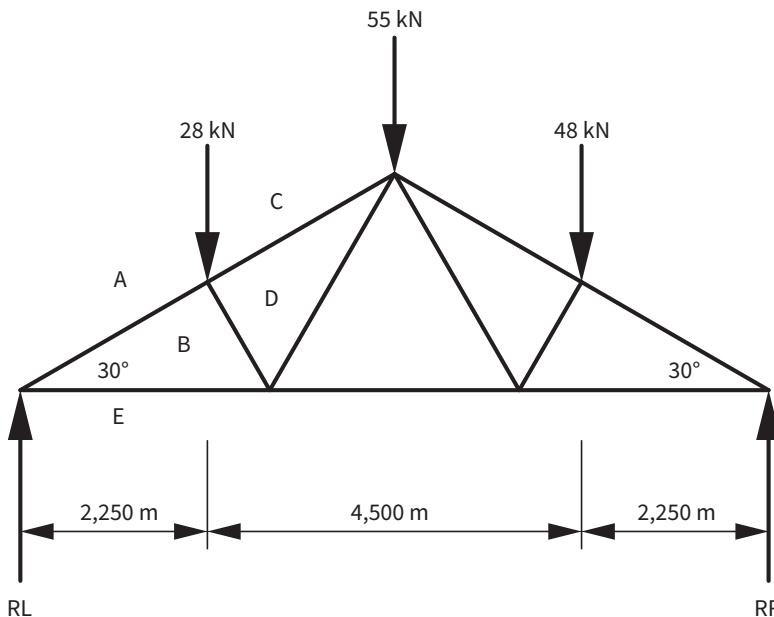


Figure 1

[18]

QUESTION 3

A simply supported reinforced concrete beam is cast over a wide opening for a roll-up metal garage door. The effective span for the opening is 9 m.

The beam supports the following loads:

- (a) TWO uniformly distributed live loads of 4,475 kNm and 12,8 kNm.
- (b) An 88-kN point load 3,5 m from the right-end support.

Use the following specifications:

- Grade 25 MPa concrete
- High yield tensile reinforcement

Calculate the following:

- 3.1. The reactions RL and RR of the beam (4)
- 3.2. Draw a neat sketch of the shear force diagram. (2)
- 3.3. Calculate and draw a neat sketch of the bending moment diagram. (4)
- 3.4 Calculate the value of 'K' to determine if compression reinforcement is required.

DO NOT insert any reinforcement. Ignore the self-weight of the reinforced concrete beam. (3)

[13]

QUESTION 4

A simply supported I-section steel beam supports a load of 65 kNm over an effective span of 6,35 m. The bending stress is 156 MPa.

Calculate the following:

- 4.1 Select a suitable parallel flange steel beam to support the given load. (5)
 - 4.2 Add the mass of the chosen beam to the downward load and then check if the chosen steel beam is adequate to support the load as well as its own weight. (7)
- [12]**

QUESTION 5

A double reinforced concrete beam must be cast as a simply supported beam over a wide panoramic sliding door and window.

The following specifications are given to design the RC beam:

Width of beam: 330 mm
 Effective span: 8 m
 f_{cu} : 25 MPa
 f_y : 450 MPa
 Density of concrete: 2 425 kg/m³

- 5.1 Calculate the following:
- 5.2 The effective depth of the beam (2)

- 5.3 The design dead load (6)
- 5.4 The maximum bending moment (4)
- 5.5 The lever arm distance (2)
- 5.6 The required compression reinforcement (3)
- 5.7 The required tension reinforcement (3)

Check for the minimum and maximum reinforcement. (2)

The self-weight of the beam must be considered in the calculations. The relevant codes and clauses must be indicated. [22]

QUESTION 6

1. Calculate the maximum effective span for a $457 \times 191 \times 89,7$ kg/m structural steel beam able to carry a 375-kN point load at mid-span. The self-weight of the beam must be included in your calculations. Use a bending stress of 175 MPa. (8)
2. Figure 2 shows a tie bar (F) welded to a gusset plate by means of TWO 8-mm side fillet welds.

Use an allowable stress of 130 MPa and calculate the safe load. (5)

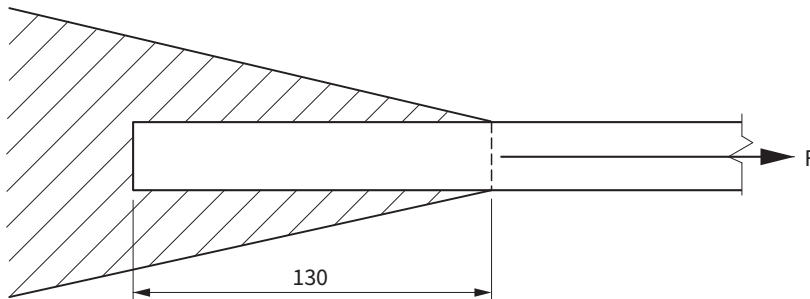


Figure 2

[13]

QUESTION 7

- 7.1 Name TWO of the materials used to charge up a steelmaking furnace. (2)
- 7.2 State the size of the concrete stone used to make concrete. (1)
- 7.3 Explain the effects of the water:cement ratio in a concrete mix. (2)
- 7.4 State the aim(s) of the water permeability test. (2)

Total: 100 marks



Exemplar examination paper 3

The following is an example of a final question paper.

Candidates are always reminded to carefully read the instructions before answering the questions.

Duration: 4 hours

Mark allocation: 100 marks

Instructions and information:

1. Answer ALL the questions. You may start with any question.
2. Number the answers according to the numbering system laid out in the question paper.
3. Start each question on a new page.
4. Draw a line across the page at the end of each answer.
6. All calculations must conform to the relevant SABS / SANS Codes of Practice.
7. All the applicable codes and reference clause numbers must be indicated.
8. Complement your answers with neat sketches.
9. Use the applicable required schedules at the back of your textbook.

REQUIREMENTS: BOE 8/6 Hot-rolled structural steel sections (red book)

OPEN-BOOK EXAMINATION

Candidates may use their own personal notes and textbooks. No past question papers and marking guidelines will be allowed in the examination centre.

QUESTION 1

- 1.1 State TWO advantages of the cupola furnace. (2)
 - 1.2 Explain how you would ensure adequate moisture content during the concrete curing process of a concrete column or wall. (2)
 - 1.3 Name any TWO tests that are done for concrete. (2)
- [6]**

QUESTION 2

Figure 1 shows a part of a strutted roof truss. The strut and tie are connected to the main rafter by means of an 8-mm thick gusset plate.

The strut and tie are single discontinuous equal-leg rolled steel angles. The Grade parts marked 'S' and 'T' are Grade 43 single discontinuous equal-leg rolled steel angles.

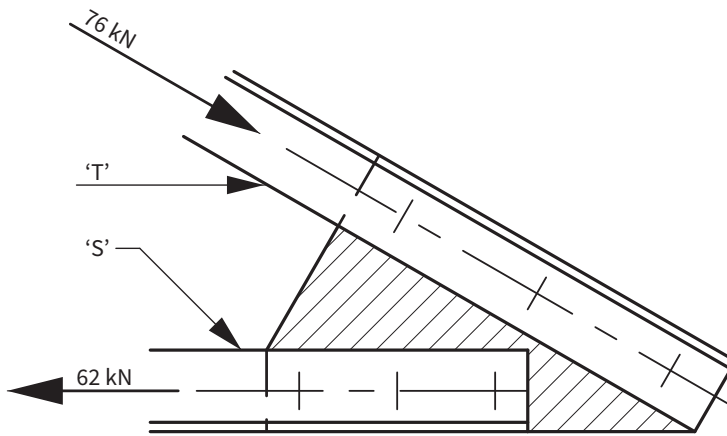


Figure 1

- 2.1 Select a suitable equal-leg rolled steel angle for the part marked 'T'. The tie will be bolted to the gusset plate using Grade 4,6 M16 bolts. (9)
 - 2.2 The strut is welded to the gusset plate using an 8-mm fillet weld. Calculate the effective length for the fillet weld. The maximum shear stress 155 MPa. (5)
- [14]**

QUESTION 3

Figure 2 shows a fully dimensioned T-beam with a span of 5,5 m.

Use Grade 25 concrete with high-yield tensile steel reinforcement to calculate suitable tension reinforcement for the T-beam. The beam will support a dead load of 6,5 kNm² and an imposed load of 7,5 kNm².

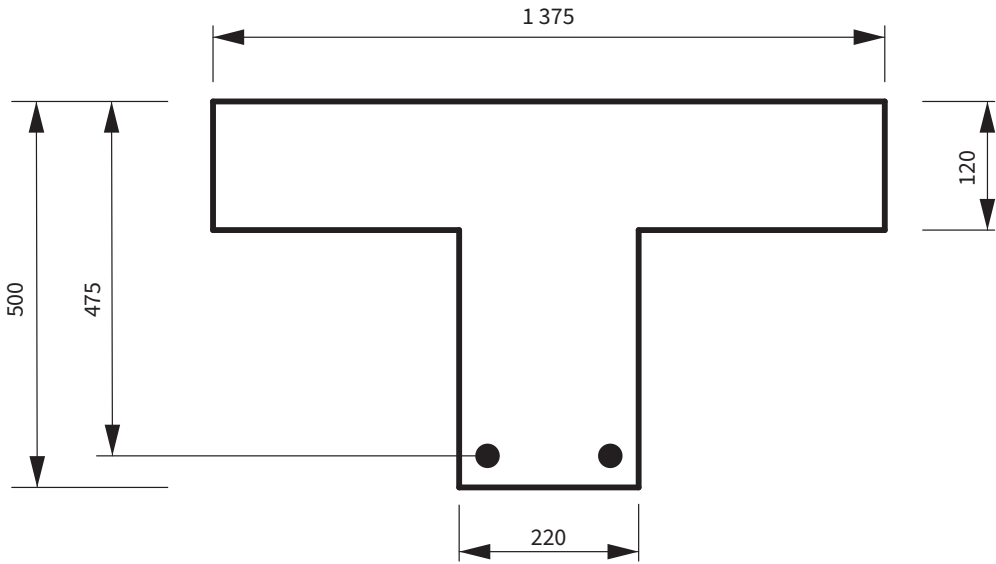


Figure 2

Your answers must include the following:

- 3.1 The lever arm distance (2)
- 3.2 The position of the neutral axis (3)
- 3.3 The total design load (2)
- 3.4 The maximum bending moment (2)
- 3.5 The required tension reinforcement. (4)

Use the formula: $AS = m + 0,1 f_{cu} b_w d(0,45 - hf) / 0,87 f_y (d - 0,5hf)$ [13]

QUESTION 4

Figure 3 shows a compound steel beam with TWO steel plates attached to the flanges of a 305 × 102 × 32,8 kg/m I-parallel flanged steel beam. The steel beam will be secured over a 6,25-m wide panoramic window.

The steel beam must support an additional uniformly distributed load of 35 kNm.

Include the self-weight of the compound beam and then calculate the maximum uniformly distributed load that the steel beam can safely support.

Use a bending stress of 165 MPa and note that the density of structural steel as 7 865kg/m³.

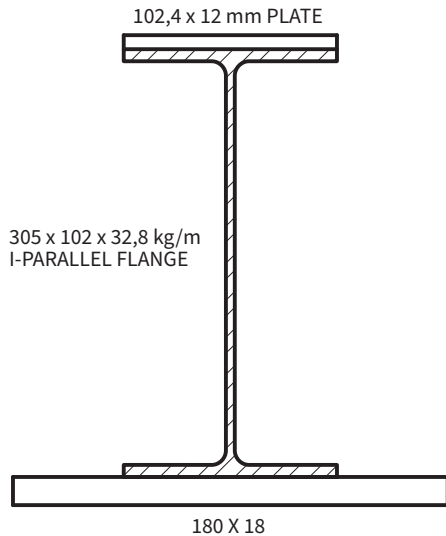


Figure 3

[20]

QUESTION 5

Figure 4 shows an eccentrically loaded connection. A load of 28 kN is subjected to the connection at a distance of 300 mm from the centre of the steel column.

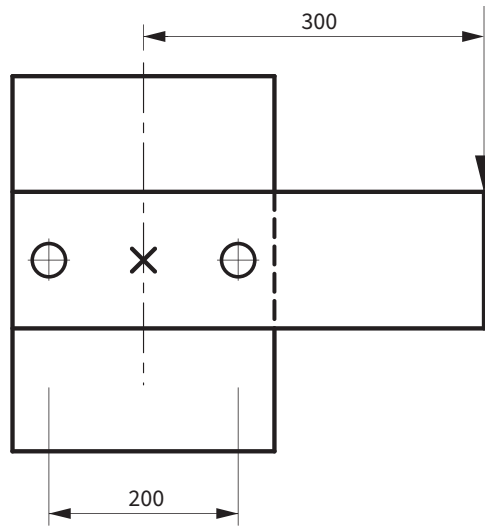


Figure 4

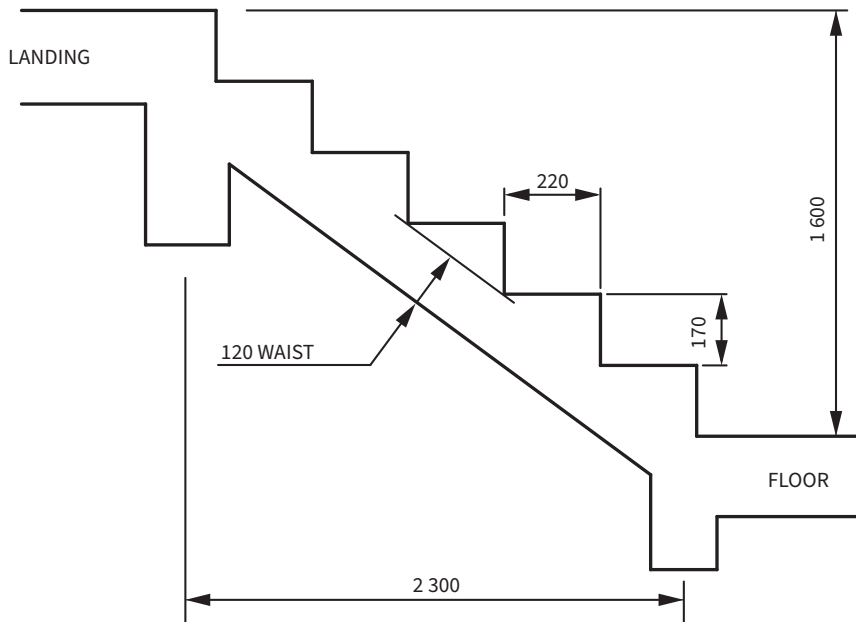
Calculate the diameter of the bolts required to hold the connection in place. Use a shear stress value of 105 MPa. [11]

QUESTION 6

A one-directional, simply supported reinforced concrete slab has an effective span of 5,25 m and supports a live load of 7,5 kNm². Use Grade 25 MPa concrete with mild steel reinforcement. The density of the concrete is 2 450 kg/m³.

Calculate the suitable tension and secondary reinforcement for the given slab.

The self-weight of the slab must be, considered in the calculations. [18]

QUESTION 7*Figure 5*

Calculate the suitable tension and secondary reinforcement for the reinforced concrete staircase shown in Figure 5. The staircase is supported at both ends and is subjected to a $12,5 \text{ kNm}^2$ imposed load. The width of the stairway is 1,15 m (1 150 mm).

The stairway is cast monolithically using Grade 20 concrete with mild steel reinforcement. The density of the concrete is 2420 kg/m^3 .

[18]**Total: 100 marks**

Exemplar examination paper 1

memorandum

The following is an example of the marking guidelines for a final examination paper.

QUESTION 1

Given information:

<p><u>305 × 165 × 40,5 kg/m I-section beam:</u></p> $I_{xx} = 85,51 \times 10^{-6} \text{ m}^4$ $\text{Area} = 5,165 \times 10^{-3} \text{ m}^2$ $\frac{h}{2} = \frac{303,8}{2} = 151,9 \text{ mm}$	<p><u>Channel: 140 mm × 60 × 16 kg/m</u></p> $I_{yy} = 0,6249 \times 10^{-6} \text{ m}^4$ $\text{Area} = 2,037 \times 10^{-3} \text{ m}^2$ $A_y = 17,5 \text{ mm}$ $T_1 = 7 \text{ mm}$
<p>Total area = $5,165 \times 10^{-3} \text{ m}^2 + 2,037 \times 10^{-3} \text{ m}^2$ Total area = $7,202 \times 10^{-3} \text{ m}^2$</p>	

<p><u>Calculate neutral axis using area moments from bottom</u></p> $7,202 \times 10^{-3} \text{ m}^2 \times Y_1 = \text{Area beam} + \text{distance to centre}$ $(5,165 \times 10^{-3} \text{ m}^2 \times 0,1519) = 0,785 \times 10^{-3}$ $+ (2,037 \times 10^{-3} \text{ m}^2 \times 0,3213) = 0,654 \times 10^{-3}$ <hr/> $\text{Total} = 1,44 \times 10^{-3} \text{ m}^2$ $Y_1 = \frac{1,44 \times 10^{-3} \text{ m}^2}{7,202 \times 10^{-3} \text{ m}^2}$ $Y_1 = 0,19994 \text{ m}$ $Y_1 = 199,94 \text{ mm}$	$303,8 + 17,5$ $= 321,3 \text{ mm}$	<p>(4)</p>
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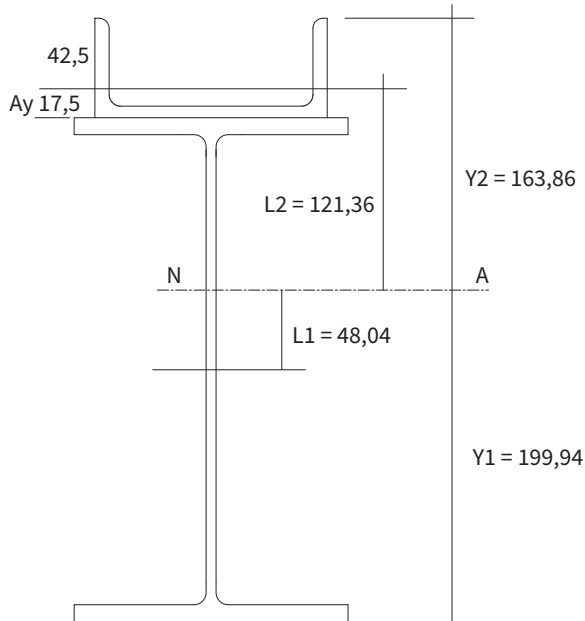


Figure A

$$L_1 = 199,94 - 151,9 = 48,04$$

$$L_2 = 163,86 - 42,5 = 121,36$$

Calculate second moment of area (I_{xx} total)

$$I_{xx \text{ tot}} = (I_{xx \text{ Beam}} + al^2) + (I_{yy \text{ Channel}} + al^2)$$

$$I_{yy \text{ Beam}} = (85,51 \times 10^{-6} + 5,165 \times 10^{-3} \times 0,04804^2)$$

$$= (85,51 \times 10^{-6} + 11,92 \times 10^{-6}) = 97,43 \times 10^{-6} \text{ m}^4$$

$$I_{xx \text{ Channel}} = (0,6249 \times 10^{-6} + 4,183 \times 10^{-3} \times 0,12136^2)$$

$$= (0,6249 \times 10^{-6} + 61,6 \times 10^{-6}) = 62,23 \times 10^{-6} \text{ m}^4$$

$$I_{xx \text{ total}} = 159,66 \times 10^{-6} \text{ m}^4$$

(5)

Calculate maximum bending moment

(Bending stress = 158 MPa)

$$\frac{M}{I} = \frac{f}{y} \text{ where } M = \frac{f \times I}{y}$$

$$BM_{\text{max}} = \frac{158 \times 159,66 \times 10^6}{199,94}$$

$$BM_{\text{max}} = 124,57 \text{ kNm}$$

(3)

<p><u>Calculate the self-weight of the beam</u> <u>Beam:</u> $40,5 \text{ kg/m} \times 9,81 \times 10^{-3} = 0,397 \text{ kNm}$ <u>Channel:</u> $16 \text{ kg/m} \times 9,81 \times 10^{-3} = 0,157 \text{ kNm}$ Total self-weight = 0,554 kNm</p>		(3)
<p><u>Calculate the maximum point load the beam can carry</u> <u>Additional 35 kNm UDL</u> beam + channel + add load + load to support</p> $BM = \frac{W l^2}{8} + \frac{W l^2}{8} + \frac{W \times L}{4} + \frac{W x l^2}{8}$ $124,57 = \frac{0,397 \times 6,75^2}{8} + \frac{0,157 \times 6,75^2}{8} + \frac{25 \times 6,75}{4} + \frac{W \times 6,75^2}{8}$ $124,57 = 2,26 + 0,894 + 42,19 + 1,688 W$ $W = \frac{124,57 - (2,26 + 0,894 + 42,19)}{5,695}$ $W = 15,85 \text{ kNm}$		(4) [20]

QUESTION 2

All references taken from SANS 10100-1 (2000).

<p>Fcu = 25 MPa Fy = 450 MPa Span = 4,80 mm</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.1) Cl. 4.3.1.2</p>	
<p><u>Determine the area of the main steel</u> Y16 at 150 centres: As = 1 340 mm²</p>		(1)
<p><u>Calculate distance of lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K^1}{0,9}} \right\}$ $Z = 175 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 175\{0,777\}$ $Z = 135,98 \text{ mm}$	<p>(CL.4.3.3.4.1)</p>	(2)
<p><u>Calculate maximum moment of resistance</u></p> $AS = \frac{M}{0,87 \times fy \times z}$ $M = 0,87 \times 450 \times 135,98 \times 1\ 340$ $M = 71,34 \text{ kNm}$	<p>(CL.4.3.3.4.1)</p>	(2)

<p><u>Determine the total load</u></p> $BM_{\max} = \frac{wL^2}{8} 71,34 = \frac{w \times 4,8^2}{8}$ $w = \frac{71,34 \times 8}{4,8^2}$ $w = 24,77 \text{ kNm}$		(2)
<p><u>Determine the dead load</u></p> <p>Dead load = area \times density $\times 9,81 \times 10^{-3}$</p> <p>Dead load = $0,2 \times 1 \times 2 430 \text{ kg/m}^3 \times 9,81 \times 10^{-3}$</p> <p>Dead load = 4,77kNm</p>		(2)
<p><u>Determine the maximum imposed load</u></p> <p>Total load = 1,2 (Gn) + 1,6 (Qn)</p> <p>24,77 = 1,2 (4,77) + 1,6 (Qn)</p> <p>Qn = 3,86 kNm</p>	(CL.4.2.2.1)	(2)
<p><u>The maximum imposed load therefore is:</u></p> <p>Qn = 11,9 kNm²</p>		(1) [12]

QUESTION 3

All references taken from SANS 10100-1 (2000).

3.1	<p>Fcu = 30 MPa</p> <p>Fy = 450 MPa</p>	<p>Table 2 (4.1.5.1)</p> <p>Table 3 (4.1.5.2)</p>	
	<p><u>Calculate the nett area of the concrete</u></p> <p>Nett area of the steel = $4\left(\frac{\pi d^2}{4}\right) + 2\left(\frac{\pi d^2}{4}\right)$</p> <p>= $4\left(\frac{\pi 20^2}{4}\right) + 2\left(\frac{\pi 16^2}{4}\right)$</p> <p>= 1 256,76 + 402</p> <p>Nett area of the steel = 1 658,76 mm²</p> <p>Nett area of concrete = $(600 \times 200) - 1 658,76 \text{ mm}^2$</p> <p>= 118 341,24 mm²</p>		(3)
	<p><u>Calculate the axial load</u></p> <p>N = 0,4 fcu Ac + 0,67 fy Asc (Cl. 4.7.4.3)</p> <p>N = $(0,4 \times 30 \times 118 341,24) + (0,67 \times 450 \times 1 658,76)$</p> <p>N = 1 420 094,8 + (500116,14)</p> <p>N = 1 920,2 kN</p>		(4)

	<p><u>Diameter and spacing of binders</u> <u>Binders:</u> $\frac{1}{4}$ of the smallest compression bar $\frac{1}{4} \times 16 = 4 \text{ mm}$ (not available) Use: min R8 binders. (R6 discontinued)</p> <p><u>Spacing of binders</u> $12 \times$ diameter of smallest compression bar $12 \times 12 = 144 \text{ mm}$ Use spacing of 140 mm.</p>	(Cl. 4.11.4.5.1)	(1)
			(1)
			(9)
3.2	<p><u>Calculate area of pad foundation</u> $\text{Area} = \frac{\Sigma \text{ of Downward loads}}{\text{Upward soil pressure}}$ $\text{Area} = \frac{3\,400 \text{ kN} + 600 \text{ kN} + 85 \text{ kN}}{220 \text{ kNm}^2}$ $\text{Area} = 18,568 \text{ m}^2$ $\text{Size of foundation} = \sqrt{18,568 \text{ m}^2}$ $4,31 \text{ m} \times 4,31 \text{ m}$ Use base size of 4,5m \times 4,5m</p>		(5) [14]

QUESTION 4

4.1	<p>Water : cement ratio = $\frac{\text{Mass of water}}{\text{Mass of cement}}$ Mass of cement = $\frac{\text{Mass of water}}{\text{Water : cement ratio}}$ Mass of cement = $\frac{46 \text{ litres}}{0,35}$ Mass of cement = 128,6 litres = 128,6 kg</p>		(3)
4.2	<p>Non-ferrous metals do not contain iron content; therefore the are resistant to rust and corrosion. Non-ferrous metals are also non-magnetic.</p>		(2)
4.3	<p>Brass is composed of copper and zinc while bronze is composed of copper and tin.</p>		(2) [7]

QUESTION 5

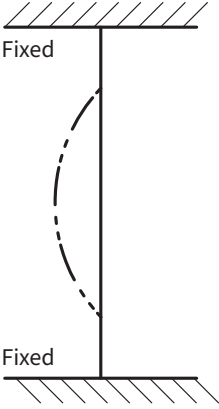
All references taken from SANS 10100-1 (2000).

	<p>$F_{cu} = 20 \text{ MPa}$ $F_y = 250 \text{ MPa}$ Span = 7,00 m Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) Cl. 4.3.1.2 $2\,400 \text{ kg/m}^3$</p>	
5.1	<p><u>Determine the effective depth of the slab</u> Effective depth = span / 16 Effective depth = $7\,000 / 16$ Effective depth = 437,5 mm</p>	<p>Table 10 (Cl.4.3.6.2.1)</p>	(1)
	<p><u>Determine the overall depth</u> Assume R20 main steel, R8 binders and 25 mm cover. Overall depth = $437,5 + 10 + 8 + 25$ Overall depth = 480,5 mm (Use overall depth = 500 mm)</p>		(2)
5.2	<p><u>Determine the design dead loads of the beam</u> Design dead load = Volume \times density $\times 9,81 \times 10^{-3} \times 1,2Q_n$ DDL = $0,50 \times 0,32 \times 1 \times 2\,400 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2 \text{ Gn}$ Design dead load = 4,52 kNm Design imposed UDL = $7 \text{ kNm} \times 1,6Q_n = 11,2 \text{ kNm}$ Design imposed point load = $12 \text{ kN} \times 1,6Q_n = 19,2 \text{ kN}$</p>	<p>Cl.4.2.2.1 Cl.4.2.2.1</p>	(4)
	<p><u>Calculate bending moment maximum</u> $BM_{\max} = \frac{WL^2}{8} + \frac{WL^2}{8} + \frac{WL}{4}$ $BM_{\max} = \frac{4,52 \times 7^2}{8} + \frac{11,2 \times 7^2}{8} + \frac{19,2 \times 7}{4}$ $= 27,69 + 68,6 + 33,6$ $BM_{\max} = 129,89 \text{ kNm}$</p>		(3)
	<p><u>Calculate value for 'K'</u> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{129,89 \times 10^6}{20 \times 320 \times 437,5^2}$ $K = 0,106 < K^1 = 0,156$ Provide tension reinforcement only.</p>	<p>(Cl.4.3.3.4.1)</p>	(2)

	<p><u>Calculate distance of lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k}{0,9}} \right\} \leq 0,95d$ $Z = 437,5 \left\{ 0,5 + \sqrt{0,25 - \frac{0,106}{0,9}} \right\} \leq 0,95 \times 437,5$ $Z = 437,5 \{0,864\} \leq 415,63$ $Z = 377,84 \text{ mm} < 415,63 \text{ mm}$	(Cl.4.3.3.4.1)	(2)
	<p><u>Calculate tension reinforcement</u></p> $A_s = \frac{M}{0,87 \times f_y \times z}$ $A_s = \frac{129,89 \times 10^6}{0,87 \times 250 \times 377,84}$ $A_s = 1\,518,72 \text{ mm}^2$ <p>Use 4R25 ($A_s = 1\,964 \text{ mm}^2$)</p>	(Cl.4.3.3.4.1)	(3)
5.3	<p><u>Check for minimum main reinforcement</u></p> $\frac{100 A_s}{A_c}$ $= \frac{100 \times 1\,964}{500 \times 320}$ $= 0,92$ $1,23 > 0,8$ <p>The reinforcement is sufficient.</p>	Table 23 (Cl.4.11.4)	(2)
	<p><u>Check for maximum area of reinforcement</u></p> <p>4% of AC</p> $4\% \times 500 \times 320$ $6\,400 \text{ mm}^2$ $1\,964 < 6\,400$ <p>The reinforcement is sufficient.</p>	(Cl.4.11.5.1)	(1) [20]

QUESTION 6

6.1	<p><u>Calculate the effective length</u></p> <p>Effective height (l) = $1,0 \times L$</p> $L_{\text{effective}} = 1 \times 4,75 \text{ m}$ $= 4\,750 \text{ mm (4,750 m)}$	(SABS 0162-1984 Table 19)	(3)
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	<p><u>Calculate the slenderness ratio</u></p> $L/r = \frac{4\,750}{37,7} = 125,99 \text{ (Use 126 MPa)}$ <p><u>From Table 17 (SABS 0162-1984)</u></p> $126 = 55 \text{ MPa}$		(2)
	<p><u>Calculate the maximum load</u></p> <p>Load = Stress × Area</p> $\text{Load} = 55 \text{ N/mm}^2 \times 5,702 \times 10^3 \text{ mm}^2$ $\text{Load} = 313,61 \text{ kN}$		(2)
6.2	<p>SABS 0162 -1984 Table 19 states that the compression member will be, effectively held in position and restrained against rotation at both ends.</p> <p><u>The symbol:</u></p> <div style="text-align: center;">  <p><i>Figure B</i></p> </div> <p><u>Mark allocation:</u></p> <p>Code and reference stated = 1 mark</p> <p>Description corr. = 1mark</p> <p>Drawing = 2 marks</p>		(2)
			(2)
			[13]

QUESTION 7

I-Parallel flange 203 × 133 × 25,3 kg/m		
<p><u>Given information:</u></p> <p>Beam A: $I_{xx} = 23,49 \times 10^{-6} \text{ m}^3$</p> $\frac{h}{2} = \frac{203,2}{2} = 101,5 \text{ mm}$	<p>Beam B: $I_{yy} = 3,090 \times 10^{-6} \text{ m}^3$</p> $\frac{b}{2} = \frac{133,4}{2} = 66,7 \text{ mm}$	

Calculate bending moment maximum

7.1	<p><u>Beam A:</u></p> $\frac{M}{I} = \frac{F}{Y}$ $M = \frac{f \times I}{y}$ $M = \frac{165 \times 23,49 \times 10^6}{101,5}$ $M = 38,186 \text{ kN m}$	<p><u>Beam B:</u></p> $\frac{M}{I} = \frac{F}{Y}$ $M = \frac{f \times I}{y}$ $M = \frac{165 \times 3,090 \times 10^6}{66,7}$ $M = 7,643 \text{ kN m}$	<p>(3)</p> <p>+</p> <p>(3)</p>
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Calculate maximum point load

7.1	<p><u>Beam A:</u></p> $BM = \frac{Wl^2}{8}$ $38,186 = \frac{W \times 5,55^2}{8}$ $W = \frac{38,186 \times 8}{5,55^2}$ $W = \text{UDL} = 9,92 \text{ kNm}$	<p><u>Beam B:</u></p> $BM = \frac{Wl^2}{8}$ $7,643 = \frac{W \times 5,55^2}{8}$ $W = \frac{7,643 \times 8}{5,55^2}$ $W = \text{UDL} = 1,98 \text{ kNm}$	<p>(2 × 4)</p>
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7.2 The loads (W) are not the same because the **second moment of area differs as the beams rotated**. This also causes the **section modulus to change**.
 At beam 'A', the load is, subjected vertically through the stronger centre of the beam.
 At beam 'B', the load is, subjected on the horizontal web. This will cause the web to bend, thus collapsing the beam. (2)

7.3

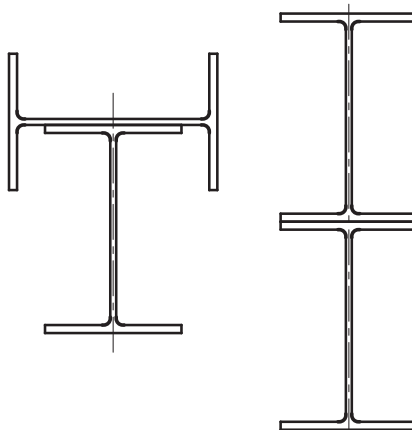


Figure C

(Also consider alternative arrangements.)

(2 × 2)

[16]

Total: 100 marks

Exemplar examination paper 2

memorandum

QUESTION 1

All references taken from SANS 10100-1 (2000).

	<p>$f_{cu} = 30 \text{ MPa}$ $f_y = 450 \text{ MPa}$ Axial load = 7 500 kN</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2)</p>	
1.1	<p><u>Calculate the number of longitudinal reinforcement</u> $N = 0,4 f_{cu} A_c + 0,67 f_y A_{sc}$ (Cl. 4.7.4.3) $7\,500 \times 10^3 = 0,4 \times 30 \times \left(\frac{\pi 850^2}{4}\right) + 0,67 \times 450 \times A_{sc}$ $8\,500 \times 10^3 = 6\,809\,402,07 + 301,5 A_{sc}$ $7\,500 \times 10^3 \text{ minus } 6\,809\,402,07 = 301,5 A_{sc}$ $A_{sc} = \frac{690\,597,93}{301,5}$ $A_{sc} = 2\,290,54 \text{ mm}^2$ Use 8Y20 ($A_s = 2\,513 \text{ mm}^2$) (Minimum spacing between bars = height aggregate + 5 mm)</p>		(4)
1.2	<p><u>Maximum and minimum percentage of the steel reinforcement</u> <u>Maximum:</u> 6% of gross sectional area (Cl. 4.11.4.5.2) $6\% \times \left(\frac{\pi 850^2}{4}\right) = 34\,047,01 \text{ mm}^2$ <u>Minimum:</u> 0,4% of gross sectional area (Table 23) $0,4\% \times \left(\frac{\pi 850^2}{4}\right) = 2\,269,8 \text{ mm}^2$</p>		(2)
1.3	<p><u>Calculate the diameter of the helical binder</u> <u>Binders:</u> $\frac{1}{4}$ of the smallest main bar $\frac{1}{4} \times 32 = 8 \text{ mm}$ Use: R8 Helical binder.</p>	(Cl. 4.11.4.5.1)	(2)

Calculate the pitch of the binder.

Spacing of binders:

12 × diameter of smallest main bar

12 × 20 = 240 mm (maximum)

Use Binder pitch = 240 mm

Summary:

8y20 main bars with R8 helical binders at 240 mm pitch.

(Cl. 4.11.4.5.1)

(2)

1.4

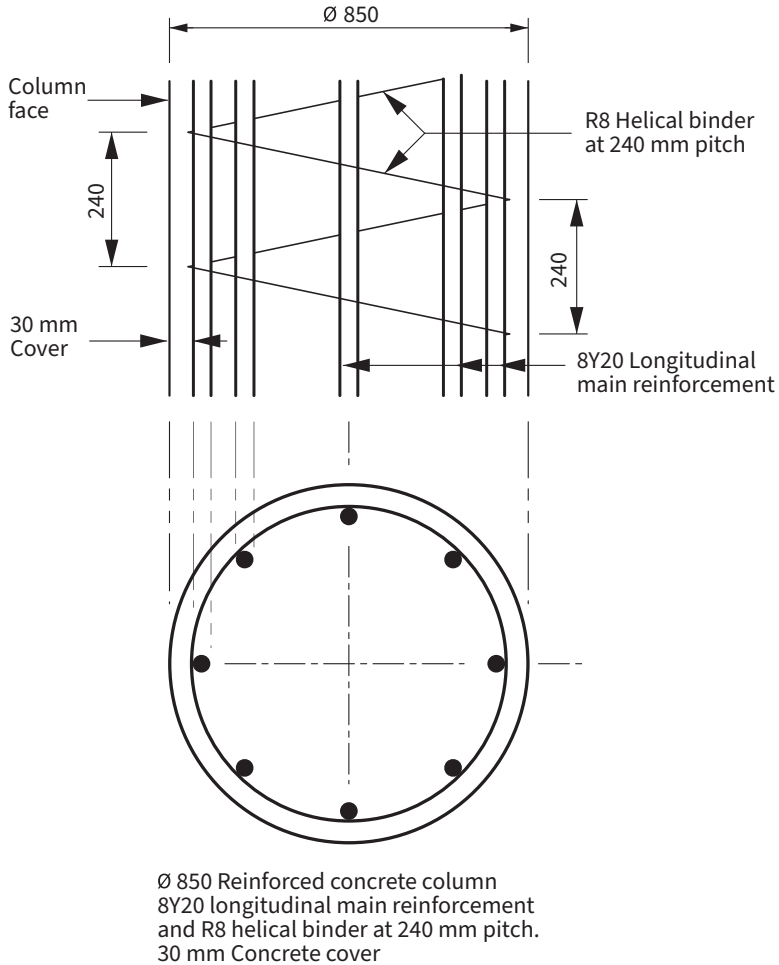


Figure A

Top view correct = 1

Sectional view = 2

Reinforcement = 2

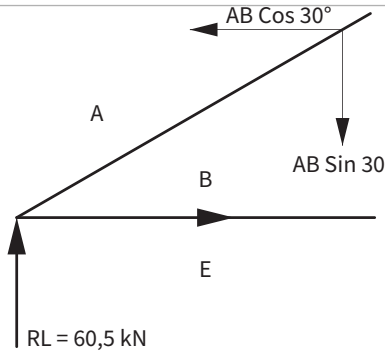
5

[15]

QUESTION 2

2.1	<p><u>Calculate the reactions</u></p> <p><u>Take moments about RL:</u></p> $(RR \times 9) = (48 \times 6,75) + (55 \times 4,5) + (28 \times 2,25)$ $RR9 = 324 + 247,5 + 63$ $RR = 634,5 / 9$ $RR = 70,5 \text{ kN}$ <p><u>Take moments about RR:</u></p> $(RL \times 9) = (28 \times 6,75) + (55 \times 4,5) + (48 \times 2,25)$ $RL 9 = 189 + 247,5 + 108$ $RL = 544,5 / 9$ $RL = 60,5 \text{ kN}$		(2)
			(2)

Determine the size and type of the members.

2.2	$\Sigma VC = 0$ $AB \sin 30^\circ = 60,5 \text{ kN}$ $AB = 60,5 / \sin 30^\circ$ $AB = 121 \text{ kN (Strut)}$ $\Sigma HC = 0$ $BE = A \cos 30^\circ$ $BE = 121 \times \cos 30^\circ$ $BE = 104,79 \text{ kN (Tie)}$	 <p style="text-align: center;"><i>Figure B</i></p>	(6)
	$\Sigma VC = 0$ $121 \sin 30^\circ + BD \sin 30^\circ = 28 + CD \sin 30^\circ$ $60,5 + 0,5BD = 28 + 0,5CD$ $60,5 + 0,5BD - 28 = 0,5CD$ $32,5 + 0,5BD = 0,5CD$ $CD = \frac{32,5 + 0,5BD}{0,5}$ $CD = 65 + BD \dots (1)$		(3)

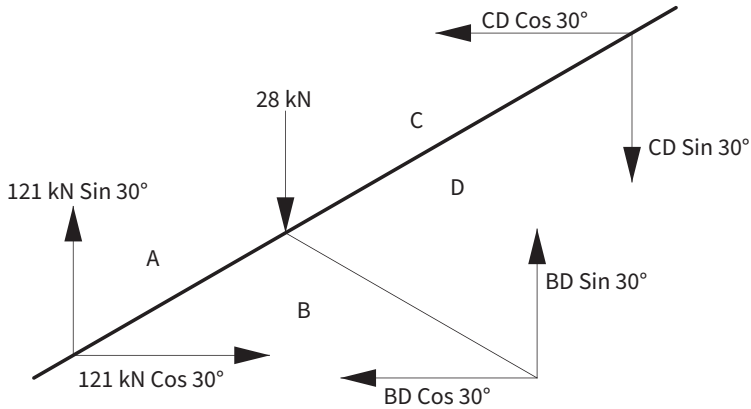


Figure C

2.3 $\Sigma HC = 0$
 $121 \cos 30^\circ = CD \cos 30^\circ + BD \cos 30^\circ$
 $104,79 = 0,866 CD + 0,866 BD$
 $104,79 = 0,866 (65 + BD) + 0,866 BD$
 $104,54 = 56,29 + 0,866 BD + 0,866 BD$
 $BD = \frac{164,54 - 56,29}{1,732}$
 $BD = 62,5 \text{ kN (Strut)}$
 Therefore $CD = 65 + BD$
 $CD = 65 + 62,5 = 127,50 \text{ kN (Strut)}$

(5)
 [18]

QUESTION 3

Calculate reactions

3.1 Take moments about RL:
 $(RR \times 9) = (12,8 \times 9 \times 4,5) + (4,475 \times 9 \times 4,5) + (88 \times 5,5)$
 $RR = 518,4 + 181,24 + 484 / 9 (1\ 183,64 / 9)$
 $RR = 131,52 \text{ kN}$
Take moments about RR:
 $(RL \times 9) = (12,8 \times 9 \times 4,5) + (4,475 \times 9 \times 4,5) + (88 \times 3,5)$
 $RL = 518,4 + 181,24 + 308 / 9 (1\ 007,64 / 9)$
 $RL = 111,96 \text{ kN}$

(2)

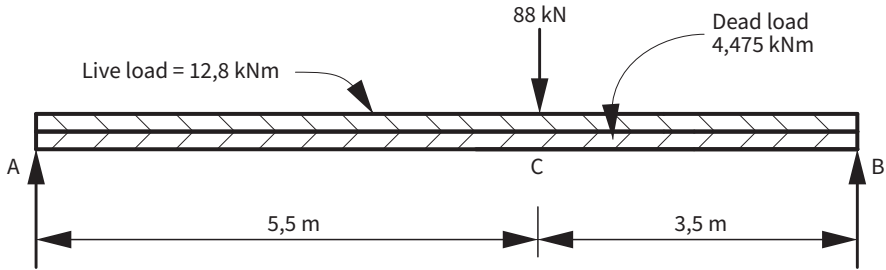


Figure D

3.2 Shear force diagram

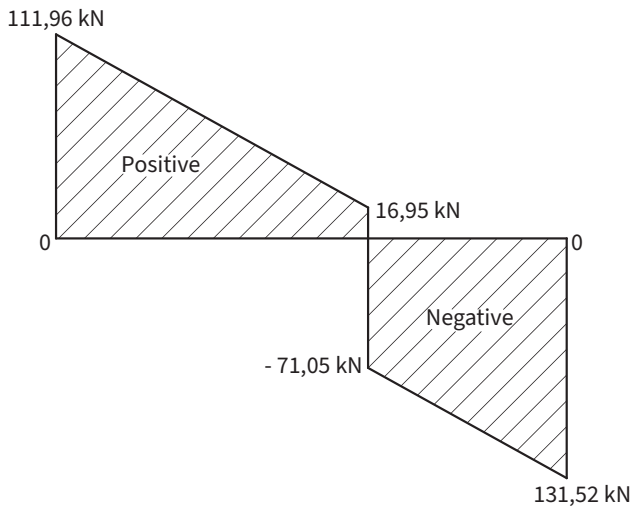


Figure E

(2)

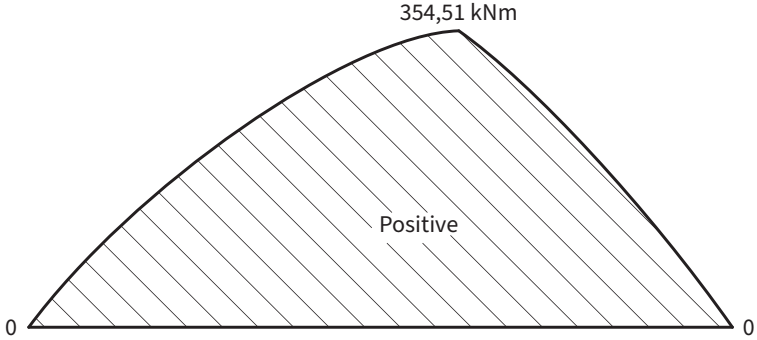
3.3 Calculate bending moment Max

$$\text{BM at 'C': } (131,52 \times 3,5) - (12,8 \times 3,5 \times 1,75) - (4,475 \times 3,5 \times 1,75)$$

$$460,32 - 78,4 - 27,41$$

$$\text{BM at 'C' = } 354,51 \text{ kNm}$$

(2)

	<p>Bending moment diagram</p>  <p style="text-align: center;"><i>Figure F</i></p>		(2)
3.4	<p>Calculate value for 'K'</p> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{354,51 \times 10^6}{25 \times 330 \times 425^2}$ $K = 0,238$ <p>$K < K^1 = 0,156$ Compression reinforcement will therefore be required.</p>	<p>(Cl.4.3.3.4.1)</p> <p>$d = 475 - 50$ cover $= 425 \text{ mm}$</p>	(3) [13]

QUESTION 4

4.1	<p>Select a suitable I-section steel beam</p> $\frac{M}{I} = \frac{f}{y}$ <p>Bending moment max = $\frac{w \times l^2}{8}$</p> $= \frac{65 \times 6,35^2}{8}$ <p>BM max = 327,62 kNm</p> <p>Then:</p> $z = \frac{M}{f}$ $z = \frac{327,62 \times 10^6}{156}$ <p>$z = 2\,100\,128,2 \text{ mm}^3$</p> <p>$z = 2\,100,13 \times 10^{-6} \text{ m}^3$</p> <p>Select 533 × 210 × 101 kg/m (Z_e value = $2\,297 \times 10^{-6} \text{ m}^3$)</p>		(5)
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<p>4.2 <u>Check if the beam is adequate</u> Determine the self-weight of the beam Dead load = $101 \text{ kg/m} \times 9,81 \times 10^{-3}$ Dead load = 0,991 kNm</p> <p>Total load = 65 kNm + 0,991 kNm = 65,991 kNm</p> <p>Revised bending moment max = $\frac{w \times l^2}{8}$ = $\frac{65,991 \times 6,35^2}{8}$</p> <p>BM max = 332,62 kNm</p> <p>Maximum bending moment Then: $z = \frac{M}{f}$ $z = \frac{332,62 \times 10^6}{156}$ $z = 2\,132\,187,5 \text{ mm}^3$ $z = 2\,132,9 \times 10^{-6} \text{ m}^3$</p> <p>The selected steel beam is $533 \times 210 \times 101 \text{ kg/m}$ (Z_e value = $2\,297 \times 10^{-6} \text{ m}^3$) is adequate the support its own weight as well as the imposed load.</p>	<p>(7) [12]</p>
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QUESTION 5

All references taken from SANS 10100-1 (2000).

<p>Fcu = 25 MPa Fy = 450 MPa Span = 8 metres Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) Cl. 4.3.1.2 2 425 kg/m³</p>	<p>(5)</p>
<p>5.1 <u>Determine the effective depth of the beam</u> Effective depth = span / 16 Effective depth = 8 000 / 16 Effective depth = 500 mm</p>	<p>Table 10 (4.3.6.2.1)</p>	<p>(1)</p>

5.2	<p><u>Determine the overall depth</u> Assume Y25 main steel and Y10 binders Assume Cover of 25 mm. Overall depth = $500 + \frac{25}{2} + 10 + 25$ Overall depth = 547,5 mm (Use overall depth = 550 mm)</p>		(2)
	<p><u>Determine the design dead loads of the beam</u> Design dead load = Volume \times density $\times 9,81 \times 10^{-3} \times 1,2G_n$ DDL = $0,55 \times 0,33 \times 1 \times 2 425 \text{ kg/m}^3 \times 9,81 \times 10^{-3} \times 1,2 \text{ Gn}$ Design dead load = 5,18 kNm</p> <p>Design imposed load = $36 \text{ kNm} \times 1,6Q_n$ Design imposed load = 57,6 kNm</p> <p>Total design load = $5,18 + 57,6 = 62,78 \text{ kNm}$</p>	(Cl.4.2.2.1)	(2)
5.3	<p><u>Calculate bending moment maximum</u> $BM_{\max} = \frac{WL^2}{8}$ $BM_{\max} = \frac{62,78 \times 8,0^2}{8}$ $BM_{\max} = 502,25 \text{ kNm}$</p>		(2)
	<p><u>Calculate value for 'K'</u> $k = \frac{BM}{f_{cu} b d^2}$ $k = \frac{502,25 \times 10^6}{25 \times 330 \times 500^2}$ $k = 0,244 > K^1 = 0,156$ Tension and compression reinforcement required.</p>	(Cl.4.3.3.4.1)	(2)
5.4	<p><u>Calculate distance of lever arm (Z)</u> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k^1}{0,9}} \right\}$ $Z = 500 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 500\{0,777\}$ $Z = 388,50 \text{ mm}$</p>	(Cl.4.3.3.4.1)	(2)

5.5	<p><u>Determine compression reinforcement</u></p> $A_s = \frac{(k - k^1) F_{cu} b d^2}{F_{yc} (d - d^1)} \text{ (Use } d^1 = 50 \text{ mm)}$ <p>Where: $F_{yc} = \frac{F_y}{1,15 + \frac{F_y}{2\,000}}$</p> $F_{yc} = \frac{450}{1,15 + \frac{450}{2\,000}}$ $F_{yc} = 327 \text{ MPa}$ $A_s = \frac{(0,244 - 0,156) 25 \times 330 \times 500^2}{327 (500 - 50)}$ $A_s = 1\,233,44 \text{ mm}^2$ <p>Use 4Y20 ($A_s = 1\,257 \text{ mm}^2$)</p>	(Cl.4.3.3.4.1)	
	<p><u>Check for minimum compression reinforcement</u></p> $\frac{100 A_s}{A_c} = \frac{100 \times 1\,257}{550 \times 330}$ $= 1,06$ <p>$0,69 > 0,24$</p> <p>The reinforcement is sufficient.</p>	Table 23 (Cl.4.11.4)	(1)
5.6	<p><u>Determine tension reinforcement</u></p> $A_s = \frac{k^1 F_{cu} b d^2}{0,87 \times f_y \times z} + \frac{A'_s F_{yc}}{0,87 \times f_y}$ $A_s = \frac{0,156 \times 25 \times 330 \times 500^2}{0,87 \times 450 \times 388,5} + \frac{1\,257 \times 327}{0,87 \times 450}$ $A_s = 2\,115,42 + 1\,049,91$ $A_s = 3\,165,33 \text{ mm}^2$ <p>Use 4y32 ($A_s = 3\,217 \text{ mm}^2$)</p>	(Cl.4.3.3.4.2)	
5.7	<p><u>Check for minimum main reinforcement</u></p> $\frac{100 A_s}{A_c} = \frac{100 \times 3\,217}{550 \times 330}$ $= 1,77$ <p>$1,77 > 0,45$</p> <p>The reinforcement is sufficient</p>	Table 23 (Cl.4.11.4)	

	<p><u>Check for maximum area of reinforcement</u> 4% of AC $4\% \times 550 \times 330$ $5\,940\text{ mm}^2$ $(3\,217 + 1\,257) < 7\,260$ The reinforcement is sufficient</p>	(Cl.4.11.5.1)	(1) [22]
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QUESTION 6

6.1	<p><u>I-Section parallel flange (457 × 191 × 89,7 kg/m)</u> $I_{xx} = 411,4 \times 10^{-6}\text{ m}^4$ $Y = 463,6/2 = 231,8\text{ mm}$ Bending stress = 175 MPa</p>		
	<p><u>Self-weight of the steel beam</u> Weight = $89,7\text{ kg/m} \times 9,81 \times 10^{-3}$ Weight = 0,88 kNm</p>		(1)
	<p><u>Calculate the bending moment maximum</u> $BM_{\max} = \frac{wL}{4} + \frac{WL^2}{8}$ $BM_{\max} = \frac{375 \times L}{4} + \frac{0,88 \times L^2}{8}$ $BM_{\max} = (93,75 L + 0,11 L^2)$</p>		(2)
	<p><u>Equate to maximum bending moment</u> $\frac{M}{I} = \frac{f}{y}$ $\frac{(93,73 L + 0,11 L^2) \times 10^6}{411,4 \times 10^6} = \frac{175}{231,8}$ $231,8 (93,73 L + 0,11 L^2) = 175 \times 411,4$ $21\,726,614 L + 25,498 L^2 = 71\,995$ Span: $25,489 L^2 + 21\,726,614 L = 71\,995$ (divide by 25,489) Span: $L^2 + 852,09 L - 2\,823,55$ $Span = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $Span(L) = \frac{-852,09 \pm \sqrt{852,09^2 - 4 \times 1 \times -2\,823,55}}{2 \times 1}$ $Span(L) = \frac{-852,09 \pm 858,69}{2}$ Span(L) = 3,3 m</p>		(5) [8]

6.2	Effective length on each side: $130 - (2 \times 8) = 114 \text{ mm}$ Total effective length: $2 \times 114 = 228 \text{ mm}$ Throat thickness: $\sin 45^\circ \times 8 = 5,66 \text{ mm}$ Throat area: $5,66 \text{ mm} \times 228 \text{ mm}$ $= 1\,290,5 \text{ mm}^2$ Safe load: Stress \times area $130 \frac{\text{N}}{\text{mm}^2} \times 1\,290,5 \text{ mm}^2$ $= 167,765 \text{ kN}$		(5) [13]
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QUESTION 7

- 7.1 Any TWO of the following:
 Iron ore, coal, limestone and recycled steel. (2)
- 7.2 19 mm. (Also accept 13 mm). (1)
- 7.3 Any TWO of the following:
 The water:cement ratio determines the potential **strength, permeability** and **durability** of the hardened concrete. (2)
- 7.4 The aim of the water permeability test is to determine how **durable and resistant the concrete is in extreme weather conditions and exposure to its environment.** (2)
- [7]

Total: 100 marks

Exemplar examination paper 3

memorandum

QUESTION 1

1.1	<p>Any TWO of the following:</p> <ul style="list-style-type: none"> • It has simple construction design. • The cupola requires less floor space. • A can melt a wide range of materials. • The construction and maintenance of the cupola is cost effective. • It does not require highly skilled operators. 		(2)
1.2	<p>Any TWO of the following:</p> <ul style="list-style-type: none"> • Leaving the formwork in place, • Covering the concrete with a material that would shelter it from direct sunlight by keeping the concrete moist. • Applying a membrane-forming compound. 		(2)
1.3	<p>Any TWO of the following:</p> <ul style="list-style-type: none"> • The bending test • The slump test. • The water permeability test • The cube test. • The concrete abrasion test. 		(2) [6]

QUESTION 2

2.1	<p><u>Select a suitable rolled steel angle for marked part 'S' (Tie)</u> Force = 62 kN Select trial section: 70 × 70 × 6 mm. Area = 0,813 × 10³ mm² Allowable stress = 155 MPa</p> <p><u>Calculate effective area (A_{eff})</u> $A_{\text{eff}} = \frac{3(A_1)^2 + 4 A_1 A_2}{3A_1 + A_2}$ <u>A₁ = Connected leg</u> $A_1 = t(b - \frac{t}{2}) - (\text{area of hole})$ $A_1 = 6(70 - \frac{6}{2}) - (22 \times 10) \text{ (M18 bolts)}$ $A_1 = 294 \text{ mm}^2$ <u>A₂ (unconnected leg) 90</u> $A_2 = t(b - \frac{t}{2})$ $A_2 = 6(70 - \frac{6}{2})$ $A_2 = 402 \text{ mm}^2$ $A_{\text{eff}} = \frac{3(294)^2 + 4(294)(402)}{3(294) + (402)}$ $A_{\text{eff}} = \frac{732\,060}{1\,284}$ $A_{\text{eff}} = 570,14 \text{ mm}^2 \text{ (} 0,57014 \times 10^3 \text{ mm}^2 \text{)}$</p>	<p>(SABS 0162 Table 20)</p> <p>(SABS 0162 Cl. 9.2.1) Where A₁ is the connected leg and A₂ is the unconnected leg</p>	<p>(2)</p> <p>(3)</p>
	<p><u>Therefore Load:</u> Force = Pt × A_{eff} Force = 155 Nmm² × 570,14 mm² Force = 88,4 kN The bolted tie bar will be able to withstand the given load of 62 kN</p>	<p>(Table 20 SANS 10162)</p>	<p>(3)</p>

<p>2.2</p>	<p><u>Select a suitable rolled steel angle for marked Part ‘T’ (Strut)</u> Force = 76 kN The angle is discontinuous. Actual length = 0,9 m Effective length = $0,9 \times 0,85$ $L_{\text{eff}} = 0,765$ (765 mm) Select trial section: $70 \times 70 \times 6$ mm. Area = $0,813 \times 10^3$ mm² $R_{\text{min}} = 13,7$ mm <u>Calculate slenderness ratio</u> $L/r = \frac{765}{13,7}$ $= 55,83 \quad 55,83 = 129,15 \text{ MPa (Table 17)}$</p>	<p>(SABS 0162 Table 20)</p>	<p>(3)</p>
<p>2.3</p>	<p><u>Therefore load:</u> <u>Calculate the load</u> Load = stress \times area $= 107,25 \times 0,183 \times 10^3$ Load = 87,2 kN The $70 \times 70 \times 6$ will be suitable.</p>	<p>(Table 20 SANS 10162)</p>	<p>(2) [13]</p>

QUESTION 3

All references taken from SANS 10100-1 (2000).

	<p>$F_{\text{cu}} = 25$ MPa $F_y = 450$ MPa Effective span Dead load Imposed load</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) 5,5 m 6,5 kNm² 7,5 kNm²</p>	
<p>3.1</p>	<p><u>Calculate the lever arm distances</u> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{K^1}{0,9}} \right\} \leq 0,95d$ $Z = 475 \left\{ 0,5 + \sqrt{0,25 - \frac{0,156}{0,9}} \right\}$ $Z = 475(0,777)$ $Z = 369,1 \text{ mm}$</p>	<p>(Cl.4.3.3.4.1)</p>	<p>(2)</p>

3.2	<u>Determine the position of the neutral axis</u> $X = \frac{d - z}{0,45}$ $X = \frac{475 - 369,1}{0,45}$ $X = 235,33 \text{ mm} > 150 \text{ mm}$ Therefore, the N A lies below the flange.	(Cl.4.3.3.4.1)	(3)
3.3	<u>Calculate the total design load</u> $W = 1,2(G_n) + 1,6(Q_n)$ $W = 1,2(6,5 \times 1) + 1,6(7,5 \times 1)$ $W = 7,80 + 12,0$ $W = 19,8 \text{ kNm}$	(Cl.4.3.3.4.1)	(2)
3.4	<u>Calculate bending moment due to the concrete</u> $BM = \frac{wl^2}{8}$ $BM = \frac{19,8 \times 5,5^2}{8}$ $BM = 74,87 \text{ kNm}$	(Cl.4.3.3.4.1)	(2)
3.5	<u>Calculate tension reinforcement</u> $A_s = \frac{m + 0,1 f_{cu} b_w d (0,45d - h_f)}{0,87 f_y (d - 0,5h_f)}$ $A_s = \frac{74,87 \times 10^6 + (0,1 \times 25 \times 220 \times 475) (0,45 \times 475 - 120)}{0,87 \times 450 (475 - 0,5 \times 120)}$ $A_s = \frac{74,87 \times 10^6 + (261\ 250) (93,75)}{0,87 \times 450 (415)}$ $A_s = \frac{74,87 \times 10^6 + 24\ 492\ 187,5}{162\ 472,5}$ $A_s = \frac{99\ 362\ 187,5}{162\ 472,5}$ $A_s = 611,55 \text{ mm}^2$ Use 2R20 bars ($A_s = 628 \text{ mm}^2$)	(Cl.4.3.3.4.2)	(1) (1) (2) [13]

QUESTION 4

Given information:

<p>3.2</p> <p><u>Plate: 180 mm × 18 mm</u></p> $I_{xx} = \frac{bd^3}{12} = \frac{0,180 \times 0,018^3}{12} = 0,0875 \times 10^{-6} \text{ m}^4$ $\text{Area} = 0,180 \times 0,018 = 3,24 \times 10^{-3} \text{ m}^2$ <p><u>305 × 102 × 32,6 kg/m I-Parallel flange:</u></p> $I_{xx} = 65,01 \times 10^{-6} \text{ m}^4$ $\text{Area} = 4,183 \times 10^{-3} \text{ m}^2$ $\frac{h}{2} = \frac{312,7}{2} = 156,35 \text{ mm}$ <p><u>Plate: 102,4 mm × 12 mm</u></p> $I_{xx} = \frac{bd^3}{12} = \frac{0,1024 \times 0,012^3}{12} = 0,01475 \times 10^{-6} \text{ m}^4$ $\text{Area} = 0,1024 \times 0,012 = 1,229 \times 10^{-3} \text{ m}^2$ $\text{Total area} = 3,24 \times 10^{-3} \text{ m}^2 + 4,183 \times 10^{-3} \text{ m}^2 + 1,229 \times 10^{-3} \text{ m}^2$ $\text{Total Area} = 8,652 \times 10^{-3} \text{ m}^2 \text{ (1)}$	
<p>4.</p> <p><u>Calculate neutral axis using area moments from bottom</u></p> $8,652 \times 10^{-3} \text{ m}^2 \times Y_1 =$ $(3,24 \times 10^{-3} \text{ m}^2 \times 0,009) = 0,0292 \times 10^{-3}$ $+ (4,183 \times 10^{-3} \text{ m}^2 \times 0,1895) = 0,7921 \times 10^{-3}$ $+ (1,229 \times 10^{-3} \text{ m}^2 \times 0,3367) = 0,4138 \times 10^{-3}$ $\text{Total} = 1,2351 \times 10^{-3} \text{ m}^2$ <hr style="width: 50%; margin-left: 0;"/> $Y_1 = \frac{1,2351 \times 10^{-3} \text{ m}^2}{8,652 \times 10^{-3} \text{ m}^2}$ $Y_1 = 0,14275 \text{ m}$ $Y_1 = 142,75 \text{ mm}$	<p>(4)</p>

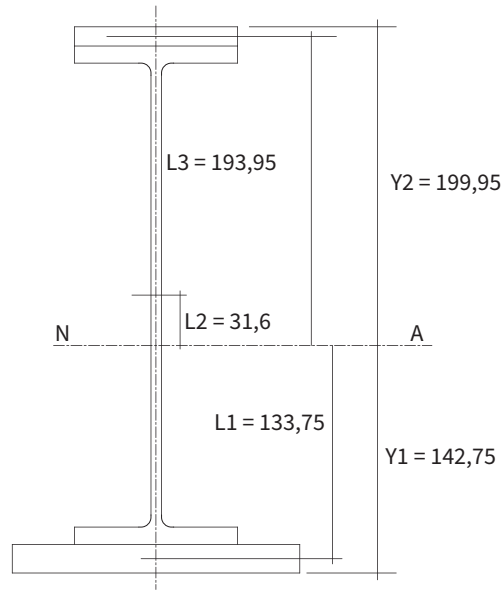


Figure A

4. Calculate second moment of area (I_{xx} total)

$$I_{xx \text{ tot}} = (I_{xx \text{ Plate}} + al^2) + (I_{xx \text{ Beam}} + al^2) + (I_{xx \text{ Plate}} + al^2)$$

$$I_{yy \text{ Plate}} = (0,0875 \times 10^{-6} + 3,24 \times 10^{-3} \times 0,13375^2)$$

$$= (0,0875 \times 10^{-6} + 57,96 \times 10^{-6}) = \underline{58,05 \times 10^{-6} \text{ m}^4}$$

$$I_{xx \text{ Beam}} = (65,01 \times 10^{-6} + 4,183 \times 10^{-3} \times 0,0316^2)$$

$$= (65,01 \times 10^{-6} + 4,177 \times 10^{-6}) = \underline{69,87 \times 10^{-6} \text{ m}^4}$$

$$I_{xx \text{ Plate}} = (0,01475 \times 10^{-6} + 1,229 \times 10^{-3} \times 0,19395^2)$$

$$= (0,01475 \times 10^{-6} + 46,23 \times 10^{-6}) = \underline{46,25 \times 10^{-6} \text{ m}^4}$$

$$I_{xx \text{ total}} = \underline{174,17 \times 10^{-6} \text{ m}^4}$$

(7)

Calculate maximum bending moment (Bending stress = 158 MPa)

$$\frac{M}{I} = \frac{f}{y} \text{ where } M = \frac{f \times I}{y}$$

$$BM_{\text{max}} = \frac{165 \times 174,17 \times 10^6}{142,75}$$

$$BM_{\text{max}} = 201,32 \text{ kNm}$$

(3)

	<p><u>Calculate the self-weight of the beam</u></p> <p><u>Plate:</u> $7\,865\text{ kg/m}^3 \times 0,180 \times 0,018 \times 9,81 \times 10^{-3} = 0,25\text{ kNm}$</p> <p><u>Beam:</u> $65,1\text{ kg/m} \times 9,81 \times 10^{-3} = 0,638\text{ kNm}$</p> <p><u>Plate:</u> $7\,865\text{ kg/m}^3 \times 0,1024 \times 0,012 \times 9,81 \times 10^{-3} = 0,095\text{ kNm}$</p> <p>Total self-weight = 0,983 kNm</p>	(2)
	<p><u>Calculate the maximum point load the beam can carry</u></p> <p><u>Additional 15 kNm UDL</u></p> $BM = \frac{W l^2}{8} + \frac{W l^2}{8} + \frac{W l^2}{8}$ $201,32 = \frac{0,983 \times 6,25^2}{8} + \frac{35 \times 6,25^2}{8} + \frac{W \times 6,25^2}{8}$ $201,32 = 4,8 + 170,9 + 4,88 W$ $W = \frac{201,32 - 170,9}{4,88}$ $W = 6,23\text{ kN}$	(3) [20]

QUESTION 5

5.	<p><u>Calculate the direct shear on each bolt</u></p> <p>Force direct = Force / No of bolts</p> $F_{\text{direct}} = 28\text{ kN} / 2 = 14\text{ kN}$	(1)
	<p><u>Calculate the distance from the centroid to the furthest bolt</u></p> $r = 200 / 2 = 100\text{ mm}$	(1)
	<p><u>The direct load on the bolts due to the imposed load</u></p> $\Sigma cwm = \Sigma acwm$ $(28 \times 300) = (F_T \times 100 \times 2)$ $F_T = \frac{28 \times 300}{100 \times 2}$ $F_T = 42\text{ kN}$	(3)
	<p><u>The resultant load on each bolt</u></p> $F_R = 14 + 42 = 56\text{ kN}$	(2)

<p>Calculate the size of the bolts. (Shear stress = 105 MPa)</p> $F_R = \text{Shear stress} \times \text{Area of bolt}$ $\frac{\pi d^2}{4} = \frac{Fr}{\text{Shear stress}}$ $d = \sqrt{\frac{Fr \times 4}{\pi \times \text{stress}}}$ $d = \sqrt{\frac{56 \times 10^3 \times 4}{\pi \times 125}}$ $d = 23,88 \text{ mm}$ <p>Use 2M24 bolts</p>	<p>(4) [11]</p>
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QUESTION 6

All references taken from SANS 10100-1 (2000).

	<p>$F_{cu} = 25 \text{ MPa}$ $F_y = 250 \text{ MPa}$ Span = 5,25 m Density of reinforced concrete</p>	<p>Table 2 (4.1.5.1) Table 3 (4.1.5.2) Cl. 4.3.1.2 2 450 kg/m³</p>	
6.	<p><u>Determine the effective depth of the slab</u> Effective depth = span / 16 Effective depth = 5 250 / 16 Effective depth = 328,13 mm</p>	<p>Table 10 (4.3.6.2.1)</p>	(1)
	<p><u>Determine the overall depth</u> <i>Assume R16 main steel and cover of 25 mm.</i> Overall depth = 328,13 + 16/2 + 25 cover Overall depth = 361,13 mm (Use overall depth = 370 mm)</p>		(2)
	<p><u>Determine the design dead loads of the slab</u> Design dead load = Volume \times density \times 9,81 \times 10⁻³ \times 1,2Gn = 0,37 \times 1 \times 1 \times 2 450 kg/m³ \times 9,81 \times 10⁻³ \times 1,2 Gn Design dead load = 10,67 kNm Design imposed load = 7,5 kNm² \times 1 \times 1,6Qn Design imposed load = 12,0 kNm Total design load = 10,67 + 12,0 = 22,38 kNm</p>	<p>Cl.4.2.2.1 (Cl.4.2.2.1)</p>	(3)

	<p><u>Calculate bending moment maximum</u></p> $BM_{\max} = \frac{WL^2}{8}$ $BM_{\max} = \frac{22,67 \times 5,25^2}{8}$ $BM_{\max} = 78,11 \text{ kNm}$		(2)
	<p><u>Calculate value for 'K'</u></p> $K = \frac{BM}{f_{cu} b d^2}$ $K = \frac{78,11 \times 10^6}{25 \times 1\,000 \times 328,13^2}$ $K = 0,029$ <p>$K < K^1 = 0,156$ therefore only tension reinforcement required.</p>	4.3.3.4.1	(2)
	<p><u>Calculate distance of lever arm (Z)</u></p> $Z = d \left\{ 0,5 + \sqrt{0,25 - \frac{k}{0,9}} \right\} \leq 0,95d$ $Z = 328,13 \left\{ 0,5 + \sqrt{0,25 - \frac{0,029}{0,9}} \right\} \leq 0,95d$ $Z = 328,13 \{0,97\} \leq 0,95 \times 328,13$ $Z = 317,19 \text{ mm} \leq 311,72 \text{ mm} \leq 0,95d$	(Cl.4.3.3.4.1)	(2)
	<p><u>Calculate tension reinforcement</u></p> $A_s = \frac{M}{0,87 \times f_y \times z}$ $A_s = \frac{77,11 \times 10^6}{0,87 \times 250 \times 317,19}$ $A_s = 1\,117,72 \text{ mm}^2$ <p>Use R16 at 175 centres ($A_s = 1\,149 \text{ mm}^2$)</p>	(Cl.4.3.3.4.1)	(2)
	<p><u>Check for minimum main reinforcement</u></p> $\frac{100 A_s}{A_c} = \frac{100 \times 1\,149}{1000 \times 360}$ $= 0,32$ $0,24 = 0,32$ <p>The reinforcement is sufficient.</p>	Table 23 (Cl.4.11.4)	(2)

	<p><u>Determine secondary reinforcement</u></p> $\frac{100 A_s}{A_c} = 0,24$ $A_s = \frac{0,24 \times 1\,000 \times 360}{100}$ $A_s = 864 \text{ mm}^2$ <p>Use R12 at 125 centres ($A_s = 905 \text{ mm}^2$)</p>	Cl.4.11.4.3.1 & Table 23	(2) [18]
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Total: 100 marks

Glossary

A

Additives – a substance which can be added to something to enhance or alter its properties

Admixtures – cement mixtures comprising natural or manufactured chemicals or additives

Alloying elements – elements which are used to change the properties of other metals

B

Bleed water – the excess water in a concrete mix which pushes up to the surface and is part of a process called *bleeding*

Bod – clay lining

C

Cast iron – an alloy of iron and carbon produced from pig iron in a furnace

Charge – the furnace charge of iron-bearing materials, coke and flux

Coke – a solid fuel made by heating coal in the absence of air so that the volatile components are driven off

Cupola furnace – a cylindrical or shaft-like furnace for melting metals

Curing compound – a liquid substance applied as a surface coating on freshly cast concrete to prevent loss of water and heat

D

Decarburises – related to *decarburisation*, which is the process of decreasing carbon content in metalworking

Drying shrinkage – the change in volume of concrete when water leaves the concrete during the curing process

Ductility – the ability of a material to be drawn or plastically deformed without fracture

E

Efflorescence – a white, powdery deposit of salts which forms on the surface of concrete

Electric arc – an electrical discharge between two electrodes or points

Electrodes – conductors used to make contact with the parts of a circuit which are not metallic

F

Falsework – temporary structures (the props, beams and plates etc.) which support the formwork

Ferromanganese – an alloy of iron and manganese which usually contains about 80% manganese and is used in the manufacture of steel

Ferrous – containing iron

Friable – a substance that crumbles easily

Frustum – the opening of the cone

G

Galena – the principal ore and the most important compound of lead

Gypsum – a cement retarding agent

H

Hearth – the base or floor of a furnace or fireplace

Hessian – a woven fabric made from the jute plant or sisal fibres

Hydration – the chemical reaction between the cement and water that allows the cement to set.

Hydraulic – a material (in this case, cement) that reacts with water by hardening and setting

I

Ingots – a block of relatively pure metal, like a gold bar, which is so shaped to make it easier to process further

Interpolation – a method of calculating values using given data points

Intumescent paint – considered to be the lightest form of passive fire protection; the paint swells as a result of heat exposure and causes an increase in volume and a decrease in density

Ironmongery – the manufacturing of iron goods

M

Mill scale – a black scale of magnetic oxide of iron formed on iron and steel when heated for rolling, forging or other processing; unlike rust, which forms over a long period due to exposure to oxygen and moisture, scale forms on all steel and iron products that are hot-rolled

Mineral spirits – a petroleum-derived chemical compound

Molybdenum – a chemical element used to produce alloys

O

Oxidation – a chemical reaction involving the loss of electrons when a substance comes into contact with oxygen or another oxidising substance

Oxide film – a thin, protective deposit on the surface of a metal which has undergone oxidation

Oxidised roasting – thermal gas- and solid reactions involved in the process of converting metallic compounds into oxides

P

Pig iron – crude iron ore smelted in a blasted furnace

Plastic shrinkage cracking – when the rate of evaporation of moisture from the surface *exceeds* the rate at which moisture is being supplied

R

Refractory – a substance that is resistant to heat

Residuals – metal elements which are present but aren't purposefully included when working with a particular metal

Retarding agent – a chemical agent which slows down a chemical reaction

Rust-inhibitive primer – an anti-rust treatment which prevents the rusting and corrosion of metals

S

Sea coal – a mineral coal that is distinct from other types of coal and charcoal; used as a constituent of foundry sand

Slag – a by-product of smelting ores and other metals

Solder – a low-melting alloy or the act of joining with a solder, as in *soldering*

Spiegeleisen – a type of pig iron that is rich in manganese and carbon

Superplasticisers – additives used to produce high-strength concrete; also known as high-range water reducers

T

Truncated – shortened or cut off

Trunnion – a pin or pivot allowing a turning bucket to turn from one side to the other

Tuyeres – a nozzle through which air is forced into a smelter, furnace or forge

W

Welding – the art of joining metals by pressure after heating it to a plastic or semi-molten state, or by fusion of the metals alone.

Workability – in metalworking processes, the extent to which a material can be deformed without cracking; or the measure of ease with which concrete can be placed, compacted and finished without the segregation of the aggregate